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Simulation of space-borne tsunami detection using GNSS-Reflectometry applied to tsunamis in the Indian Ocean

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Abstract. Within the German-Indonesian Tsunami Early Warning System project GITEWS (Rudloff et al., 2009), a feasibility study on a future tsunami detection system from space has been carried out. The Global Navigation Satellite System Reflectometry (GNSS-R) is an innovative way of using reflected GNSS signals for remote sensing, e.g. sea surface altimetry. In contrast to conventional satellite radar altimetry, multiple height measurements within a wide field of view can be made simultaneously. With a dedicated Low Earth Orbit (LEO) constellation of satellites equipped with GNSS-R, densely spaced sea surface height measurements could be established to detect tsunamis. This simulation study compares the Walker and the meshed comb constellation with respect to their global reflection point distribution. The detection performance of various LEO constellation scenarios with GPS, GLONASS and Galileo as signal sources is investigated. The study concentrates on the detection performance for six historic tsunami events in the Indian Ocean generated by earthquakes of different magnitudes, as well as on different constellation types and orbit parameters. The GNSS-R carrier phase is compared with the PARIS or code altimetry approach. The study shows that Walker constellations have a much better reflection point distribution compared to the meshed comb constellation. Considering simulation assumptions and assuming technical feasibility it can be demonstrated that strong tsunamis with magnitudes ($M \geq 8.5$) can be detected with certainty from any orbit altitude within 15–25 min by a 48/8 or 81/9 Walker constellation if tsunami waves of 20 cm or higher can be detected by space-borne GNSS-R. The carrier phase approach outperforms the PARIS altimetry approach especially at low orbit altitudes and for a low number of LEO satellites.

1 Introduction

122 tsunami events have been reported for the Indian Ocean before the devastating Sumatra-Andaman or Sumatra tsunami occurred in 2004, 15 of them took by far more than 100 lives (National Geophysical Data Center, 2009). The high number of victims caused by tsunamis has desperately shown the need for a tsunami early warning system in the Indian Ocean. The waves of the Sumatra tsunami arrived at the coast within only 20 min after the earthquake. Any tsunami early warning system must fulfill the requirement to detect tsunami waves as soon as possible and with highest certainty to prevent false warnings. This means that tsunamis should be detected on the open sea within only 15 min after their generation by an earthquake or another triggering event like, e.g. a submarine slide (Brune et al., 2010). In the case of GITEWS an epicenter will be localized by a network of seismometers (Hanka et al., 2008) and GPS deformation monitoring stations (Babeyko et al., 2010; Falck et al., 2010) very quickly, but these do not provide any information if a tsunami has been generated or not. The ocean surface has therefore to be monitored for tsunami wave signatures. Pressure sensors, buoys and tide gauges are measuring sea surface height anomalies with very high accuracy in case a tsunami wave arrives at these sensors (Behrens et al., 2010). Even though the spatial distribution of these sensors has been selected carefully, the number of sensors is limited due to the high cost for development and deployment. The setup and maintenance of a large sensor network for all vulnerable regions worldwide would be extremely expensive.

Tsunami detection from space could be a valuable complement to ground based systems. Tsunamis are a global phenomenon and for global observations satellites are predestined. Tsunami waves can be detected from space as Ablain et al. (2006) have demonstrated for the Sumatra tsunami with radar altimeter (RA) data from TOPEX/POSEIDON,
2 The GNSS-Reflectometry method

In GNSS-R two altimetry approaches, the code altimetry and the carrier phase altimetry, can be distinguished. In the code altimetry or Passive Reflectometry and Interferometry System (PARIS) concept proposed by Martín-Neira (1993) the time delays between the direct and reflected signals are measured, which can be translated into absolute height of the reflecting surface at the specular point. In ground based GNSS reflection experiments above an artificial pond, height accuracies of 1 cm are obtained (Martín-Neira et al., 2002). Within the range of 500–1000 m above the reflecting water surface, height values with accuracies of 2 cm were found (Treuthaft et al., 2001). In a series of airplane and balloon experiments this technique was successfully applied in airborne campaigns (Garrison et al., 1998; Garrison and Katzberg, 2000; Rius et al., 2002; Cardellach et al., 2003; Ruffini et al., 2004; Nogués-Correig et al., 2007; Cardellach et al., 2009). In these experiments, sea level heights with accuracies of up to 5 cm as well as the relation between C/A-code correlation function and significant wave heights were determined using dedicated delay mapping GPS receivers. First observations of GNSS signal reflections from space-borne platforms were presented by Pavelyev et al. (1996) and Lowe et al. (2002). Gleason et al. (2005) report on first, promising results from the GNSS reflection experiment aboard the UK-DMC satellite. They succeeded in showing that bistatically reflected GPS signals are detectable from a LEO spacecraft and that signal characteristics are consistent with model results taking into account knowledge of sea state conditions at the places and times of the observations. For an intended in-orbit demonstrator mission PARIS IOD Martín-Neira et al. (2008) expect that the height accuracy of such a system is within 17 cm RMS for measurements over 100 km along track.

On the other hand, signatures of coherent GPS reflections at low elevation angles were observed in radio occultation data of the GPS/MET, SAC-C and CHAMP satellites (Beyerle and Hocke, 2001; Beyerle et al., 2002; Hajj et al., 2004). With a carrier phase interferometric approach the phase variation between direct and reflected signal can be translated into height variations of the reflecting surface. This only works for coherent reflections, which are limited to grazing elevation angles. In a ground based experiment from 800 m above the water level of lake Walchen, Bavarian Alps, the water surface height has been measured with an accuracy of 2 cm by using a modified commercial off-the-shelf (COTS) receiver (Helm et al., 2008). For phase measurements of the CHAMP satellite Cardellach et al. (2004) has achieved 70 cm height accuracy for GPS reflections from the Greenland ice sheet.

These two approaches have many advantages compared to conventional RA. Instead of RA a GNSS-R receiver aboard a LEO satellite receives reflections from many GNSS satellites at various elevation angles simultaneously. This results in a high spatial coverage of reflections. GNSS signals are

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Jason-1, ENVISAT, and GEOSAT Follow-On. There are only few RA satellites in space and they measure only in nadir direction. Their spatial coverage is therefore coarse and their temporal coverage is not high enough for tsunami early warning, because they do not transmit their data immediately to the ground. Martín-Neira (1993) has proposed that the GNSS-Reflectometry (GNSS-R) technique is applicable for ocean altimetry and therefore for tsunami detection from space (Martín-Neira et al., 2005). The technique uses GNSS signals that are reflected from water or ice surfaces as measurement signals. The travel time of the reflected signal compared to the direct one is a measure of the height of the reflecting surface and the reflected signal provides information about the properties of the surface (Fig. 1). GNSS-R is a passive measurement technique, which allows to build micro satellites and to arrange them as a LEO constellation intended for global and permanent altimetric and scatterometric ocean observation. In combination with a seismic sensor network and in addition to local sea surface observation sensors such a system would contribute sea surface height observations over areas of several thousand km² and would provide the only source of information in those regions where no local sensors exist.

In this simulation study we analyse various GNSS-R LEO constellations with respect to their tsunami detection performance. First, different constellation types are compared due to their global reflection point distribution. GPS, GLONASS and Galileo signals are assumed to be available and to be receivable without any principal or technical restrictions. The detection performance for each parameter combination is calculated empirically based on 100 independent simulation runs. Six tsunamis that occurred in the Indian Ocean triggered by earthquakes with different magnitudes are investigated. The orbit parameters altitude and inclination angle are varied to show their effects on the detection performance. Four assumed altimetric sensitivities and two different GNSS-R approaches are compared.

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**Fig. 1.** Illustration of bistatic GNSS reflection geometry. GNSS signals transmitted by GNSS satellites are reflected from the Earth’s surface and received by a dedicated GNSS-R receiver on board a LEO satellite. There are multiple reflection footprints forming several reflection point ground tracks within the field of view of the satellite (from Martín-Neira et al. (2002)).
available for free and continuously over many years which guarantees a reasonable and constant resource of measurement signals. The existing GPS is modernized by introducing new frequencies and signal codes and the GLONASS system will be completed in 2010. The number of GNSS satellites will increase due to the installation of Galileo to over 80 within the next decade. Further GNSS systems are scheduled by China (COMPASS/Beidou), Japan (QZSS) and India (IRNSS). GNSS-R is a passive measurement technique that has a low energy budget. It can therefore be applied to small affordable micro satellites like, e.g. MicroGEM (Brieß et al., 2009). Because of this, also satellite constellations are possible at comparably low costs, especially if COTS technology can be applied. With a satellite constellation the temporal coverage can be increased to fulfill given tsunami early warning requirements.

3 Reflection point calculation

In this study the GNSS-R LEO satellites of a constellation are represented by simulated two-line elements (TLE). To provide circular orbits, the eccentricity parameter is set to minimum. The satellite positions are calculated using a SDP4 orbit propagator (Hoots and Roehrich, 1980). GNSS satellites are considered as signal transmitters. GPS and GLONASS orbit parameters are obtained from IGS broadcast ephemerides (Dow et al., 2005) and positions are calculated according to NAVSTAR (1995). In case of Galileo, simulated two-line elements (TLE) are used because this constellation is not yet operating. Kepler orbit parameters for each satellite are created from known parameters like orbit altitude, inclination angle and constellation type assuming circular orbits. Satellite positions are calculated by applying a SDP4 orbit propagator (Hoots and Roehrich, 1980). Only the 27 nominal Galileo satellites are considered, the 3 spare satellites are neglected. This simulates a realistic situation with some operational satellites occasionally not available.

The reflection points on the WGS84 ellipsoid are calculated using the double differences method by Garrison et al. (1997). The geometrical ray path length of a signal transmitted from a GNSS satellite T with cartesian coordinates \((X_T, Y_T, Z_T)\), that touches the reflection point with polar coordinates \((\phi_S, \lambda_S)\) on the specular surface and that is received by a satellite \(L\) with the antenna coordinates \((X_L, Y_L, Z_L)\) is given by

\[
\rho_L(\phi_S, \lambda_S) = \sqrt{(X_L - X_S)^2 + (Y_L - Y_S)^2 + (Z_L - Z_S)^2} + \sqrt{(X_T - X_S)^2 + (Y_T - Y_S)^2 + (Z_T - Z_S)^2}
\]

with \(a\) and \(b\) as major and minor axes length of the WGS84 ellipsoid, respectively. For a given pair of LEO and GNSS satellite positions, this path length is minimized by varying the polar coordinates of the specular point \(S\). The reflection point geometry is shown in Fig. 2.

All GNSS reflection points from GNSS satellites that are visible from the LEO satellite position are taken into account. This means that all GNSS signals reflected from the WGS84 ellipsoid that would reach the LEO satellite positions geometrically are assumed to be technically receivable. The issue of technical feasibility is discussed in more detail in Sect. 5. For any LEO satellite of the constellation, reflection points are calculated with 1 min temporal resolution over a one day period. In this period there are about 2 repetitions of any GNSS system and it is long enough to cover all observable areas at least 2 times with a minimum of 4 LEO satellites evenly distributed on 2 orbit planes if a maximum footprint size is assumed.

4 Comparison of GNSS-R LEO constellations

According to Soulat et al. (2005) most seismic driven tsunamis occur within \(\pm 60^\circ\) latitude. A satellite constellation for tsunami detection should cover at least this area...
but also at higher latitudes tsunamis triggered by submarine slides may occur (Brune et al., 2009). A space-borne tsunami early warning system should also cover higher latitudes. There, a lower temporal coverage is sufficient because slides are very rare and they will trigger only local tsunamis. They are less dangerous because the regions in high latitudes are not densely populated.

For global ocean observations a LEO constellation must provide an optimum spatial coverage of GNSS reflections. Walker constellations (Walker, 1984) are designed to provide a good global coverage, but near the Equator this coverage is reduced. The meshed comb constellation (Jackson, 1998) solves this by arranging all satellites along the Equator at the same moment. A Walker constellation consists of different evenly distributed circular orbit planes that have the same inclination angle and a certain number of satellites that are evenly distributed on each orbit plane. The satellites on adjacent orbit planes are phase shifted to each other. For example a 18/3 constellation consists of 18 satellites that are distributed evenly on 3 orbit planes with 6 satellites on each plane. The 6 satellites follow each other every 60°. With 3 orbit planes the phase shift is 60°/3=20°. The satellites follow prograde orbits if the inclination angle is <90° and retrograde orbits if this angle is >90° (Larson and Wertz, 1995). In the meshed comb constellation, each satellite has its own orbit plane and the satellites on adjacent orbit planes move in opposite directions. This means that half of the satellites follow prograde orbits while the others follow retrograde orbits.

To find out which of these constellations should be used for global GNSS-R observations, the reflection point coverage of four different constellations with 18 satellites each at 900 km altitude are compared (Table 1). The number of reflection points within each grid cell of a 1° spaced spatial grid are counted and cumulated for each degree of latitude. Figure 3 shows the global latitude distributions of reflection points of the four constellations. The prograde and retrograde 18/3 Walker constellations show similar distributions with high values between ±60° latitude and a strong decrease when advancing to higher latitudes. In the combined 9/3 Walker constellations with different inclination angles the high latitudes are represented stronger and the low latitudes between ±40° show a very high number of reflection points. In contrast to this the meshed comb constellation overrepresents latitudes between 30° and 60° and the overall number of reflections is significantly lower as compared to the three Walker constellation types.

From a scientific point of view, only the reflection point coverage is relevant, but if a decision between these constellations has to be made, also other driving factors like the costs to install such a system in space may be considered. The number of satellites is the same for all scenarios but the number of necessary launches differs significantly. In the constellation prograde 18/3 constellation there are 6 satellites distributed on 3 orbit planes so that the entire constellation may be set up with 3 launches only. The same is true for the retrograde constellation, but retrograde orbits are much more expensive due to a much higher amount of fuel needed because the Earth's rotation moment has to be overcome during launch (Larson and Wertz, 1995). For the combined 9/3 constellations at least 6 launches are necessary. In the meshed comb constellation every satellite is on its own orbit plane and half of the satellites need to be in a retrograde orbit which means up to 18 launches to install such a constellation. Even though the number of launches may be reduced by using temporary altitude separation like it is demonstrated by the COSMIC constellation (Anthes et al., 2008) the prograde Walker constellation is most favorable and will be used throughout our simulation study.

### Table 1. Four constellations with 18 satellites at 900 km altitude but with different inclination angles and number of orbits. The constellation in row 3 consists is a combination of two 9/3 Walker constellations with different inclination angles.

<table>
<thead>
<tr>
<th>type</th>
<th>satellites</th>
<th>orbits</th>
<th>inclination</th>
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<td>9</td>
<td>3</td>
<td>80°</td>
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<tr>
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<td>9</td>
<td>9</td>
<td>60°</td>
</tr>
<tr>
<td></td>
<td>9</td>
<td>9</td>
<td>120°</td>
</tr>
</tbody>
</table>

![Fig. 3.](image-url)
5 Tsunami detection simulation

The Sumatra earthquake on 26 December 2004 had $M$ between 9.0 (National Geophysical Data Center, 2009) and 9.3 (Stein and Okal, 2005) and generated a tsunami that took more than 225,000 lives. On 28 March 2005 another strong earthquake of $M$ 8.5 near the island of Nias occurred. The earthquake and the tsunami that followed killed about 1300 people (ITIC, 2005). The histogram of historic tsunamis worldwide (Fig. 4) shows that events like the Sumatra and Nias tsunami are very rare, but their effects are dramatic. In this study we are interested in the question at which minimum magnitude of an earthquake, a tsunami can be sensed by a GNSS-R LEO constellation with certainty and what are the parameters that have a major impact on the detection performance.

The detection performances of various prograde Walker constellations are calculated for six tsunami events with different earthquake magnitudes (Table 2). These tsunamis are modeled using code TUNAMI-N2 (Imamura et al., 1997) which implements nonlinear shallow water equations and computes sea surface height anomalies. Tsunami model output comprises 70° to 110° longitude and −15° to 25° latitude with 5 arcmin spacing and 1 min temporal resolution over a period of 3 h after the earthquake. Initial condition for tsunami modeling is vertical sea floor displacement. For the Sumatra event, this has been obtained from the GPS-based earthquake source inversion by Hoechner et al. (2008), and the same technique has been applied for the Nias event. Geodetic inversions are especially adequate for tsunami modeling, since they are better able to capture the coseismic sea floor deformation due to an earthquake than traditional seismic inversions (Sobolev et al., 2007). The smaller earthquakes are computed using simpler one-fault models. Figure 5 shows sea surface heights 15 min after the earthquake for the four strongest tsunamis listed in Table 2.

To simulate a GNSS-R sea surface observation during the tsunami events, GPS, GLONASS and Galileo signals are used in combination. Their ephemerides were obtained for those days the tsunamis have happened. For the events that occurred in 1936 and 1941 the same ephemerides as for the Nias event are used. The reflection points form tracks of reflection measurements across the sea surface (Fig. 1). When passing over the tsunami model grid the measurable height anomalies are extracted from the grid cells at discrete time steps of 1 min, which is illustrated in Fig. 6.

Typically the waves of a strong tsunami in the deep sea region propagate at about 700 km/h and have a wavelength of 50–200 km but only about 50 cm of amplitude (NOAA/IOC/ITIC/LDG, 2002). Right after the earthquake the tsunami wave height is highest. While the energy induced by the earthquake spreads over an expanding tsunami area the maximum wave height decreases at a rate of about $1/\sqrt{r}$, and $r$ denoting the radius of the area, in case the water depth persists. When the tsunami waves reach the marine shelf region, the water depth decreases and the wave height increases. To detect tsunamis even within the deep sea region a GNSS-R system must detect waves of only a few decimeters.

The assumption that a GNSS-R system is able to detect tsunami waves of ≥20 cm (Germain and Ruffini, 2006) is technically very ambitious. There are many error sources that will influence the GNSS signal on its way from the transmitter through the atmosphere over the reflecting surface to the receiver. The GNSS position has to be known very precisely and the clock error of the transmitter has to be corrected. The direct and reflected signal path follow different ways through the ionosphere and especially the troposphere. Their impact on the GNSS signal is addressed in radio occultation research but not fully understood yet (Syndergaard, 2000; Gorbunov,

**Table 2.** Historical tsunami events in the Indian Ocean taken from a Murty and Rafiq (1991), b ITIC (2005), c National Geophysical Data Center (2009), and d Kanamori (2006). The events in rows 3 and 4 are the same but modeled with different magnitudes found in the literature. Colors correspond to those in Figs. 4 and 9.

<table>
<thead>
<tr>
<th>$M$</th>
<th>longitude</th>
<th>latitude</th>
<th>date</th>
<th>color</th>
</tr>
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<tbody>
<tr>
<td>9.1</td>
<td>95.8</td>
<td>3.3</td>
<td>26 Dec 2004</td>
<td>black</td>
</tr>
<tr>
<td>8.5</td>
<td>97.0</td>
<td>2.1</td>
<td>28 Mar 2005</td>
<td>red</td>
</tr>
<tr>
<td>8.1</td>
<td>92.5</td>
<td>12.5</td>
<td>26 Jun 1941</td>
<td>blue</td>
</tr>
<tr>
<td>7.6</td>
<td>92.5</td>
<td>12.5</td>
<td>26 Jun 1941</td>
<td>green</td>
</tr>
<tr>
<td>7.1</td>
<td>94.7</td>
<td>6.1</td>
<td>23 Aug 1936</td>
<td>orange</td>
</tr>
<tr>
<td>6.7</td>
<td>99.6</td>
<td>−1.6</td>
<td>10 Apr 2005</td>
<td>magenta</td>
</tr>
</tbody>
</table>
The figures show Cardellach 1993, Beyerle 2010, Heise et al. 2001, 2010. Ionospheric delays may be compensated if two signal frequencies can be used. Tropospheric effects are dominated by the water vapor content which is highly variable especially in tropical regions (Heise et al., 2006). The properties of the reflecting surface like roughness or to a lower extent temperature, salinity, polarity and permittivity also may contribute to the overall error (Cardellach, 2001). The reflected signal has to pass the troposphere and ionosphere again until it can be received by the GNSS-R satellite antenna. The signal strength and optical path length depend on the gain and the changing orientation of the antenna, respectively (Wu et al., 1993; Beyerle, 2009). Additionally, multipath effects may distort the reflected signal. All of these effects may reduce the altimetric accuracy that can be achieved with such a system. We are aware of these error sources but the complexity of their corrections is beyond the scope of this simulation study. The altimetric sensitivity is therefore a simulation assumption that describes the detectable minimum wave height after an exhaustive elimination of all error sources. In this simulation, tsunami wave anomalies of 20 cm are assumed, smaller anomalies are considered undetectable.

Fig. 5. Tsunami wave propagation simulations of the four strongest historic tsunamis in the Indian Ocean listed in Table 2. The figures show the situation after 15 min. The tsunami events in (c) and (d) are at the same location but modeled with different magnitudes.

Fig. 6. Schematic representation of a reflection point ground track (line) passing over a tsunami model grid between calculated reflection points (dots). Blue cells show negative, red cells show positive surface height anomalies. Those cells that are crossed by the track are marked bold. These cells are analyzed if their absolute height anomaly is higher than the altimetric sensitivity assumed for the GNSS-R system.
This assumption will be used for the code altimetry as well as for the phase altimetry approach for comparability reasons. We are aware that the altimetric accuracy for phase altimetry from space is still unknown. Each grid cell that will be passed by a reflection point track (Fig. 6) fulfilling this sensitivity criterion will be counted. All cells counted for each time step and within 3 h after the earthquake represent a tsunami detection series as shown exemplary in Fig. 7.

The moment when a tsunami occurs is a priori unknown and the configurations of the GNSS and LEO satellites are therefore unknown as well. Each detection series calculation is repeated 100 times with random starting times of the tsunami within the same day to account for this randomness. For each time period since the tsunami generation, the number of all simulation runs that show a detection the first time are cumulated. This cumulation of first detections over time forms a step function that can be interpreted in terms of detection probability. The time when this detection probability function reaches 100% is the maximum time this scenario needs to detect the tsunami with certainty. The detection performance increases with increasing slope of the probability function, i.e. it reaches absolute certainty earlier the higher the performance is.

Fig. 7. Detection series for a Sumatra tsunami detection simulation with a LEO GNSS-R 18/3 Walker constellation at 900 km with 60° inclination angle and GPS, GLONASS and Galileo as signal sources. The figure shows a periodicity of detections due to the series of LEO satellites along the same orbit passing over the tsunami region. The number of detections increases with time because the tsunami region increases and therefore the probability that a reflection ground track is passing through it. After 150 min the number of detections decreases because the overall wave height decreases and starts to drop below the assumed altimetric sensitivity limit.

6 Detection performance analyses

In this study we want to investigate which parameters have a significant impact on the detection performance of a LEO GNSS-R-based tsunami detection system. We compare the detection performance of scenarios with different LEO constellations, different tsunamis, different sensitivity assumptions and different orbit parameters. In these analyses the basic simulation assumption of no technical restrictions is retained and the altimetric sensitivity is set to 20 cm. The two different GNSS-R approaches with different antenna concepts mentioned above are also compared. GPS, GLONASS and Galileo together are taken as signal sources assuming they would have been available when the tsunamis occurred in reality. The differences between these GNSS systems with respect to their individual detection performance and their combination is addressed in Stosius et al. (2010).

6.1 Comparison of different constellation types

To compare the detection performances of the constellations listed in Table 1, their detection probabilities are calculated for the Sumatra tsunami. Here the combination of GPS, GLONASS and Galileo reflections is considered. The three Walker type constellation scenarios in Fig. 8 show a significantly better detection performance than the meshed comb constellation in Fig. 8 as expected from the reflection point distributions in Fig. 3. The detection performances of the prograde and retrograde 18/3 Walker constellations are very similar and show a certain detection within only 17 and 22 min, respectively. Although the detection probability of the two 9/3 constellations after 15 min is only 90%, a certain
Figure 9a and b shows detection results for a 18/3 and a 48/8 constellation scenario, respectively. In both cases the detection performance for the 9.1 magnitude event (Sumatra tsunami) is comparable. The detection performance will not increase significantly by having more satellites in the constellation. In the case of the 8.5 magnitude event (Nias tsunami) the performance within the first 15 min is very high (≥90%) for both scenarios. The probability for the 18/3 scenario reaches 100% after 45 min while this can be achieved by the 48/8 scenario within only 12 min, which clearly fulfills a 15 min detection requirement. The comparison of the medium events with M 8.1, 7.6, and 7.3 shows a remarkable difference in the detection performance between both scenarios. While all of these events have only about 30% detection probability after 15 min, in the 18/3 scenario they reach about 90%, 70%, and 60% within the same time for the 48/8 scenario, respectively. The 8.1 and 7.6 events differ only in magnitude but not in location. The 8.1 event will be detected with certainty nearly after the same time as the 7.6 event when taking the 18/3 scenario. For the 48/8 scenario the certain detection of the 8.1 event will be reached ~10 min earlier than that of the 7.6 event. During the last 10 decades the tsunami events in Indonesia that have taken the lives of more than 100 people were triggered by earthquakes with M ≥7.7 (National Geophysical Data Center, 2009). The simulations show that a 7.6 event can be detected within 35 min with certainty when using the 48/8 constellation, but this cannot be guaranteed with only a 18/3 constellation. An event with M 6.7 is too small in size and wave height and cannot be detected by any of these constellations, but such events are not really perilous.

6.3 Comparison of different orbit parameters

The orbit parameters “altitude” and “inclination angle” of the GNSS-R Walker constellations used in this study are varied to show their impact on the detection performance. The orbit altitudes chosen are 450 km, 600 km, 800 km, 1350 km, and 1800 km and the orbit inclinations vary between 40° and 80° with an increment of 10°. In addition, the number of satellites and the number of orbit planes are varied to create the six different constellation scenarios listed in Table 3. The combination of all parameters adds to 180 different scenarios. For each parameter combination, the detection performance analysis is carried out for the most devastating Sumatra and Nias tsunami, respectively. The detection time is crucial for early warning, and the shorter this time is, the more effective the early warning can be. The detection time is therefore classified by 15 min time intervals. For each calculation the time when the detection probability reaches 100% is sorted into one of the detection time classes 1: ≤15 min, 2: ≤30 min, 3: ≤45 min or 4: >45 min or not at all. The classified results for each parameter combination of each scenario are shown in Fig. 10 for the Sumatra and Nias tsunami, respectively.
In general, the detection time decreases with the total number of satellites of the scenario. The detection time is higher for lower orbit altitudes. This is obvious because the field of view and, therefore, the number of visible reflection ground tracks increases with orbit altitude. The detection time decreases with an increase of orbit inclination because the tsunamis observed here are close to the Equator and there the number of repeated observations increases when the orbit inclination is low. This may be different for tsunamis at higher latitudes which has not been investigated here. The classification of detection times in Fig. 10 shows clearly, that a 9/3 constellation is inappropriate for tsunami detection at all and also the 18/3 scenario only shows good results for low inclinations and high orbit altitudes. Although the results for the 24/8 and 36/6 scenarios look promising for the Sumatra event this can not be stated for the Nias event. The 36/6 detection result for the Nias event looks very similar to the 18/3 result of the Sumatra event, which means that the number of satellites and orbit planes must be doubled to achieve similar detection results for the Nias tsunami. With a 48/8 constellation nearly the same detection results can be expected for both events and with the 81/9 scenario a certain detection within 15 min can be achieved for both events for all altitude and inclination combinations.

### Table 3. Number of satellites and orbit planes for six GNSS-R Walker constellation scenarios.

<table>
<thead>
<tr>
<th>num. of satellites</th>
<th>9</th>
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<th>24</th>
<th>36</th>
<th>48</th>
<th>81</th>
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<td>18/3</td>
<td>24/8</td>
<td>36/6</td>
<td>48/8</td>
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</tr>
</tbody>
</table>

### 6.4 Comparison of different altimetric sensitivity assumptions

To analyse the performance of the tsunami detection with respect to the altimetric sensitivity, different assumptions are made. In Fig. 11 the detection probability of the 18/3 and the 48/8 scenario is calculated for the four strongest tsunamis in Table 2. The altimetric sensitivity is varied between 10 cm, 20 cm, 50 cm, and 100 cm. In the case of the Sumatra tsunami (Fig. 11a and e) in both scenarios no significant difference between the results of all four sensitivities
can be found, because the detectable tsunami wave heights of this event are $\geq 100$ cm within the first 20 min after the earthquake. For the 18/3 scenario of the Nias event (Fig. 11b) the results for a sensitivity of 10 cm, 20 cm, and 50 cm are similar within the first 15 min. After that the 50 cm probability function starts to differ slightly from that of the 10 and 20 cm sensitivity. The detection performance of the 100 cm sensitivity is significantly lower. It reaches only 60% after 15 min and 100% only after 151 min. This can not be observed in the 48/8 scenario of the Nias event (Fig. 11f). The detection probability stays below the 15 min requirement for the 10, 20, and 50 cm sensitivity and is very high (−90%) for the 100 cm sensitivity. The tsunami event of 1941, which is calculated for both scenarios with $M$ 8.1 (Fig. 11c and g) and with $M$ 7.6 (Fig. 11d and h) shows significant differences in the detection performance between the four sensitivity assumptions. For both scenarios the probabilities start to diverge after 5 to 10 min. In the 18/3 scenario 100% detection probability is not reached within the 3 h period after the earthquake with any of the sensitivity assumptions. With the 10 cm sensitivity only 40% and 30% can be reached within 15 min in the 8.1 and 7.6 magnitude event, respectively. The performance difference between 10 cm and 100 cm sensitivity is up to −40% for the 8.1 event and up to 85% for the 7.6 event. In the case of the 48/8 scenario the detection performance for the 8.1 event (Fig. 11g) is very high. The tsunami would be detected within 15 min for the 10 cm sensitivity and 45 min for the 100 cm sensitivity, respectively. For the 7.6 event (Fig. 11h) the detection performance of the 10 and 20 cm sensitivity is still good but for the 50 cm sensitivity the certain detection takes up to 75 min. The 100 cm sensitivity will not reach more than 35% which is not sufficient for tsunami detection at all because this means that only about 1 of 3 tsunamis is detectable. The overall result of this analysis is that at least a 48/8 scenario is necessary to fulfill the 15 min requirement for the detection of a strong or medium tsunami and that the altimetric sensitivity should be at least 20 cm to detect a tsunami with $M \geq 7.6$.

6.5 Comparison of different GNSS-R altimetry approaches

The PARIS (Martín-Neira, 1993) or code altimetry approach uses GNSS signals that are scattered due to the roughness of the reflecting surface. It requires an uplooking right handed circular polarized (RHCP) antenna for the direct GNSS signals and a downlooking left handed circular polarized (LHCP) antenna to retrieve the reflections. The signal-to-noise ratio (SNR) of scattered GNSS signals is very low and the antenna gain must therefore be very high ($\sim 23$ dB (Martín-Neira et al., 2008)). To retrieve several scattered reflections from different directions simultaneously, a high gain antenna with beam steering is necessary, which is technically challenging. From bistatic model theory, e.g. (Valenzuela, 1978; Voronovich, 1994), it is known that for reflections on sea surfaces at small elevation angles below $\sim 20^\circ$–$30^\circ$, effects like trapping or Bragg scattering start to dominate the scattering process. In this case the SNR becomes very low, so that this approach is, therefore, applicable only for reflections with higher elevation angles.

In carrier phase altimetry the interference between direct signals and coherent reflections are used to determine the height or height variation of the reflecting surface. Coherent reflections can only be observed at low elevation angles with low gain (10–20 dB) RHCP antennas (Beyerle and Hocke, 2001) directing to horizon. This antenna configuration is applied in radio occultation experiments like on CHAMP, GRACE or COSMIC/Formosat-3 (Wickert et al., 2009). In these satellite missions one or two antennas looking in aft and/or forward direction are used.
To compare these two approaches, the detection simulation is repeated for two different antenna configuration scenarios. The PARIS approach is applied with a downlooking omnidirectional antenna assuming that the antenna can be steered to all directions from where reflections can be retrieved. The elevation angle of receivable signals is restricted to $\geq 30^\circ$. For the carrier phase approach a typical radio occultation configuration with a fore and aft looking antenna with $120^\circ$ opening angle is chosen. This configuration is recommended in a phase A study of the planned MicroGEM satellite. This micro satellite is designed for radio occultation, carrier phase reflectometry and gravimetry using precise orbit determination (POD), satellite laser ranging (SLR) and very-long baseline interferometry (VLBI) in combination (Brieve et al., 2009). In this simulation the elevation angle for this approach is restricted to $< 10^\circ$.

Figure 12 shows the detection probability plots for both GNSS-R altimetry approaches when applied to the Sumatra tsunami. Different LEO GNSS-R Walker constellations at different orbit altitudes with $60^\circ$ inclination angle are included. As stated above the detection performance increases with the number of satellites in the constellation and with orbit altitude for both approaches. Regarding the first 15 min after the earthquake both approaches perform very similar. For orbit altitudes up to 900 km and the scenarios with up to 48 satellites the phase altimetry probability functions are steeper than the PARIS functions, which indicates that in these cases the detection performance is better because the tsunami will be detected earlier with a higher degree of certainty. At higher orbits or with a higher number of satellites both approaches perform similar and in some cases the PARIS approach performs slightly better. Consequently...
both concepts perform similar at high orbits. At low orbits the phase altimetry approach should be preferred. Only the PARIS concept results for the 81/9 scenario with ≥1350 km altitude stay below the 15 min detection time requirement. Despite of this exception none of these two concepts is able to fulfill the 15 min requirement alone, and because of that a GNSS-R tsunami detection system should combine both approaches.

7 Conclusions

A tsunami detection simulation study has been carried out with GNSS-R as detection system that is able to measure sea surface height anomalies induced by tsunamis. As the Sumatra tsunami has shown, a limit of 15 min detection time is required for such a tsunami detection system. In this study GPS, GLONASS and Galileo signals are assumed to be available and GNSS-R receivers are applicable aboard LEO satellites in a constellation. In a first step a meshed comb and several types of Walker constellations are compared with respect to their global reflection point distribution. It can be shown that the Walker constellations outperform the meshed comb constellation. The simulations consider prog-grade Walker constellations as most appropriate for global GNSS-R tsunami detection. The detection performance is calculated based on first time detections of 100 independent detection series. The detection performance for several parameter combinations is analysed. The parameters taken into account are orbit altitude, inclination angle, number of satellites and number of orbit planes of the GNSS-R LEO constellation as well as the altimetric sensitivity and the GNSS-R altimetry approach. Tsunami wave heights are modeled for six historical tsunamis in the Indian Ocean. The analyses show that very strong tsunamis can be detected within 15 min with 18 LEO satellites only at special orbit parameter combinations and weaker tsunami events can not be detected adequately even with 48 satellites. The detection performance in general increases with the number of satellites and the orbit altitude. For tsunamis in the Indian Ocean low inclination angles are advantageous but a global detection system should operate at least up to 60° latitude. With a 48/8 constellation and at least 20 cm altimetric sensitivity strong and medium tsunamis can be detected within 15 to 25 min. These results only hold true under the assumption that all reflections that occur geometrically are receivable technically and that errors can be reduced to obtain an altimetric sensitivity adequate for tsunami detection. In reality there are many principal and technical drawbacks. Two different GNSS-R altimetry approaches with different antenna configurations exist. The simulations show that the carrier phase approach outperforms the PARIS or code altimetry approach especially at low orbit altitudes and for a low number of LEO satellites. Both approaches alone do not fulfill the 15 min requirement and, therefore, any GNSS-R tsunami detection system should combine both approaches to build an effective operational tsunami detection system. In addition there must be an efficient downlink concept to transmit the data immediately. This requires some kind of on board processing, a network of downlink stations (ideally located near vulnerable coastal regions) and/or a communication satellite network as well as a tsunami early warning center to evaluate the data and to mitigate the warning. A GNSS-R system like the one proposed here would not be designed only for tsunami detection alone but for GNSS-R observations of water, ice and land as well as for atmospheric sounding, i.e. radio occultation. This can be achieved with similar or the same GNSS-R hardware, which makes GNSS-R a very versatile remote sensing technique.

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