Free core nutation observed by VLBI

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ABSTRACT

Aims. The signature of free core nutation (FCN) is found in the motion of the celestial intermediate pole in the celestial reference frame and in the resonance behaviour of the frequency-dependent Earth tidal displacement in its diurnal band. We focus on estimation of the FCN parameters, i.e. the period and amplitude.

Methods. We run several global adjustments of 27 years of very long baseline interferometry (VLBI) data (1984.0–2011.0) to determine the FCN period from partial derivatives of the VLBI observables with respect to the FCN as contained in the nutation of the celestial intermediate pole and in the solid Earth tidal displacement in the diurnal band. Finally, we estimate the FCN period by a global adjustment from both phenomena simultaneously, which has not been done before.

Results. We find that our estimate of the FCN period of $-431.18 \pm 0.10$ sidereal days slightly deviates from the conventional value of $-431.39$ sidereal days. Additionally, we present our empirical model of the FCN with variable amplitude and phase compatible with the estimated period.

Key words. publications, bibliography – methods: data analysis – techniques: interferometric – astrometry – reference systems – Earth

1. Introduction

The rotating Earth has several free rotational modes, one of them being free core nutation (FCN). This normal mode is caused by the fact that the ellipsoidal liquid core inside the visco-elastic Earth’s mantle rotates around an axis which is slightly misaligned with the axis of the mantle. In the celestial reference frame (CRF) it is visible as a retrograde motion of the Earth figure axis with a period of about 431 days and has an amplitude of about 100 microarcseconds (Mathews et al. 2002; Vondrák et al. 2005; Lambert & Dehant 2007). Since there are no models available which could predict this free motion with its time-varying excitation and damping, it is not included in the precession-nutation model of the Earth axis adopted in the current International Earth Rotation and Reference Systems Service (IERS) conventions 2010 (Petit & Luzum 2010). Therefore, the dominant part of the residuals between the direction of the celestial intermediate pole (CIP) in the CRF as observed by very long baseline interferometry (VLBI) and the direction modelled by the very accurate precession-nutation model, adopted by the International Astronomical Union (IAU), IAU 2006/2000A (Mathews et al. 2002; Capitaine et al. 2003) is caused by the FCN. In the terrestrial reference frame (TRF) the motion is observed at a period of about one day and is designated as nearly diurnal free wobble (NDFW). At this frequency, i.e. in the diurnal band, there is a strong resonance between the NDFW and the solid Earth tidal displacement. In this work we focus on estimation of the FCN period from the nutation motion of the Earth’s axis in space and also from the resonance behaviour in the diurnal tidal band.

Fig. 1. Fourier spectrum of CPO ($dX + idY$) estimated with software VieVS with respect to the IAU 2006/2000A precession-nutation model.

There have been several investigations on the FCN period from VLBI data in the past. For example, spectral and wavelet techniques have been applied to the celestial pole offsets (CPO) to estimate the period and amplitude of the FCN. It turned out that the obtained spectrum contains broad double peaks in the vicinity of the expected FCN signal (e.g. Malkin & Miller 2007) or an apparently varying period between $-425$ to $-450$ days (Schmidt et al. 2005). Figure 1 shows the spectrum of the CPO with a double peak around $-410$ and $-470$ days as obtained by fast Fourier transformation of our VLBI estimates from 1984.0 to 2011.0.

Earth rotation theory, as nowadays widely accepted, predicts one strong oscillation with a stable period. The apparent change of the period, which is seen in the spectral analysis of CPO, is attributed to a variable phase and amplitude of the rotation. The non-rigid Earth nutation model of Mathews et al. (2002) is the basis for the current IAU 2000A nutation model.
It predicts an FCN period between \(-429.93\) and \(-430.48\) solar days. The time stability of the FCN period was first examined by Roosbeek et al. (1999), who found a period between \(-431\) and \(-434\) sidereal days from analysing several sub-intervals of the VLBI time series. They used the transfer function by Wahr (1979), which expresses the ratio between rigid and non-rigid amplitudes of nutation terms at their frequencies and which accounts for a resonance effect of the FCN at forced frequencies. This proposal of Roosbeek et al. (1999) for an indirect estimation of the FCN period was extended by Vondrák et al. (2005) by applying the transfer function given in Mathews et al. (2002) to the CPO obtained by a combined VLBI/global positioning system (GPS) solution, yielding a stable value of \(-430.55 \pm 0.11\) solar days \((-431.73 \pm 0.11\) sidereal days). Lambert & Dehant (2007) extended the work of Vondrák et al. (2005) by investigating the CPO time series from 1984.0 to 2006.0 provided by several VLBI analysis centres. They concluded that the resonant period stays stable within half a day with an average value of \(-429.75 \pm 0.42\) solar days \((-430.93 \pm 0.42\) sidereal days).

All these studies estimated the FCN period “a posteriori”, i.e. by analysing the CPO time series. In this work we use a common adjustment of the VLBI measurements for the estimation of the FCN period within a so-called global solution, where partial derivatives of the group delay \(\tau\), i.e. of the primary geodetic observable of the VLBI technique, with respect to the FCN period are set up.

2. FCN in nutation motion

The FCN components \(X_{\text{FCN}}\) and \(Y_{\text{FCN}}\) in a nutation model can be described by a time-varying sinusoidal representation:

\[
X_{\text{FCN}} = A_C \cos(\sigma_{\text{FCN}}) - A_S \sin(\sigma_{\text{FCN}}),
Y_{\text{FCN}} = A_S \cos(\sigma_{\text{FCN}}) + A_C \sin(\sigma_{\text{FCN}}),
\]

where \(A_C\) and \(A_S\) are the amplitudes of the cosine and sine term, \(t\) is the time given since J2000.0, and \(\sigma_{\text{FCN}}\) is the frequency of FCN in the CRF.

In order to obtain the partial derivatives of the VLBI observable with respect to the FCN period and amplitude, the Eqs. (1) for FCN offsets are included into the description of the celestial motion of the CIP. The FCN offsets from Eqs. (1) are simply added to the celestial pole coordinates \(X_{\text{IAU}}\) and \(Y_{\text{IAU}}\) following the IAU 2006/2000A precession-nutation-model:

\[
X = X_{\text{FCN}} + X_{\text{IAU}},
Y = Y_{\text{FCN}} + Y_{\text{IAU}}.
\]

This addition is practically equivalent to a multiplication of the transformation matrix \(Q_{\text{IAU}}\) (Pett & Luzum 2010):

\[
Q(t) = \frac{dQ(t)}{d\sigma_{\text{NDFW}}} Q(t)_{\text{IAU}} = \begin{bmatrix}
1 & 0 & X_{\text{FCN}} \\
0 & 1 & Y_{\text{FCN}} \\
-X_{\text{FCN}} & -Y_{\text{FCN}} & 1
\end{bmatrix} Q(t)_{\text{IAU}}.
\]

For the combined estimation of the FCN period \(P_{\text{FCN}}\) with the solid Earth tidal displacement, we express the FCN period in the CRF with the frequency of NDFW in the TRF \(\sigma_{\text{NDFW}}\). The transformation is done by a basic relationship between frequencies in the terrestrial and celestial reference systems:

\[
P_{\text{FCN}} = \frac{2\pi}{\sigma_{\text{FCN}}} = \frac{1}{1 - \sigma_{\text{NDFW}} \cdot sd}.
\]

It follows that \(\sigma_{\text{FCN}} = 2\pi \cdot sd(1 - \sigma_{\text{NDFW}})\) with \(sd = 1.002737909\) giving the number of sidereal days per one solar day. The partial derivatives of \(dQ\) with respect to the NDFW frequency \(\sigma_{\text{NDFW}}\) then read

\[
\frac{d\sigma_{\text{FCN}}}{d\sigma_{\text{NDFW}}} = \begin{bmatrix}
0 & 0 & -2\pi \cdot sd \cdot t \cdot T_x \\
0 & 0 & -2\pi \cdot sd \cdot t \cdot T_y \\
2\pi \cdot sd \cdot t \cdot T_x & 2\pi \cdot sd \cdot t \cdot T_y & 0
\end{bmatrix},
\]

where \(T_x\) and \(T_y\) denote \(\sigma_{\text{FCN}}\) and \(\sigma_{\text{NDFW}}\) as determined empirically from the solid Earth tidal displacement, we express the FCN frequency in the CIP with the frequency of NDFW in the TRF \(\sigma_{\text{NDFW}}\).

The partial derivatives of \(dQ\) with respect to the amplitude of the cosine term \(A_C\) are easily created as

\[
\frac{d\sigma_{\text{FCN}}}{dA_C} = \begin{bmatrix}
0 & 0 & \cos(\sigma_{\text{FCN}}) \\
0 & 0 & -\sin(\sigma_{\text{FCN}}) \\
\sin(\sigma_{\text{FCN}}) & -\cos(\sigma_{\text{FCN}}) & 0
\end{bmatrix},
\]

and the partial derivatives of \(dQ\) with respect to the amplitude of the sine term \(A_S\) read

\[
\frac{d\sigma_{\text{FCN}}}{dA_S} = \begin{bmatrix}
0 & 0 & -\sin(\sigma_{\text{FCN}}) \\
0 & 0 & \cos(\sigma_{\text{FCN}}) \\
\sin(\sigma_{\text{FCN}}) & -\cos(\sigma_{\text{FCN}}) & 0
\end{bmatrix}.
\]

The incorporation of the partial derivatives of \(dQ\) into the partial derivative of the whole basic VLBI model follows as

\[
\frac{\partial \tau}{\partial \sigma_{\text{NDFW}}} = k(t) \cdot \frac{d\sigma_{\text{FCN}}}{d\sigma_{\text{NDFW}}} Q(t)_{\text{IAU}} \cdot R(t) \cdot W(t) \cdot b(t),
\]

where \(k\) is the source unit vector defined in the barycentric celestial reference system, \(Q, R, W, b\) are the transformation matrices between the CRF and TRF due to nutation, Earth rotation angle, and polar motion respectively, and \(b\) is the baseline vector between two VLBI stations expressed in the terrestrial reference system. In the same way one gets the partial derivative of the VLBI model with respect to the amplitude of the cosine and sine term.

2.1. Analysis of the VLBI measurements

We estimated the FCN period from the motion of the CIP in the geocentric celestial reference system (GCRS) as a global parameter in a common adjustment (global solution) of 3360 24-h sessions of the International VLBI Service for geodesy and astrometry (IVS; Schuh & Behrend 2012). These sessions fulfil two criteria: a) the network is built with at least three stations; and b) the a posteriori sigma of unit weight obtained from a single-session adjustment does not exceed the value of 2. The whole analysis of 4.6 million observations from 1984.0 to 2011.0 was done with the Vienna VLBI Software (VieVS; Böhm et al. 2012). The theoretical time delays were modelled according to recent IERS Conventions 2010, with the exception of applying a priori corrections on station coordinates due to non-tidal atmosphere loading (Petrov & Boy 2004), which is a common procedure in VLBI analysis. The celestial motion of the CIP was modelled according to Eqs. (2). The FCN offsets were taken from the model by Lambert (2007), who uses the a priori FCN period of \(-431.39\) sidereal days by Mathews et al. (2002) and provides the amplitude terms \(A_C\) and \(A_S\) as determined empirically from the CPO in the IERS EOP05 C04 combined series. The values of \(A_C\) and \(A_S\) are given in yearly steps and the amplitudes during the year are obtained by linear interpolation.
Table 1. Period of the FCN estimated in solutions S1 and S2, together with constant corrections to the a priori amplitudes of the FCN from Lambert (2007) and to the annual and semi-annual nutation terms given in the IAU 2000A model.

<table>
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</thead>
<tbody>
<tr>
<td>S1</td>
<td>$-431.17 \pm 0.09$</td>
<td>$64.6 \pm 1.0$</td>
<td>$34.0 \pm 1.2$</td>
<td>$-4.6 \pm 1.0$</td>
<td>$14.9 \pm 0.9$</td>
<td>$-19.3 \pm 0.9$</td>
<td>$-8.9 \pm 0.9$</td>
</tr>
<tr>
<td>S2</td>
<td>$-431.18 \pm 0.09$</td>
<td>$64.1 \pm 1.0$</td>
<td>$33.9 \pm 1.2$</td>
<td>$-4.6 \pm 1.0$</td>
<td>$14.9 \pm 0.9$</td>
<td>$-19.3 \pm 0.9$</td>
<td>$-8.9 \pm 0.9$</td>
</tr>
</tbody>
</table>

The VieVS was extended with partial derivatives of the measured time delay with respect to the FCN period as described in Eq. (9) and to the FCN amplitude. Furthermore, partial derivatives with respect to the annual and semi-annual harmonic terms in the nutation motion were added.

Two solutions were run with the same a priori parameterisation. In both solutions a new TRF and a new CRF were estimated as global parameters by applying no-net-translation and no-net-rotation conditions with respect to VTRF2008 (Böckmann et al. 2010) and ICRF2 (Fey et al. 2009) respectively. Clock parameters, zenith wet delays, tropospheric parameters, and Earth rotation parameters were session-wise reduced.

- In solution S1 the FCN period together with the constant corrections to the cosine and sine amplitude terms were estimated as global parameters.
- Solution S2 is identical to solution S1, but additional cosine and sine amplitudes of the annual and semi-annual harmonic terms in nutation were determined.

Due to the non-linear relationship of the FCN period in the FCN offsets, several iterative solutions had to be run. In solution S1 the period of FCN in the global solution is estimated as $-431.17 \pm 0.09$ sidereal days and the amplitude corrections are $64.6 \pm 1.0 \mu$as for the cosine term and $34.0 \pm 1.2 \mu$as for the sine term. The resulting FCN period obtained from solution S2 ($-431.18 \pm 0.09$ sidereal days) is almost identical to the estimates from solution S1. The values of the remaining absolute amplitudes of the annual and semi-annual terms (in addition to the values included in the IAU 2000A nutation model) are $15.6 \pm 1.0 \mu$as and $21.3 \pm 1.0 \mu$as respectively. The amplitude value from the cosine and sine terms is obtained in the usual way as $A = \sqrt{(A_C^2 + A_S^2)}$. The comparison of solutions S1 and S2 shows that an additional estimation of corrections to the annual and semi-annual nutation terms does not influence the FCN period determination. The FCN period from solutions S1 and S2 with the constant corrections to the cosine and sine amplitude terms for the FCN and the annual and semi-annual nutation terms are summarised in Table 1.

3. FCN in solid Earth tides

The FCN affects the solid Earth tides in their diurnal band, causing a strong resonance effect. The Love and Shida numbers, i.e. the proportionality parameters between the tide-generating potential and the tidal displacement, for the diurnal tidal waves in the vicinity of the NDFW period depend on frequency, see e.g. Krásná et al. (2013). We use the resonance effect in these tidal waves to determine the FCN period directly from VLBI analysis, which was first done by Haas & Schuh (1996).

Love and Shida numbers in the diurnal band can be represented by a resonance formula as a function of the tidal excitation frequencies with the frequency of Chandler wobble $\sigma_{CW}$, of the NDFW $\sigma_{NDFW}$, and of the free inner core nutation (FICN) $\sigma_{FICN}$ (Mathews et al. 1995; Petit & Luzum 2010):

$$L_4 = L_0 + \frac{L_{CW}}{\sigma_{CW}} + \frac{L_{NDFW}}{\sigma_{NDFW}} + \frac{L_{FICN}}{\sigma_{FICN}},$$

where $L_4$ is a generic symbol for the frequency-dependent Love $(h)$ and Shida $(l)$ numbers, with $L_0$, $L_{CW}$, $L_{NDFW}$, and $L_{FICN}$ as resonance coefficients (Petit & Luzum 2010). In the terrestrial diurnal band only the periods of the NDFW and the FCN can be found. The principal resonance comes from the NDFW with a resonance strength factor ($L_{NDFW} = 0.18053 \times 10^{-3}$) 100 times larger than that of the FICN ($-0.18616 \times 10^{-5}$). The partial derivative of the station displacement in the local coordinate system with respect to the NDFW frequency follows from the frequency-dependent corrections $\delta d_l$ to the displacement vector, which can be written as (Petit & Luzum 2010)

$$\delta d_l = -3 \frac{5}{24\pi} H_l \left\{ \frac{1}{2} \delta h_l \sin 2\Phi \sin (\theta_l + \Lambda) \hat{r} + \frac{1}{2} \delta l \sin \Phi \cos (\theta_l + \Lambda) \hat{e} + \delta l \cos 2\Phi \sin (\theta_l + \Lambda) \hat{n}\right\},$$

where $\delta h_l$ and $\delta l$ are the corrections to the constant values of Love and Shida numbers $h_2$ and $l_2$, which equal to 0.6078 and 0.0847 respectively, according to Petit & Luzum (2010); $H_l$ is the amplitude of the tidal term with frequency $f$ using the defining convention by Cartwright & Tayler (1971); $\Phi$ and $\Lambda$ are the geocentric latitude and longitude of the station; $\theta_l$ is the tide argument for tidal constituent with frequency $f$; $\hat{r}$, $\hat{e}$, $\hat{n}$ are unit vectors in radial, east, and north direction respectively.

The partial derivative of the basic VLBI model with respect to the NDFW frequency contained in the solid Earth tides, i.e. in the displacement of stations building a baseline, is in its general form given by Eq. (12):

$$\frac{\partial r}{\partial \sigma_{NDFW}} = k(t) \cdot Q(t) \cdot R(t) \cdot W(t) \cdot \frac{\partial b(t)}{\partial \sigma_{NDFW}}.$$

For the analysis of the VLBI measurements, the same a priori modelling and parameterisation as described in Sect. 2.1 were applied. The FCN period was obtained together with a simultaneously estimated TRF and CRF. After four iterative runs the period stayed stable at $-431.23 \pm 2.44$ sidereal days.

4. Simultaneous estimation of the FCN period from solid Earth tides and nutation

In previous sections the presence and effects of the FCN in the solid Earth tides and in the nutation of the CIP were treated separately. In this part we introduce a rigorous determination of the FCN period, where the partial derivative of the observation equation contains changes in both parameters (nutation matrix and
Table 2. Cosine and sine amplitude terms of the FCN model determined in yearly steps within global solutions of VLBI measurements.

<table>
<thead>
<tr>
<th>Year</th>
<th>Ac [μas]</th>
<th>As [μas]</th>
<th>Year</th>
<th>Ac [μas]</th>
<th>As [μas]</th>
<th>Year</th>
<th>Ac [μas]</th>
<th>As [μas]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1986.0</td>
<td>−256.6 ± 9.8</td>
<td>−162.6 ± 9.8</td>
<td>1994.0</td>
<td>−108.3 ± 2.6</td>
<td>19.7 ± 2.6</td>
<td>2002.0</td>
<td>98.4 ± 2.0</td>
<td>−82.9 ± 2.0</td>
</tr>
<tr>
<td>1987.0</td>
<td>−261.1 ± 9.1</td>
<td>−104.3 ± 9.1</td>
<td>1995.0</td>
<td>−105.2 ± 2.1</td>
<td>17.7 ± 2.2</td>
<td>2003.0</td>
<td>104.5 ± 1.9</td>
<td>−71.0 ± 1.9</td>
</tr>
<tr>
<td>1988.0</td>
<td>−216.3 ± 9.1</td>
<td>−84.9 ± 9.1</td>
<td>1996.0</td>
<td>−99.4 ± 2.2</td>
<td>18.3 ± 2.2</td>
<td>2004.0</td>
<td>109.0 ± 1.8</td>
<td>−56.2 ± 1.7</td>
</tr>
<tr>
<td>1989.0</td>
<td>−180.5 ± 7.5</td>
<td>−45.6 ± 7.5</td>
<td>1997.0</td>
<td>−89.9 ± 2.3</td>
<td>16.9 ± 2.3</td>
<td>2005.0</td>
<td>111.9 ± 2.0</td>
<td>−23.0 ± 2.0</td>
</tr>
<tr>
<td>1990.0</td>
<td>−160.0 ± 6.1</td>
<td>−6.3 ± 6.1</td>
<td>1998.0</td>
<td>−76.0 ± 2.4</td>
<td>2.8 ± 2.4</td>
<td>2006.0</td>
<td>121.1 ± 1.8</td>
<td>25.4 ± 1.8</td>
</tr>
<tr>
<td>1991.0</td>
<td>−145.3 ± 5.0</td>
<td>19.8 ± 5.0</td>
<td>1999.0</td>
<td>−39.8 ± 2.7</td>
<td>−32.2 ± 2.8</td>
<td>2007.0</td>
<td>150.3 ± 1.7</td>
<td>75.5 ± 1.7</td>
</tr>
<tr>
<td>1992.0</td>
<td>−146.3 ± 4.0</td>
<td>26.7 ± 3.9</td>
<td>2000.0</td>
<td>8.3 ± 2.6</td>
<td>−82.3 ± 2.6</td>
<td>2008.0</td>
<td>162.1 ± 1.8</td>
<td>134.0 ± 1.8</td>
</tr>
<tr>
<td>1993.0</td>
<td>−128.7 ± 3.0</td>
<td>23.5 ± 3.0</td>
<td>2001.0</td>
<td>57.7 ± 2.3</td>
<td>−102.4 ± 2.3</td>
<td>2009.0</td>
<td>145.8 ± 2.2</td>
<td>156.3 ± 2.2</td>
</tr>
</tbody>
</table>

The treatment of the FCN in the CIP motion agrees with solution S1 in Sect. 2, i.e. a priori values for the FCN period and amplitudes are taken from the model of Lambert (2007). Constant offsets to the sine and cosine amplitudes over the 27 years of VLBI data are estimated in the global adjustment. Other globally estimated parameters are the TRF and CRF. The estimate of the FCN period after four iterations is −431.18 ± 0.10 sidereal days, which is very close to the result from the “nutation only” solution. We assume that the highly precise estimation of the FCN period from nutation motion is achieved by the direct observation of the FCN in the rotation motion of the Earth axis. The less precise estimate of the FCN period obtained from the station displacement may reflect the indirect resonance effect on the solid Earth tidal motion.

5. Empirical FCN model with globally estimated varying amplitude

In Sect. 2 the FCN model created by Lambert (2007) was introduced where the time-varying amplitudes (sine and cosine) were fitted through the CPO in IERS EOP 05 C04 combined series with a sliding window over two years and displaced by one year. Following this idea of a varying amplitude and phase estimated in a one-year step, we determined the amplitudes Ac and As in several global solutions. The data input for each run are VLBI measurements carried out over four years, starting in 1984.0. Estimated parameters are constant cosine and sine amplitude terms corresponding to the FCN period of −431.18 sidereal days, as estimated in the joint adjustment described in Sect. 4. The partial derivatives are given by Eqs. (7) and (8) and the estimates of the Ac and As refer to the middle of the analysed data spans. Other estimated parameters are the session-wise reduced clock parameters, zenith wet delays, tropospheric gradients, and Earth rotation parameters. The TRF and CRF are fixed to the reference frames estimated in Sect. 4 to avoid a different datum definition dependent on included stations and radio sources in the respective groups of four years’ measurement data. In the first run data from 1984.0 to 1988.0 were involved and thus the estimates are valid for 1986.0. The second global solution includes data from 1985.0 till 1989.0, and it continues to the year 2011.0. The estimated values are shown in Table 2 and the resulting FCN model is plotted in Fig. 2. We found a very good agreement between our solution and the one from Lambert (2007) with differences in the cosine and sine amplitudes smaller than several microarcseconds.

6. Conclusions

The FCN period is estimated within a global VLBI solution from solid Earth tidal displacement as −431.23 ± 2.44 sidereal days and from the motion of the CIP as −431.17 ± 0.09 sidereal days, together with constant sine and cosine amplitude terms. The final value for the FCN period is derived from the solid Earth tidal displacement and from the motion of the CIP in a joint solution. Its estimated value of −431.18 ± 0.10 sidereal days differs slightly from the conventional value −431.39 sidereal days given in Petit & Luzum (2010). Furthermore, we present new values of an empirical FCN model. The period is fixed to the value determined in our joint solution, and the cosine and sine amplitudes are estimated from several global solutions in yearly steps directly from VLBI measurements.

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