

Originally published as:

Ruiz-Fuertes, J., Winkler, B., Bernert, T., Bayarjargal, L., Morgenroth, W., Koch-Müller, M., Refson, K., Milman, V., Tamura, N. (2015): Ferroelectric soft mode of polar ZnTiO3 investigated by Raman spectroscopy at high pressure. *- Physical Review B*, *91*, 21, p. 214110.

DOI: http://doi.org/10.1103/PhysRevB.91.214110

# <span id="page-1-0"></span>Ferroelectric soft mode of polar ZnTiO<sub>3</sub> investigated by Raman spectroscopy at high pressure

J. Ruiz-Fuertes,<sup>1,\*</sup> B. Winkler,<sup>1</sup> T. Bernert,<sup>2</sup> L. Bayarjargal,<sup>1</sup> W. Morgenroth,<sup>1</sup> M. Koch-Müller,<sup>3</sup> K. Refson,<sup>4</sup>

V. Milman, $5$  and N. Tamura<sup>6</sup>

<sup>1</sup>*Institut fur Geowissenschaften, Goethe-Universit ¨ at, Altenh ¨ oferallee 1, 60438 Frankfurt am Main, Germany ¨*

<sup>2</sup>Max-Planck-Institut für Kohlenforschung, Kaiser-Wilhelm-Platz 1, D-45470 Mülheim a.d. Ruhr, Germany

<sup>4</sup>*Department of Physics, Royal Holloway, University of London Egham, Surrey TW20 0EX, United Kingdom*

<sup>5</sup>*Dassault Systemes BIOVIA, 334 Science Park, Cambridge CB4 0WN, United Kingdom `*

<sup>6</sup>*Advanced Light Source, Berkeley, California 94720, USA*

(Received 15 April 2015; revised manuscript received 1 June 2015; published 22 June 2015)

We explore the vibrational behavior and stability of ferroelectric ZnTiO<sub>3</sub> under high pressure by Raman spectroscopy and second-harmonic-generation (SHG) measurements. *Ab initio* lattice-dynamics calculations have been employed to solve a controversy concerning the phonon-dispersion relations of ZnTiO<sub>3</sub> and to carry out an assignment of the Raman modes. A ferroelectric to paraelectric phase transition has been observed both by Raman spectroscopy and SHG at 20.8 GPa. Contrary to  $LiNbO<sub>3</sub>$ , the ferroelectric soft mode of  $ZnTiO<sub>3</sub>$  has been found to be the  $A_1(2)$  and not the  $A_1(1)$  mode. The calculated eigenvectors show that the  $A_1(2)$  mode of ferroelectric  $ZnTiO<sub>3</sub>$  is an antiphase vibration of the Ti atom against the oxygen framework, similar to the soft modes observed in ferroelectric perovskites. The SHG signal of  $ZnTiO<sub>3</sub>$  has been found to be independent of the grain size below the phase transition, indicating that  $ZnTiO<sub>3</sub>$  is a phase-matchable compound.

DOI: [10.1103/PhysRevB.91.214110](http://dx.doi.org/10.1103/PhysRevB.91.214110) PACS number(s): 77*.*80*.*B−*,* 78*.*55*.*Ap*,* 42*.*65*.*Ky

# **I. INTRODUCTION**

Nonlinear optic behavior, piezoelectricity, pyroelectricity, and spontaneous polarization make ferroelectric materials of great technological importance [\[1–4\]](#page-7-0). Applications such as ferroelectric random access memories (FRAM) [\[5\]](#page-7-0) or piezoactuators in microelectromechanical systems such as scanning probe microscopes [\[6,7\]](#page-7-0) are examples of their industrial relevance. Lead-based perovskites with a high-ferroelectic polarization have therefore been employed in many applications despite concerns regarding the impact of lead-bearing compounds on the environment [\[5,8,9\]](#page-7-0). In order to minimize the environmental impact, lead-free perovskite-related *AB*O3 polar oxides are currently being investigated extensively [\[10–13\]](#page-7-0). In this context, the recent high-pressure and hightemperature synthesis of polar zinc titanate  $(ZnTiO<sub>3</sub>)$  [\[12\]](#page-7-0) with an estimated spontaneous polarization of 75  $\mu$ C/cm<sup>2</sup>, which is similar to that of  $PbTiO<sub>3</sub>$ , and a second-harmonic-generation (SHG) signal 24 times as intense as that of  $\text{ZnSnO}_3$  [\[10\]](#page-7-0) has been a breakthrough in this search.

Polar  $ZnTiO<sub>3</sub>$  is isostructural to  $LiNbO<sub>3</sub>$  (space group *R*3*c*) with both cations being octahedrally coordinated in a three-dimensional corner-sharing octahedra perovskite (Pv) like framework. In this structure, both cations shift along the trigonal *c* axis, thereby producing a spontaneous polarization which is enhanced by a second-order Jahn-Teller distortion due to the  $Ti^{4+}$  ( $d^0$ ). In terms of designing and developing possible applications based on  $LiNbO<sub>3</sub>$  (LN)-type  $ZnTiO<sub>3</sub>$ , its ferroelectric instability needs to be understood.

The paraelectric parent structure of  $ZnTiO<sub>3</sub>$  is the ilmenite (II)-type phase (space group  $R\overline{3}$ ), which is the stable phase at ambient conditions. Both the LN-type and the Il-type structures are related by a zone-center ferroelectric mode that involves the displacement of the cations [\[14\]](#page-7-0). However, the LN-type to Il-type transformation requires octahedral rotations which are hindered due to anion-anion contacts for compounds with small tolerance factors [\[14\]](#page-7-0). Instead,  $LN$ -type  $ZnTiO<sub>3</sub>$  undergoes a phase transition to an orthorhombic (space group *Pmna*) Pv-type phase by an order-disorder phase transition [\[15–17\]](#page-7-0). Several studies of other LN-type ferroelectrics, such as LN-type MnTiO<sub>3</sub> [\[15\]](#page-7-0) or LN-type PbNiO<sub>3</sub> [\[18\]](#page-7-0), confirm this model.

*Ab initio* calculations predict the phase transition of LNtype  $ZnTiO<sub>3</sub>$  to the Pv-type structure at around 16 GPa [\[12\]](#page-7-0). Postnikov *et al.* [\[19\]](#page-7-0) have shown in  $LiNbO<sub>3</sub>$  that the lowestfrequency Raman  $A_1(1)$  ferroelectric mode polarized along the threefold axis (*c* axis) is unstable against an off-center displacement along this direction [\[20\]](#page-7-0) and shows pressureinduced softening  $[21,22]$ . Although the ferroelectric mode is not responsible for the LN-type to Pv-type phase transition due to the order-disorder character of the transition, identifying this mode in LN-type  $ZnTiO<sub>3</sub>$  is a prerequisite for understanding its ferroelectric behavior. In this work, we have studied the ferroelectric instability of the recently discovered LN-type  $ZnTiO<sub>3</sub>$  by means of Raman spectroscopy and SHG at ambient temperature and high pressures. We have performed an assignment of its Raman modes and investigated its ferroelectric soft mode on the basis of *ab initio* lattice-dynamical calculations.

## **II. EXPERIMENTAL DETAILS**

 $LN$ -type  $ZnTiO<sub>3</sub>$  was synthesized in powder form using pure Il-type  $ZnTiO<sub>3</sub>$  [\[23\]](#page-7-0) sealed inside a platinum capsule at 16.5 GPa and 1150 ◦C in a multianvil press for 38 minutes following the work by Inaguna *et al.* [\[12\]](#page-7-0). The multianvil experiment was performed at GFZ Potsdam with a 10*/*5 assembly, which was calibrated using the follow-ing transitions: coesite-stishovite [\[24\]](#page-7-0),  $\alpha$ - $\beta$  Mg<sub>2</sub>SiO<sub>4</sub> [\[25\]](#page-7-0),

<sup>3</sup>*GFZ Potsdam, Sektion 3.3, Telegrafenberg, 14473 Potsdam, Germany*

<sup>\*</sup>ruiz-fuertes@kristall.uni-frankfurt.de

 $\beta$ - $\gamma$ Mg<sub>2</sub>SiO<sub>4</sub> [\[26\]](#page-7-0), and enstatite- $\beta$ -Mg<sub>2</sub>SiO<sub>4</sub>-stishovite [\[27\]](#page-7-0). In all three experiments, stepped graphite heaters were applied and temperatures were measured with type-C thermocouples, with emf's uncorrected for pressure. The product consisted of small colorless grains of around 10–60 *μ*m in size.

In order to confirm the phase purity of the  $LN-ZnTiO_3$ samples, we performed synchrotron x-ray Laue microdiffraction and microfluorescence measurements, at beam line 12.3.2 of the Advanced Light Source (ALS) [\[28\]](#page-7-0). Fluorescence scans were performed using a Vortex-EM (Hitachi High-Technologies Science America, Inc.). For the two-dimensional fluorescence maps, a 1 s exposure per step was employed, and measurements were performed on a grid with step sizes  $\Delta x = \Delta y = 2$  *μ*m. The energy window for the Ti  $K_{\alpha}$  line at 4510.84 eV was set to 3936*.*61–5093*.*22 eV, while the energy window for Zn  $K_{\alpha}$  at 8638.86 eV was from 7879.14– 9377.70 eV. For the diffraction experiments, a polychromatic x-ray beam (10–24 keV) was focused to approximately  $1 \times 1$  $\mu$ m<sup>2</sup> (FWHM) by Kirkpatrick-Baez mirrors. Laue diffraction patterns were collected with a PILATUS 1M area detector in reflection geometry. The sample was inclined to the primary beam by 45◦ and the area detector set to 90◦. Laue patterns were indexed and analyzed using XMAS v.6 [\[29\]](#page-8-0).

High-pressure Raman spectroscopy and SHG experiments were carried out using a Boehler-Almax diamond-anvil cell (DAC) equipped with  $350 \mu$ m culet diamonds and tungsten gaskets indented to 40  $\mu$ m in thickness with holes of 130  $\mu$ m. For each high-pressure experiment, a single grain of around 10  $μ$ m thickness was placed inside the gasket hole together with a ruby chip to measure the pressure [\[30\]](#page-8-0) and Ar as pressure-transmitting medium. The Raman experiment was performed in a quasibackscattering configuration with a Renishaw (RM-1000) spectrometer equipped with a 1800 grooves/mm grating and a spectral resolution of around  $2 \text{ cm}^{-1}$ . The excitation source was a HeNe laser ( $\lambda = 633 \text{ nm}$ ) focused down to a 10  $\mu$ m spot with a 20 $\times$ -long working distance objective. An edge filter was used to filter the laser allowing measurements above  $100 \text{ cm}^{-1}$ . The SHG intensities at  $\lambda_{2\omega} = 527$  nm were measured in transmission geometry using the setup described by Bayarjargal *et al.* [\[31\]](#page-8-0).

### **III.** *AB INIT IO* **CALCULATIONS**

*Ab initio* calculations for LN-ZnTiO<sub>3</sub> and Pv-ZnTiO<sub>3</sub> were carried out at different pressures up to 25 GPa. We used a plane-wave pseudopotential approach to density functional theory (DFT) as implemented in the CASTEP package [\[32\]](#page-8-0). Calculations were performed with either the Perdew-Burke-Ernzerhof (PBE) generalized gradient approximation [\[33\]](#page-8-0) or the Wu-Cohen formulation [\[34\]](#page-8-0) and either the normconserving pseudopotentials or the Vanderbilt ultrasoft-type pseudopotentials from the "on the fly" database of Accelrys Materials Studio 7. The reciprocal space was sampled according to the Monkhorst-Pack scheme [\[35\]](#page-8-0) with a maximal distance of 0.03  $\mathring{A}^{-1}$  between the *k* points and a plane-wave basis set with a kinetic energy cutoff of 1050 eV for the norm-conserving pseudopotentials or 610 eV for the on-the-fly pseudopotentials. Variational density functional perturbation theory (DFPT) was used to evaluate the lattice dynamics and the response to an electric field [\[36\]](#page-8-0) and the Raman



FIG. 1. (Color online) Elemental distribution of Ti (left) and Zn (right) in a sample of  $ZnTiO<sub>3</sub>$ . Variations in the fluorescence intensity are due to variations in the sample thickness.

intensities were computed as described in Milman *et al.* [\[37\]](#page-8-0). We complemented the calculations of the  $ZnTiO<sub>3</sub>$  polymorphs by calculations on LN-type MgTiO<sub>3</sub>, FeTiO<sub>3</sub>, and MnTiO<sub>3</sub> in order to validate the reliability of our computational approach. In the latter two cases, we employed a Hubbard U of 2.5 eV for the *d* electrons of high-spin  $\text{Fe}^{2+}$  and  $\text{Mn}^{2+}$ .

### **IV. RESULTS AND DISCUSSION**

#### **A. Sample characterization**

The fluorescence map showed the distribution of Zn and Ti in one of the synthesized grains of  $LN$ -type  $ZnTiO<sub>3</sub>$  (Fig. 1). The map showed a homogeneous distribution of the elements. No other elements were detected in the sample.

Out of the 1147 diffraction patterns obtained on a  $31 \times 37$ mesh with  $2 \mu m$  step size, 520 were on the sample. Each frame typically contained about 100 to 230 reflections (Fig. 2) and we could index almost all reflections to the  $LN$ -type  $ZnTiO<sub>3</sub>$ phase using a two-grain model. This confirms that the sample consists of two crystalline domains of pure LN-ZnTiO3.



FIG. 2. (Color online) Typical Laue diffraction pattern of the LNtype  $ZnTiO<sub>3</sub>$  sample. Nearly all reflections can be indexed using a two-grain model indicated by blue and red boxes, respectively. We only show some indices for clarity.

# **B. Geometry optimization and phase stability**

The Wu-Cohen exchange-correlation functional calculations on LN-type  $ATiO_3$ , with  $A = Mn$ , Mg, Fe, or Zn, gave lattice parameters in very good agreement (better than 0.5%) with experiments [\[12,](#page-7-0)[38–40\]](#page-8-0). The PBE-based calculations gave results which consistently showed the well-known underbinding. The full relaxed unit-cell parameters obtained from the calculation at ambient pressure for  $LN$ -type  $ZnTiO<sub>3</sub>$ are  $a_{\text{theo}} = 5.2162$  Å and  $c_{\text{theo}} = 13.9698$  Å. These unit-cell parameters are 2.4% and 1.8% larger, respectively, than the experimental values obtained by Inaguna *et al.* [\[12\]](#page-7-0) with powder x-ray diffraction.

In the case of  $Pv-ZnTiO_3$ , the calculation at 25 GPa yielded  $a = 5.3330$  Å,  $b = 7.5821$  Å, and  $c = 5.1884$  Å as unit-cell parameters. From *P*-*V* curves, we obtained a bulk modulus of 198 GPa, slightly smaller than the value reported for this phase of  $ZnTiO<sub>3</sub>$  in previous calculations (214 GPa) [\[12\]](#page-7-0). We found that the Pv-type phase of  $ZnTiO<sub>3</sub>$  is dynamically stable above 16 GPa, as then the frequencies of all modes are real, in good agreement with findings by Inaguna *et al* [\[12\]](#page-7-0).

#### **C. Phonon-dispersion curves**

In LN-type compounds with point group  $C_{3v}$ , the irreducible representation of the 20 modes at the zone center  $\Gamma$  are 5  $A_1 + 5 A_2 + 10 E$ . The two acoustic modes have  $A_1 + E$ symmetry, the five *A*<sup>2</sup> modes are silent, and the remaining polar  $4 A_1 + 9 E$  modes are Raman and infrared active. In the case of paraelectric Pv-ZnTiO<sub>3</sub> with point group  $D_{2h}$ , there are 52 modes at the  $\Gamma$  point: 7  $A_g + 5 B_{1g} + 7 B_{2g} + 5 B_{3g} +$ 10  $B_{1u}$  + 8  $B_{2u}$  + 10  $B_{3u}$ . Three of these modes are acoustic  $(B_{1u} + B_{2u} + B_{3u})$ , the 24 even (*g*) modes are Raman active, and the remaining 25 odd (*u*) modes are infrared active.

In a recent study, Inaguna *et al.* [\[12\]](#page-7-0) report the calculated phonon dispersion of  $LN-ZnTiO<sub>3</sub>$ . In ionic crystals, such as  $LN-ZnTiO<sub>3</sub>$ , the electric field splits the transversal-optic (TO) and longitudinal-optic (LO) components of the *A*<sup>1</sup> and *E* polar modes. However, Inaguna *et al.* [\[12\]](#page-7-0) report phonon branches at  $\Gamma$  that do not split and range up to 1770 cm<sup>-1</sup>. A comparison to previous experimental values obtained for LN-MgTiO<sub>3</sub> and LN-MnTiO<sub>3</sub> [\[15,](#page-7-0)[40\]](#page-8-0) implies that a phonon spectrum expanding to such high frequencies for LN-ZnTiO<sub>3</sub> is not realistic. In order to address this controversy, we have repeated the phonon-dispersion calculations for  $LN-ZnTiO_3$ . The result is shown in Fig. 3, together with the corresponding one-phonon density of states (PDOS).

The phonon branches have been calculated along the two high-symmetry directions  $X\Gamma$  and  $\Gamma Z$  of the reciprocal space. The PDOS extends up to 760 cm<sup>-1</sup>. When comparing the dispersion curves of LN-ZnTiO<sub>3</sub> with those of LiNbO<sub>3</sub> [\[41\]](#page-8-0), one can see that there is some similarity despite a mode sequence change. The LO-TO splitting is shown in Fig. 3. Similarly to LiNbO<sub>3</sub> [\[41\]](#page-8-0), in LN-ZnTiO<sub>3</sub>, the  $A_1^T$  modes correspond to phonon branches that point from the *xy* (*X* point) hexagonal plane to the  $\Gamma$  point of the Brillouin zone, and the  $A_1^L$  correspond to the same phonon branches but pointing to  $\Gamma$  from the *z* axis. The *E* modes remain doubly degenerate along  $\Gamma Z$  and split to  $E^T$  and  $E^L$  along the  $X\Gamma$  direction.



FIG. 3. (Color online) Phonon-dispersion curves of ferroelectric  $LiNbO<sub>3</sub>$ -type  $ZnTiO<sub>3</sub>$  along the main symmetry directions of the Brillouin zone at 1 atm. The branches that correspond to the transversal-optic  $A_1^T$  and longitudinal-optic  $A_1^L$  modes are in red, the black lines correspond to the *E* modes, the blue lines correspond to the silent *A*<sup>2</sup> modes, and the dashed lines correspond to the acoustic branches. The right panel shows the corresponding phonon density of states (PDOS).

#### **D. Raman spectroscopy**

The Raman spectra of LN-type compounds differing from  $LiNbO<sub>3</sub>$  or  $LiTaO<sub>3</sub>$  [\[42\]](#page-8-0) have been previously reported for  $LN-MgTiO<sub>3</sub>$  and  $LN-MnTiO<sub>3</sub>$  [\[15](#page-7-0)[,40\]](#page-8-0). However, the continuous character of the spectrum, which consists of broad overlapping bands, and the lack of single crystals to separate the TO modes from the LO modes, which tend to mix, have prevented any Raman modes assignment. Here, we intend to assign the Raman modes of  $LN$ -ZnTiO<sub>3</sub> using powder samples. We have investigated the mode assignment by comparing the experimental and calculated Raman spectra as shown in Fig. [4.](#page-4-0)

The calculated Raman spectrum of  $LN-ZnTiO<sub>3</sub>$  is shown in Fig.  $4(a)$ . It was computed by convoluting the sharp spectrum with a Lorentzian function with FWHM of  $5 \text{ cm}^{-1}$ , and does not show the LO modes due to an implementation restriction in our calculation. Despite the narrow calculated bands and although the intensity of the LO modes is zero, the calculated spectrum shows that at least 6 of the 13 Raman active modes overlap. Even though there is a substantial broadening of the experimentally determined spectrum [Fig.  $4(b)$ ] and we observe both LO and TO modes experimentally, the relative intensities in the experimentally determined and the computed Raman spectra are in very reasonable agreement.

<span id="page-4-0"></span>

FIG. 4. (Color online) (a) Calculated spectrum of  $LiNbO<sub>3</sub>$ -type  $ZnTiO<sub>3</sub>$  at 1 atm. The frequencies of the TO (black ticks) and LO (red ticks) are shown. (b) The experimental spectrum of  $LiNbO<sub>3</sub>$ -type  $ZnTiO<sub>3</sub>$  at 1 atm is shown together with the mode assignment made after comparing calculation and experiment. The ticks represent the frequencies of the experimentally observed modes.

Hence, we could unequivocally identify 9 out of 13 TO modes of  $LN$ - $ZnTiO<sub>3</sub>$  where the frequency mismatch between calculated and experimental values was *<*6% for all modes. The agreement between theory and experiment is worse for the LO modes. We have assigned 4 of the 13 LO modes that should be present, but for two of the modes (346 and 801 cm−1) the frequency mismatch is above 7%. The frequencies and symmetry of the Raman modes of  $LN$ -ZnTiO<sub>3</sub> are shown in Table I.

TABLE I. Experimental and calculated values for the zerofrequency  $(\omega_0)$  and linear pressure coefficients  $a_i$  for the zone-center TO  $(T)$  and LO  $(L)$  modes of LN-ZnTiO<sub>3</sub> at 1 atm obtained from high-pressure Raman scattering measurements and *ab initio* calculations. Raman modes  $\omega$  and their pressure coefficients  $a_i$  are expressed in cm<sup>-1</sup> and cm<sup>-1</sup> GPa<sup>-1</sup>, respectively.

		Expt.		Calc.		Expt.		Calc.	
Mode	$\omega_0$	$a_i$	$\omega_0$	$a_i$	Mode	$\omega_0$	$a_i$	$\omega_0$	$a_i$
$E^T$	154	1.3	151	1.1	$E^L$	175	1.1	171	0.8
$A_1^T(1)$			155	0.6	$A_1^L(1)$			174	0.1
$E^T$	218	0.5	207	0.8	$E^L$			213	0.4
$E^T$			230	1.3	$F^L$			231	1.3
$E^T$	251	1.2	251	1.1	$F^L$			257	1.0
$A_1^T(2)$	275	$-0.1$	280	$-0.9$	$A_1^L(2)$	346	4.3	372	4.8
$E^T$	292	3.0	283	4.3	$E^L$			283	4.6
$E^T$	332	3.8	332	3.4	$E^L$			422	3.7
$A_1^T(3)$			384	3.9	$A_1^L(3)$			431	0.3
$E^T$			426	4.1	$E^L$	462	3.4	467	3.4
$E^T$	504	3.4	537	3.8	$E^L$			554	2.3
$E^T$	586	4.1	567	3.2	$E^L$			750	3.5
$A_1^T(4)$	571	2.6	574	1.1	$A_1^L(4)$	801	3.7	733	3.8



FIG. 5. (Color online) Raman spectra at different pressures of  $LiNbO<sub>3</sub>$ -type  $ZnTiO<sub>3</sub>$  and its high-pressure phase. The ticks indicate the positions of the experimental (black) and calculated (red) frequency of the modes.

According to the calculations, the modes of  $LN-ZnTiO<sub>3</sub>$  that have not been experimentally observed are expected to be weak and to overlap strongly with the neighboring modes. In order to confirm our mode assignment, we have studied the high-pressure Raman spectrum of  $LN-ZnTiO<sub>3</sub>$ . If the mode assignment that we have made was correct, there should be an agreement between the experimental and calculated pressure coefficients of the modes. In Fig. 5, we show the evolution of the Raman spectra of  $LN$ -ZnTiO<sub>3</sub> for pressures up to 34.8 GPa.

The frequencies of the nine TO and four LO modes of  $LN-ZnTiO<sub>3</sub>$  which we could identify at ambient pressure can be determined on pressure increase up to 20.8 GPa, when additional bands emerge. On increasing pressure, all modes blueshift, except the  $A_1(2)$  mode at 275 cm<sup>-1</sup> that redshifts up to ∼9 GPa when it overlaps with a neighboring *E* mode. We shall discuss the behavior of the soft mode in detail below. We interpret the appearance of additional Raman modes at 20.8 GPa as the onset of a phase transition that is completed below 24.6 GPa when the Raman bands assigned to the low-pressure phase have completely vanished. Based on our and previous *ab initio* calculations that predict a structural phase transition of  $LN$ -ZnTiO<sub>3</sub> at around 16 GPa to a Pv-type orthorhombic structure with space group *Pmna* [\[12\]](#page-7-0), we conclude that at 20.8 GPa,  $LN$ - $ZnTiO<sub>3</sub>$  begins to transform to  $Pv-ZnTiO<sub>3</sub>$ . This is in contrast to the behavior of LiNbO<sub>3</sub>, which has been found to become amorphous

TABLE II. Experimental and calculated values for the zerofrequency  $(\omega_0)$  and linear pressure coefficients  $a_i$  of the Raman active modes of  $Pv-ZnTiO<sub>3</sub>$  at 25 GPa obtained from high-pressure Raman scattering measurements and *ab initio* calculations. Raman modes *ω* and their pressure coefficients *ai* are expressed in cm−<sup>1</sup> and cm−<sup>1</sup> GPa−<sup>1</sup> , respectively.

		Expt. $(24.6 \text{ GPa})$	Calc. $(25$ GPa $)$		
Mode	$\omega_0$	$a_i$	$\omega_0$	$a_i$	
$A_g$	141	0.9	140	0.8	
$B_{2g}$	162	0.6	161	0.7	
$B_{3g}$			163	1.1	
$A_g$	205	1.5	196	1.3	
$\boldsymbol{B}_{1g}$			199	0.9	
$B_{2g}$	217	1.7	213	1.4	
$B_{1g}$			266	0.9	
$A_g$			271	1.0	
$B_{2g}$	301	1.2	288	1.5	
$B_{3g}$	329	1.5	322	0.9	
$A_g$	354	2.2	347	1.8	
$B_{2g}$			411	1.3	
$B_{1g}$	457	2.9	430	2.6	
$A_{g}$			512	2.8	
$A_g$			524	2.3	
$B_{3g}$			527	2.3	
$B_{2g}$			540	2.7	
$B_{2g}$	559	2.9	578	3.2	
$B_{3g}$			581	3.3	
$B_{1g}$			583	3.6	
$A_g$	608	3.5	609	3.6	
$B_{1g}$	726	3.2	764	3.6	
$B_{2g}$	835	3.2	825	3.3	
$B_{3g}$	876	3.3	849	3.4	

above 31 GPa [\[43\]](#page-8-0), but it is well known that a nonhydrostatic environment can drastically shift transition pressures or induce amorphization. The tick marks in Fig. [5](#page-4-0) indicate the calculated and experimental frequencies of the modes at 24.6 GPa in the Pv-type phase. Though the broadening of the modes prevents an unambiguous assignment of the Raman modes for the Pv-type phase, some of the modes can be tentatively identified. The experimental and calculated frequencies of the Raman modes of the high-pressure phase are shown in Table II.

The pressure dependencies of the frequencies of the experimentally determined modes of  $LN-ZnTiO<sub>3</sub>$  up to 34.8 GPa are illustrated in Fig. 6. As stated before, we can observe that the frequency of all modes in the low-pressure phase increases with pressure, while the frequency of the  $A_1^T(2)$  mode decreases. For those modes that linearly depend on pressure, the pressure coefficients are  $a_i = d\omega_i/dP$ , while for those that follow a quadratic behavior (modes at 251, 275, 292, 332, and 433  $\text{cm}^{-1}$ ), the pressure coefficients have been obtained from the low-pressure linear parts. The results are shown in Table [I,](#page-4-0) where they are compared to the results of the model calculations.

Figure 6 shows that the high-frequency modes of both phases have pressure coefficients that are around three times larger than those of the low-frequency modes. The agreement



FIG. 6. (Color online) Pressure dependence of the experimentally observed modes of the low-pressure and high-pressure phases of ZnTiO<sub>3</sub>. The red solid lines are linear fits, while the dashed blue lines are quadratic fits. The coexistence range (coex) of both phases is indicated.

between the experimental and the calculated pressure coefficients of both the observed LO and TO modes is generally very good for LN-ZnTiO<sub>3</sub> where the softening of the  $A_1^T(2)$  is also predicted by our *ab initio* calculations. Only the experimental pressure coefficient of the highest-frequency  $A_1^T(4)$  mode is in disagreement with the results of our model calculations, but due to a severe overlap with the highest-frequency  $E<sup>T</sup>$  mode, the experimentally determined value is rather uncertain. For Pv-ZnTiO<sub>3</sub> (Table II), the agreement between the pressure coefficients of the experimentally observed modes and the calculated modes is also very good. The good agreement of the pressure coefficients strongly supports our mode assignments.

We have commented in Sec. [I](#page-1-0) that in LN-type compounds, the ferroelectric (*R*3*c*) phase can be transformed to the paraelectric  $(R_3)$  phase by one  $A_1$  soft mode. However, this  $R3c \rightarrow R3$  transformation would also require an octahedral tilting, which is not allowed by symmetry in  $R\overline{3}$ , and thus there is an order-disorder  $R3c \rightarrow Pnma$  transition instead, such as has already been observed for LN-ZnTiO<sub>3</sub>. In LiNbO<sub>3</sub>, this soft mode is the lowest-frequency  $A_1(1)$  mode which consists of an antiphase vibration of the Nb atoms against the O framework along the *c* axis, while the Li atoms are not displaced. This anharmonic [\[20\]](#page-7-0) mode has been controversially observed to soften at high temperature by some authors  $[44]$  in LiNbO<sub>3</sub>. Under high pressure, its frequency barely shifts, showing an experimental pressure coefficient close to zero [\[21\]](#page-7-0).



FIG. 7. Connected TiO<sub>6</sub> and ZnO<sub>6</sub> ocathedra of ZnTiO<sub>3</sub> in the LiNbO<sub>3</sub>-type structure showing the eigenvectors of the  $A_1(1)$  and *A*1(2) Raman modes. The empty, full gray, and black circles represent the Ti, Zn, and O atoms, respectively. The black arrows show the displacement.

One would expect a similar behavior of the *A*1(1) mode of  $LN$ -ZnTiO<sub>3</sub>. However, although we have not been able to detect the  $A_1(1)$  mode by Raman spectroscopy, our calculations show that the frequency of this mode (155 cm<sup>-1</sup>) blueshifts with a pressure coefficient of  $0.6 \text{ cm}^{-1} \text{ GPa}^{-1}$ . In order to better understand the difference between the  $A_1(1)$  mode of LiNbO<sub>3</sub> and  $LN$ - $ZnTiO<sub>3</sub>$ , we have shown in Fig. 7 the calculated eigenvectors of the  $A_1(1)$  and  $A_1(2)$  modes of LN-ZnTiO<sub>3</sub>. In contrast to  $LiNbO<sub>3</sub>$ , in  $LN-ZnTiO<sub>3</sub>$  the  $A<sub>1</sub>(1)$  mode consists of an in-phase vibration of the Ti and O atoms along the *c* axis with the Zn atoms vibrating in antiphase also along the polar axis as in the  $A_1(2)$  mode of LiNbO<sub>3</sub>. However, the  $A_1(2)$ mode of LN-ZnTiO<sub>3</sub>, similarly to the  $A_1(1)$  mode of LiNbO<sub>3</sub>, is an antiphase vibration of the Ti atoms against the oxygen framework with the Zn atoms at rest. In LiNbO<sub>3</sub>, the  $A_1(1)$ mode has a frequency of 256 cm<sup>-1</sup>, slightly smaller than that of the  $A_1(2)$  mode of LN-ZnTiO<sub>3</sub> (275 cm<sup>-1</sup>), as expected by the larger atomic mass of Nb compared to Ti. However, the  $A_1(1)$ of LN-ZnTiO<sub>3</sub> and the  $A_1(2)$  mode of LiNbO<sub>3</sub> involve the Zn and the 10-times-lighter Li atoms, respectively. This results in a frequency 50% larger for this mode in  $LiNbO<sub>3</sub>$  [\[45\]](#page-8-0). The strong compositional dependence of the frequencies of the two low-frequency  $A_1$  modes of LN-ZnTiO<sub>3</sub> and LiNbO<sub>3</sub> explains why in LN-ZnTiO<sub>3</sub> it is the  $A_1(2)$  and not the  $A_1(1)$  mode that softens under pressure (Table [I\)](#page-4-0). This should also be the case in other LN-type compounds where the *A* cation is a transition metal, but the lack of detailed Raman spectroscopic studies currently prevents a confirmation of this conclusion. Our findings agree with previous calculations [\[20](#page-7-0)[,46\]](#page-8-0) performed on  $LiNbO<sub>3</sub>$ , where the atomic mass of Li can be neglected in comparison to the atomic mass of Nb.

#### **E. Second-harmonic generation**

According to Inaguna *et al.* [\[12\]](#page-7-0), the intensity of the SHG signal  $(I_{2\omega})$  of LN-ZnTiO<sub>3</sub> is up to 24 times larger than that of ZnSnO3, which facilitates high-pressure experiments. We have shown earlier that high-pressure SHG measurements are an excellent approach to characterize powder samples [\[47\]](#page-8-0). Figure 8 shows the variation of the normalized  $I_{2\omega}$  with



FIG. 8. Pressure dependence of the normalized secondharmonic-generation (SHG) signal.

pressure.  $I_{2\omega}$  remains constant up to  $\approx 20$  GPa when it starts to decrease, as a consequence of the ferroelectric to paraelectric transformation, to a centrosymmetric space group (*Pmna*), in good agreement with the results of the Raman spectroscopic measurements described above and previous *ab initio* calculations [\[12\]](#page-7-0). The Raman data implied a first-order transition, where both phases coexisted in a pressure interval of about 4 GPa up to around 24 GPa. This is consistent with the pressure dependence of the SHG signal, which disappears at around 24 GPa. Non-phase-matchable materials are those materials with a noncentrosymmetric structure in which the excitation wave (with wavelength *ω*) and the generated SHG wave (with wavelength 2*ω*) propagate with different phase velocities. Therefore, the intensity of the generated SHG signal is usually many orders of magnitude lower than the intensity of the fundamental wave. In the case of phase-matchable materials, an effective conversion from the incident photons to SHG is possible by the appropriate choice of the crystal orientation and polarization fields [\[47\]](#page-8-0). We have shown earlier that for phase-matchable crystals,  $I_{2\omega}$  is independent of the grain size when the latter exceeds a critical diameter [\[47\]](#page-8-0). The application of pressure will cause a decrease of the grain size, and only in the case of a phase-matchable sample with large grains would  $I_{2\omega}$  be independent of the pressure. For phase-matchable materials with small grains, pressure would lead to either independence or a decrease of  $I_{2\omega}$ , while for non-phase-matchable compounds,  $I_{2\omega}$  would either increase or decrease, depending on whether the grain size is below or above a compound-specific diameter. For phase-matchable LiNbO<sub>3</sub>, the critical size is about 50  $\mu$ m [\[47\]](#page-8-0). From the diffraction experiments, we know that the synthesized grains of  $ZnTiO<sub>3</sub>$  used in our experiments consist of single-crystal domains with diameters of ∼30 *μ*m, and so the combination of our experimental approaches strongly implies that  $ZnTiO<sub>3</sub>$ is a phase-matchable material.

## **V. SUMMARY AND CONCLUSIONS**

<span id="page-7-0"></span>The properties and stability of ferroelectric  $LiNbO<sub>3</sub> (LN)$ type  $ZnTiO<sub>3</sub>$  have been studied under high pressure up to 34.8 GPa across the ferroelectric to paraelectric phase transition. Raman spectroscopy and second-harmonic-generation (SHG) studies reveal that the phase transition starts at 20 GPa, in agreement with previous calculations. *Ab initio* lattice-dynamic calculations have been employed to assign the symmetries of most LO and TO Raman active modes of the ferroelectric (*R*3*c*) and paraelectric (*Pmna*) phases and to determine the phonon branches in the  $X\Gamma$  and  $\Gamma Z$  directions of the Brillouin zone of  $LN-ZnTiO_3$ . The calculated one-phonon density of states (PDOS) shows that the phonon spectrum of LN-ZnTiO<sub>3</sub> extends up to 760 cm<sup>-1</sup>. The  $A_1(2)$  mode of  $LN$ -ZnTiO<sub>3</sub> has been found to soften under pressure with a pressure coefficient of <sup>−</sup>0*.*1 cm−<sup>1</sup> GPa <sup>−</sup>1. Our calculations show that the polarization vector of this mode is an antiphase vibration of the Ti cations against the O framework along the *c* axis, while the Zn cations stay at rest. This is similar to the ferroelectric soft mode of perovskites. We have also found that the frequency of the  $A_1(1)$  mode of LN-ZnTiO<sub>3</sub>, which consists of the in-phase vibration of the Ti cations and the oxygen framework along the *c* axis while the Zn cations vibrate in antiphase, and the frequency of the  $A_1(2)$  mode are swapped with respect to LiNbO<sub>3</sub>. While the ferroelectric soft mode of  $LiNbO<sub>3</sub>$ ,  $A<sub>1</sub>(1)$ , presents a similar frequency to the ferroelectric  $A_1(2)$  mode of LN-ZnTiO<sub>3</sub>, the  $A_1(1)$  mode of LN-ZnTiO<sub>3</sub> is 50% larger than the frequency of the  $A_1(2)$  mode of  $LiNbO<sub>3</sub>$ . We explain this by the contribution of the *A* cation on the  $A_1(1)$  and  $A_1(2)$  modes of LN-ZnTiO<sub>3</sub> and  $LiNbO<sub>3</sub>$ , respectively, with Zn being ten times more massive than Li. This result shows that independently of the relative atomic masses of the *A* and *B* cations in these ferroelectric compounds, the contribution of the displacement of the *A* cations is negligible in the ferroelectric instability and the displacement of the *B* cations plays the most important role in LN-type compounds. Finally, SHG experiments were employed to qualitatively follow the pressure-induced change of the spontaneous polarization. This has allowed us to confirm the nature of the ferroelectric to paraelectric phase transition of  $LN$ -ZnTiO<sub>3</sub> and conclude that polar  $ZnTiO<sub>3</sub>$  is a phase-matchable material.

#### **ACKNOWLEDGMENTS**

We thank Andreas Ebert for his support during the multianvil experiments. J.R.-F. thanks the Alexander von Humboldt Foundation for a postdoctoral fellowship. B.W. and W.M. acknowledge financial support from the BMBF Project No. 05K13RF1. The Advanced Light Source (ALS) is supported by the Director, Office of Science, Office of Basic Energy Sciences, of the U.S. Department of Energy under Contract No. DE-AC02-05CH11231 at the Lawrence Berkeley National Laboratory (LBNL).

- [1] G. Catalan and J. F. Scott, [Adv. Mater.](http://dx.doi.org/10.1002/adma.200802849) **[21](http://dx.doi.org/10.1002/adma.200802849)**, [2463](http://dx.doi.org/10.1002/adma.200802849) [\(2009\)](http://dx.doi.org/10.1002/adma.200802849).
- [2] J. B. Neaton, C. Ederer, U. V. Waghmare, N. A. Spaldin, and K. M. Rabe, [Phys. Rev. B.](http://dx.doi.org/10.1103/PhysRevB.71.014113) **[71](http://dx.doi.org/10.1103/PhysRevB.71.014113)**, [014113](http://dx.doi.org/10.1103/PhysRevB.71.014113) [\(2005\)](http://dx.doi.org/10.1103/PhysRevB.71.014113).
- [3] R. Resta, [Modell. Simul. Mater. Sci. Eng.](http://dx.doi.org/10.1088/0965-0393/11/4/201) **[11](http://dx.doi.org/10.1088/0965-0393/11/4/201)**, [R69](http://dx.doi.org/10.1088/0965-0393/11/4/201) [\(2003\)](http://dx.doi.org/10.1088/0965-0393/11/4/201).
- [4] G. Saghi-Szabo, R. E. Cohen, and H. Krakauer, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.80.4321) **[80](http://dx.doi.org/10.1103/PhysRevLett.80.4321)**, [4321](http://dx.doi.org/10.1103/PhysRevLett.80.4321) [\(1998\)](http://dx.doi.org/10.1103/PhysRevLett.80.4321).
- [5] J. F. Scott and C. A. Paz de Araujo, [Science](http://dx.doi.org/10.1126/science.246.4936.1400) **[246](http://dx.doi.org/10.1126/science.246.4936.1400)**, [1400](http://dx.doi.org/10.1126/science.246.4936.1400) [\(1989\)](http://dx.doi.org/10.1126/science.246.4936.1400).
- [6] G. Binnig, C. F. Quate, and C. Gerber, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.56.930) **[56](http://dx.doi.org/10.1103/PhysRevLett.56.930)**, [930](http://dx.doi.org/10.1103/PhysRevLett.56.930) [\(1986\)](http://dx.doi.org/10.1103/PhysRevLett.56.930).
- [7] P. J. Muralt, [Micromech. Microeng.](http://dx.doi.org/10.1088/0960-1317/10/2/307) **[10](http://dx.doi.org/10.1088/0960-1317/10/2/307)**, [136](http://dx.doi.org/10.1088/0960-1317/10/2/307) [\(2000\)](http://dx.doi.org/10.1088/0960-1317/10/2/307).
- [8] [N. Takashi, N. Yuichi, K. Akira, and T. Hidemi,](http://dx.doi.org/10.1063/1.112031) Appl. Phys. Lett. **[65](http://dx.doi.org/10.1063/1.112031)**, [1522](http://dx.doi.org/10.1063/1.112031) [\(1994\)](http://dx.doi.org/10.1063/1.112031).
- [9] B. Noheda, J. A. Gonzalo, L. E. Cross, R. Guo, S. E. Park, D. E. Cox, and G. Shirane, [Phys. Rev. B](http://dx.doi.org/10.1103/PhysRevB.61.8687) **[61](http://dx.doi.org/10.1103/PhysRevB.61.8687)**, [8687](http://dx.doi.org/10.1103/PhysRevB.61.8687) [\(2000\)](http://dx.doi.org/10.1103/PhysRevB.61.8687).
- [10] Y. Inaguna, M. Yoshida, and T. Katsumata, [J. Am. Chem. Soc.](http://dx.doi.org/10.1021/ja801843v) **[130](http://dx.doi.org/10.1021/ja801843v)**, [6704](http://dx.doi.org/10.1021/ja801843v) [\(2008\)](http://dx.doi.org/10.1021/ja801843v).
- [11] Y. Inaguna, M. Yoshida, T. Tsuchiya, A. Aimi, K. Tanaka, T. Katsumata, and D. Mori, [J. Phys.: Conf. Ser.](http://dx.doi.org/10.1088/1742-6596/215/1/012131) **[215](http://dx.doi.org/10.1088/1742-6596/215/1/012131)**, [012131](http://dx.doi.org/10.1088/1742-6596/215/1/012131) [\(2010\)](http://dx.doi.org/10.1088/1742-6596/215/1/012131).
- [12] Y. Inaguna, A. Aimi, Y. Shikaro, D. Sakurai, D. Mori, H. Kojitani, M. Akaogi, and M. Nakayama, [J. Am. Chem. Soc.](http://dx.doi.org/10.1021/ja408931v) **[136](http://dx.doi.org/10.1021/ja408931v)**, [2748](http://dx.doi.org/10.1021/ja408931v) [\(2014\)](http://dx.doi.org/10.1021/ja408931v).
- [13] D. Vanderbildt, [Curr. Opin. Solid State Mater. Sci.](http://dx.doi.org/10.1016/S1359-0286(97)80013-7) **[2](http://dx.doi.org/10.1016/S1359-0286(97)80013-7)**, [701](http://dx.doi.org/10.1016/S1359-0286(97)80013-7) [\(1997\)](http://dx.doi.org/10.1016/S1359-0286(97)80013-7).
- [14] N. A. Benedek and C. J. Fennie, [J. Phys. Chem. C](http://dx.doi.org/10.1021/jp402046t) **[117](http://dx.doi.org/10.1021/jp402046t)**, [13339](http://dx.doi.org/10.1021/jp402046t) [\(2013\)](http://dx.doi.org/10.1021/jp402046t).
- [15] X. Wu, S. Qin, and L. Dubrovinsky, [Geosci. Front.](http://dx.doi.org/10.1016/j.gsf.2010.09.003) **[2](http://dx.doi.org/10.1016/j.gsf.2010.09.003)**, [107](http://dx.doi.org/10.1016/j.gsf.2010.09.003) [\(2011\)](http://dx.doi.org/10.1016/j.gsf.2010.09.003).
- [16] [N. C. Wilson, S. P. Russo, J. Muscat, and N. M. Harrison,](http://dx.doi.org/10.1103/PhysRevB.72.024110) *Phys.* Rev. B **[72](http://dx.doi.org/10.1103/PhysRevB.72.024110)**, [024110](http://dx.doi.org/10.1103/PhysRevB.72.024110) [\(2005\)](http://dx.doi.org/10.1103/PhysRevB.72.024110).
- [17] H. Gou, J. Zhang, Z. Li, G. Wang, F. Gao, R. C. Ewing, and J. Lian, [Appl. Phys. Lett.](http://dx.doi.org/10.1063/1.3562013) **[98](http://dx.doi.org/10.1063/1.3562013)**, [091914](http://dx.doi.org/10.1063/1.3562013) [\(2011\)](http://dx.doi.org/10.1063/1.3562013).
- [18] W. Wang, S. Wang, D. He, and J. Xu, [Solid State Commun.](http://dx.doi.org/10.1016/j.ssc.2014.06.022) **[196](http://dx.doi.org/10.1016/j.ssc.2014.06.022)**, [8](http://dx.doi.org/10.1016/j.ssc.2014.06.022) [\(2014\)](http://dx.doi.org/10.1016/j.ssc.2014.06.022).
- [19] A. V. Postnikov, T. Neumann, and G. Borstel, [Phys. Rev. B](http://dx.doi.org/10.1103/PhysRevB.50.758) **[50](http://dx.doi.org/10.1103/PhysRevB.50.758)**, [758](http://dx.doi.org/10.1103/PhysRevB.50.758) [\(1994\)](http://dx.doi.org/10.1103/PhysRevB.50.758).
- [20] V. Caciuc, A. V. Postnikov, and G. Borstel, [Phys. Rev. B](http://dx.doi.org/10.1103/PhysRevB.61.8806) **[61](http://dx.doi.org/10.1103/PhysRevB.61.8806)**, [8806](http://dx.doi.org/10.1103/PhysRevB.61.8806) [\(2000\)](http://dx.doi.org/10.1103/PhysRevB.61.8806).
- [21] J. Mendes Filho, V. Lemos, and F. Cerdeira, [J. Raman Spec.](http://dx.doi.org/10.1002/jrs.1250150602) **[15](http://dx.doi.org/10.1002/jrs.1250150602)**, [367](http://dx.doi.org/10.1002/jrs.1250150602) [\(1984\)](http://dx.doi.org/10.1002/jrs.1250150602).
- [22] M. R. Tejerina, K. Pereira da Silva, A. R. Goñi, and G. A. Torchia, [Opt. Mater.](http://dx.doi.org/10.1016/j.optmat.2013.10.030) **[36](http://dx.doi.org/10.1016/j.optmat.2013.10.030)**, [581](http://dx.doi.org/10.1016/j.optmat.2013.10.030) [\(2013\)](http://dx.doi.org/10.1016/j.optmat.2013.10.030).
- [23] [T. Bernert, J. Ruiz-Fuertes, L. Bayarjargal, and B. Winkler,](http://dx.doi.org/10.1016/j.solidstatesciences.2015.03.014) Solid State Sciences **[43](http://dx.doi.org/10.1016/j.solidstatesciences.2015.03.014)**, [53](http://dx.doi.org/10.1016/j.solidstatesciences.2015.03.014) [\(2015\)](http://dx.doi.org/10.1016/j.solidstatesciences.2015.03.014).
- [24] [M. Akaogi, H. Yusa, K. Shiraishi, and T. Suzuki,](http://dx.doi.org/10.1029/95JB02395) J. Geophys. Res. **[100](http://dx.doi.org/10.1029/95JB02395)**, [22337](http://dx.doi.org/10.1029/95JB02395) [\(1995\)](http://dx.doi.org/10.1029/95JB02395).
- [25] H. Morishima, T. Kato, M. Suto, E. Ohtani, S. Urakawa, W. Utsumi, O. Shimomura, and T. Kikegawa, [Science](http://dx.doi.org/10.1126/science.265.5176.1202) **[265](http://dx.doi.org/10.1126/science.265.5176.1202)**, [1202](http://dx.doi.org/10.1126/science.265.5176.1202) [\(1994\)](http://dx.doi.org/10.1126/science.265.5176.1202).
- [26] [T. Inoue, D. J. Weidner, P. A. Northrup, and J. P. Parise,](http://dx.doi.org/10.1016/S0012-821X(98)00077-6) Earth Planet. Sci. Lett. **[160](http://dx.doi.org/10.1016/S0012-821X(98)00077-6)**, [107](http://dx.doi.org/10.1016/S0012-821X(98)00077-6) [\(1998\)](http://dx.doi.org/10.1016/S0012-821X(98)00077-6).
- [27] T. Gasparik, [Contrib. Mineral. Petr.](http://dx.doi.org/10.1007/BF00371083) **[102](http://dx.doi.org/10.1007/BF00371083)**, [389](http://dx.doi.org/10.1007/BF00371083) [\(1989\)](http://dx.doi.org/10.1007/BF00371083).
- [28] M. Kunz, N. Tamura, K. Chen, A. A. MacDowell, R. S. Celestre, M. M. Church, S. Fakra, E. E. Domning, J. M. Glossinger, J. L. Kirschman *et al.*, [Rev. Sci. Instrum.](http://dx.doi.org/10.1063/1.3096295) **[80](http://dx.doi.org/10.1063/1.3096295)**, [035108](http://dx.doi.org/10.1063/1.3096295) [\(2009\)](http://dx.doi.org/10.1063/1.3096295).
- <span id="page-8-0"></span>[29] N. Tamura, in *Strain and Dislocation Gradients from Diffraction*, edited by R. Barabash and G. Ice (Imperial College Press, London, 2014), pp. 125–155.
- [30] H. K. Mao, P. M. Bell, J. W. Shaner, and D. J. Steinberg, J. Appl. Phys. **[49](http://dx.doi.org/10.1063/1.325277)**, [3276](http://dx.doi.org/10.1063/1.325277) [\(1978\)](http://dx.doi.org/10.1063/1.325277).
- [31] L. Bayarjargal, B. Winkler, E. Haussühl, and R. Boehler, Appl. Phys. Lett. **[95](http://dx.doi.org/10.1063/1.3205120)**, [061907](http://dx.doi.org/10.1063/1.3205120) [\(2009\)](http://dx.doi.org/10.1063/1.3205120).
- [32] S. J. Clark, M. D. Segall, C. J. Pickard, P. J. Hasnip, M. J. Probert, K. Refson, and M. C. Paynei, [Z. Kristallogr.](http://dx.doi.org/10.1524/zkri.220.5.567.65075) **[220](http://dx.doi.org/10.1524/zkri.220.5.567.65075)**, [567](http://dx.doi.org/10.1524/zkri.220.5.567.65075) [\(2005\)](http://dx.doi.org/10.1524/zkri.220.5.567.65075).
- [33] J. P. Perdew, K. Burke, and M. Ernzerhof, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.77.3865) **[77](http://dx.doi.org/10.1103/PhysRevLett.77.3865)**, [3865](http://dx.doi.org/10.1103/PhysRevLett.77.3865) [\(1996\)](http://dx.doi.org/10.1103/PhysRevLett.77.3865).
- [34] Z. Wu and R. E. Cohen, [Phys. Rev. B](http://dx.doi.org/10.1103/PhysRevB.73.235116) **[73](http://dx.doi.org/10.1103/PhysRevB.73.235116)**, [235116](http://dx.doi.org/10.1103/PhysRevB.73.235116) [\(2006\)](http://dx.doi.org/10.1103/PhysRevB.73.235116).
- [35] H. J. Monkhorst and J. D. Pack, [Phys. Rev. B](http://dx.doi.org/10.1103/PhysRevB.13.5188) **[13](http://dx.doi.org/10.1103/PhysRevB.13.5188)**, [5188](http://dx.doi.org/10.1103/PhysRevB.13.5188) [\(1976\)](http://dx.doi.org/10.1103/PhysRevB.13.5188).
- [36] K. Refson, P. R. Tulip, and S. J. Clark, [Phys. Rev. B](http://dx.doi.org/10.1103/PhysRevB.73.155114) **[73](http://dx.doi.org/10.1103/PhysRevB.73.155114)**, [155114](http://dx.doi.org/10.1103/PhysRevB.73.155114) [\(2006\)](http://dx.doi.org/10.1103/PhysRevB.73.155114).
- [37] V. Milman, A. Perlov, K. Refson, S. J. Clark, J. Gavartin, and B. Winkler, [J. Phys.: Condens. Matter](http://dx.doi.org/10.1088/0953-8984/21/48/485404) **[21](http://dx.doi.org/10.1088/0953-8984/21/48/485404)**, [485404](http://dx.doi.org/10.1088/0953-8984/21/48/485404) [\(2009\)](http://dx.doi.org/10.1088/0953-8984/21/48/485404).
- [38] N. L. Ross, J. Ko, and C. T. Pewitt, [Phys. Chem. Miner.](http://dx.doi.org/10.1007/BF00223309) **[16](http://dx.doi.org/10.1007/BF00223309)**, [621](http://dx.doi.org/10.1007/BF00223309) [\(1989\)](http://dx.doi.org/10.1007/BF00223309).
- [39] K. Leinenweber, W. Utsumi, Y. Tsuchida, T. Yagi, and K. Kurita, [Phys. Chem. Miner.](http://dx.doi.org/10.1007/BF00202576) **[18](http://dx.doi.org/10.1007/BF00202576)**, [244](http://dx.doi.org/10.1007/BF00202576) [\(1991\)](http://dx.doi.org/10.1007/BF00202576).
- [40] J. A. Linton, Y. Fei, and A. Navrotsky, Am. Mineral. **84**, 1595 (1999).
- [41] K. Parlinski, Z. Q. Li, and Y. Kawazoe, [Phys. Rev. B](http://dx.doi.org/10.1103/PhysRevB.61.272) **[61](http://dx.doi.org/10.1103/PhysRevB.61.272)**, [272](http://dx.doi.org/10.1103/PhysRevB.61.272) [\(2000\)](http://dx.doi.org/10.1103/PhysRevB.61.272).
- [42] A. Jayaraman and A. A. Ballman, [J. Appl. Phys.](http://dx.doi.org/10.1063/1.337366) **[60](http://dx.doi.org/10.1063/1.337366)**, [1208](http://dx.doi.org/10.1063/1.337366) [\(1986\)](http://dx.doi.org/10.1063/1.337366).
- [43] Y. Lin, Y. Li, Y. Xu, G. Lan, and H. Wang, [J. Appl. Phys.](http://dx.doi.org/10.1063/1.358596) **[77](http://dx.doi.org/10.1063/1.358596)**, [3584](http://dx.doi.org/10.1063/1.358596) [\(1995\)](http://dx.doi.org/10.1063/1.358596).
- [44] [A. S. Backer, A. A. Ballman, and J. A. Ditzenberger,](http://dx.doi.org/10.1103/PhysRevB.2.4233) *Phys. Rev.* B **[2](http://dx.doi.org/10.1103/PhysRevB.2.4233)**, [4233](http://dx.doi.org/10.1103/PhysRevB.2.4233) [\(1970\)](http://dx.doi.org/10.1103/PhysRevB.2.4233).
- [45] A. Ridah, P. Bourson, M. D. Fontana, and G. Malovichko, [J. Phys.: Condens. Matter](http://dx.doi.org/10.1088/0953-8984/9/44/022) **[9](http://dx.doi.org/10.1088/0953-8984/9/44/022)**, [9687](http://dx.doi.org/10.1088/0953-8984/9/44/022) [\(1997\)](http://dx.doi.org/10.1088/0953-8984/9/44/022).
- [46] I. Inbar and R. E. Cohen, [Phys. Rev. B](http://dx.doi.org/10.1103/PhysRevB.53.1193) **[53](http://dx.doi.org/10.1103/PhysRevB.53.1193)**, [1193](http://dx.doi.org/10.1103/PhysRevB.53.1193) [\(1996\)](http://dx.doi.org/10.1103/PhysRevB.53.1193).
- [47] L. Bayajargal and B. Winkler, [Z. Kristallogr.](http://dx.doi.org/10.1515/zkri-2013-1641) **[229](http://dx.doi.org/10.1515/zkri-2013-1641)**, [92](http://dx.doi.org/10.1515/zkri-2013-1641) [\(2014\)](http://dx.doi.org/10.1515/zkri-2013-1641).