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Melting at the base of the Greenland Ice Sheet explained by Iceland hotspot history

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88 Ice-penetrating radar¹⁻³ and ice core drilling⁴ have shown that large parts of the north-
89 central Greenland Ice Sheet are melting from below. It has been argued that basal ice
90 melt is sourced from the anomalously high geothermal flux^{1,4} that has also influenced
91 the development of the longest ice stream in Greenland¹. Here we estimate geothermal
92 flux beneath the Greenland Ice Sheet and identify a 1200-km-long and 400-km-wide
93 geothermal anomaly beneath the thick ice cover. We suggest this anomaly explains the
94 observed melting of the ice sheet's base, which drives vigorous subglacial hydrology³
95 and controls the position of the head of the enigmatic 750-km-long north-eastern
96 Greenland ice stream⁵. Our joint analysis of independent seismic, gravity and tectonic
97 data⁶⁻⁹ implies that the geothermal anomaly, which crosses Greenland from west to east,
98 was formed by Greenland's passage over the Iceland mantle plume between
99 approximately 80 and 35 million years ago. This study shows that the complexity of the
100 present-day subglacial hydrology and dynamic features of the north-central Greenland
101 Ice Sheet originated in tectonic events that predate the onset of Greenland glaciations
102 by many tens of millions of years.

103

104 Recent observations indicate that strong regional variations in geothermal flux (GF) dominate
105 the thermal regime and melting of the ice base beneath continental parts of the Greenland and
106 Antarctic ice sheets^{1,10}. Ice flows rapidly and subglacial hydrological systems develop where
107 GF is high and melt water is present under ice cover¹¹⁻¹². Despite being small compared to the
108 observed volumes of water discharged by surface melt¹³, GF-induced basal melt is important
109 because it occurs over large areas in the accumulation zone where there are no other basal
110 water sources, and disproportionately affects the overall dynamic behavior of large ice sheet
111 sectors^{1,14}.

112 Deep ice core measurements and data from airborne ice-penetrating radar support very high
 113 rates of basal melt for parts of the Greenland Ice Sheet (GIS)^{1,4}, for example, at the head of
 114 the longest ice stream in Greenland, which drains north-east from the summit dome¹. It has
 115 been argued that anomalously high GF, exceeding 100 mW/m², is required to produce
 116 estimated rates of basal melt in the north-central GIS^{1,4}. These values significantly exceed
 117 those expected for ancient continental crust¹⁵, i.e. 37 to 50 mW/m², which forms the center of
 118 the Greenland craton. Here we present a new reconstruction of GF across north-central
 119 Greenland to explain the origin of the observed melting beneath the ice cover (Figure 1). This
 120 reconstruction reconciles a large array of independent data sets through an iterative
 121 calibration of a coupled 3-D climate-forced model of the GIS and the underlying
 122 lithosphere¹⁶ against (i) Curie depths (580°C isotherm) from satellite magnetic data¹⁷, (ii)
 123 estimates of lithosphere thickness from seismic data¹⁸, (iii) bedrock borehole temperature
 124 measurements taken in eastern Greenland and at the continental shelf, (iv) ice temperature
 125 measurements from five deep ice cores¹⁹, (v) areas of basal ice melt inferred from ice-
 126 penetrating radar studies¹⁻³, (vi) areas of increased ice surface velocity from satellite
 127 observations⁴, and (vii) measured ice thickness²⁰ (see Methods).
 128 The reconstructed GF values range from 37 to 106 mW/m² and show a continuous area of
 129 elevated GF (75 – 106 mW/m²) running from Scoresby Sund in the southeast, towards near
 130 Melville Bugt in northwest Greenland (Figure 1). The GF in the zone of anomalously high
 131 values, although elevated relative to values expected for Precambrian Greenland crust, is
 132 lower than previous estimates^{1,4}, which were in the range 98 to 970 mW/m². These earlier GF
 133 estimates were derived from inferred basal melt rates, which may locally be modulated by
 134 factors independent of the solid Earth-sourced heat flux. Sources of significant local
 135 perturbations to basal melt rates are: heat advection through subglacial hydrology or
 136 hydrothermal circulation, basal ice sliding and meltwater refreezing. Because melting rates

137 are controlled by a combination of GF and non-GF influences, we build our calibration
138 strategy on estimating GF required to reproduce the observed thawed basal ice conditions,
139 discounting basal ice melt rates as a proxy for GF. This has the effect that GF estimates will
140 likely be biased downwards where basal melt is rapid; nevertheless, our strategy is
141 sufficiently effective to separate out the signal of a strong and spatially extensive geothermal
142 anomaly beneath the GIS and provides a hard lower bound for GF values at the observed
143 basal melt locations.

144 The anomalous GF zone lies in the area with the highest density of direct measurements.
145 These include two deep ice cores (NGRIP and NEEM) and radar soundings at the heart of the
146 anomaly (Figure 1). Three other ice cores (CC, GRIP and GISP2) bound the anomaly to the
147 west and south. The lateral dimensions of the reconstructed geothermal anomaly are roughly
148 1200 by 400 km, covering about a quarter of the Greenland land area. GF values in the
149 anomalous area are up to 2.5 times background GF values derived across the northern and
150 western parts of Greenland.

151 One potential cause of elevated GF is illustrated by seismic data that link our west-to-east GF
152 anomaly with a zone of low-seismic-velocity mantle, a "negative anomaly", beneath Iceland⁶
153 ⁷ and Greenland (Figures 1 and 2a-b). Negative anomalies in seismic velocity are commonly
154 associated with anomalously high temperature and compositional heterogeneity of mantle
155 rocks²¹. Iceland has been classified as a geological hotspot interpreted to result from
156 increased magma production attributed to a mantle plume^{6,22}, which is a narrow zone of
157 hotter than average mantle rock that rises several thousand kilometers from deep within the
158 Earth²³.

159 Paleoreconstructions of relative plate motion⁸⁻⁹ and evidence from igneous rocks in eastern
160 and western Greenland²² suggest that Greenland transited over the Iceland mantle plume
161 between ~80 and 35 million years ago (Figure 2a). When continental lithosphere moves over

mantle plumes, compositional and thermal changes, magmatism and lithosphere thinning may affect areas hundreds of kilometers wide²⁴ (see Supplementary Information). These changes may be independently inferred using anomalies in the observed gravity field (Figure S6), seismic velocity (Figures 2a-b) observations and reconstructed variations in the 1300°C isotherm depth (S5) beneath Greenland, as well as GF variability near its surface (Figure 1). In addition the reconstructed zone of anomalous GF is spatially correlated with highs in the dynamic topography²⁵ and isostatically compensated bedrock surface (Figure S7), both of which are likely induced by thermal anomalies in the mantle (see Supplementary Information). Our interpretation of the origin of the geothermal anomaly is further supported by evidence of former magmatism found under the present-day ice cover and along the western and eastern margins of Greenland. Mafic dyke fragments recovered from bedrock beneath the GISP2 ice core²⁶ are similar to basalts from eastern Greenland and there is evidence of large volcanic crater caldera-like formations under the north-central GIS¹. Together with abundant magmatic rocks from the Greenland margins (Figure 2a), these provide evidence for former volcanic activity in the area of anomalous GF, which may be directly or indirectly plume-related. Taken together, the accumulated evidence indicates that the prominent geothermal anomaly beneath the ice has its origin in the remanent thermal imprint and lithosphere thinning imposed by the plume's residence beneath Greenland tens of millions of years ago. This synopsis of independent evidence supports our earlier hypothesis¹⁶ that the lithosphere thinning beneath the Summit region of the GIS could have resulted from thermal erosion by the Iceland plume.

To date, paleoreconstructions of the Iceland plume history have been marked by a high degree of uncertainty in the location and timing of its residence beneath Greenland, resulting in proposed hotspot tracks located in a 1000-km-wide band from north to south (Figures 2a and S8). A joint interpretation of the geothermal anomaly reconstructed from independent

geophysical data (Figure 1) and seismic tomography data (Figures 2a-b) provides new evidence that the Greenland lithosphere passed over the mantle plume several hundred km from the tracks suggested by most existing paleoreconstructions. Of previously proposed plume tracks, the most northerly⁹ (Figures 2a and S3) best explains the location of the reconstructed geothermal anomaly. A cursory comparison might suggest that this plume track disagrees with evidence from hotspot-related magmatic rocks at the western margin of Greenland (Figure 2a), where the track reconstruction is less reliable (see Supplementary Information). The degree of disagreement is however hard to judge, since more extensive magmatic sequences supporting this northerly track may be hidden beneath the thick ice cover shielding most of the north-western margin of Greenland (Figure 1). In addition, previous studies have demonstrated that magmatic expression of the plume head at the surface may not necessarily coincide with the position of a plume-feeding conduit²⁷. A majority of basal ice melt identified by ice-penetrating radar and ice core measurements¹⁻⁴ lies within what we argue to be the area affected by the long-lived thermal and physical imprint of the Iceland plume (Figure 1). The reconstruction of subglacial thermal conditions suggests that about half of the north-central GIS is currently resting on a thawed bed, with extensive melting areas interconnecting fragmentary evidence of basal melt along the flight routes of radar-survey aircraft and at the location of the NGRIP ice core (Figure 3a). In addition we have identified numerous regions such as, for example, in the surroundings of the NEEM ice core, where basal ice is nearly at the pressure-melting point and may contain some meltwater. High basal melt rates estimated from internal ice layering account for several mm to cm of ice annually lost to melting¹. Since substantial subglacial lakes are uncommon in Greenland²⁸, the generated basal meltwater has to be effectively routed towards the ice sheet margins without ponding along the way. A recent subglacial topographic study³ has

suggested potential pathways for drainage of subglacial meltwater, where it may exist, from beneath the GIS. We have compared the topography of this potential drainage system with our reconstructed areas of basal melt and selected for the most likely paths along which the subglacial meltwater must be evacuated (Figure 3a). The overwhelming majority of the previously suggested potential hydrological routes³ cluster within our predicted basal melt areas, and may be currently active. Furthermore, most of these routes have their headwaters in the zone of the geothermal anomaly. We argue that the combination of enhanced melting, elevated GF, concentration of hydrological pathways, and deeply incised subglacial topography²⁰ can be explained by the long-lasting imprint of the passage of Greenland over the Iceland mantle plume.

The tectonothermal history is also implicated in the location of development of rapid ice flow in central Greenland. Existing studies attribute the start point of the 750-km-long North-Eastern Greenland Ice Stream (*NEGIS*, Figure 3b) to the influence of high GF and rapid basal melt located at its head¹. Our study demonstrates that the areas of high GF and basal ice melt inferred from ice-penetrating radar studies¹ and the start point of the *NEGIS*⁵ (Figure 3b) are all located within the reconstructed geothermal anomaly. The elevated GF however is unlikely to be the only factor controlling the observed speed and shape of the *NEGIS*, which may also be modulated by ice geometrical settings, subglacial hydrology and mechanical properties of the ice-bedrock interface²⁹.

Our reconstruction of the present-day thermal regime of the GIS reveals more extensive areas of GF-induced basal ice melt than previously recognised¹⁻⁴ and makes it possible that a dense network of subglacial meltwater pathways is currently operating beneath the ice, most of which spring from the zone affected by passage over the Iceland plume. Despite the weight of aggregated evidence presented here, it has not previously been hypothesised that the observed melting beneath large sectors of the GIS and anomalous ice streaming in north-eastern

Greenland may be the expression of Iceland hotspot history. The geothermal anomaly provides evidence for a more northerly hotspot track than previously proposed and will offer a useful test for existing paleoreconstructions of absolute plate motion. This study advocates a previously undocumented strong coupling between Greenland's present-day ice dynamics, subglacial hydrology, and the remote tectonothermal history of the North Atlantic region.

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Author contributions

I.R. developed the concept. I.R. and A.G.P. designed and performed all numerical experiments. I.R. and A.P.M.V. wrote the manuscript, with the assistance of A.G.P., B.S. and J.V.J. A.G.P. analyzed the seismic tomography models provided by F.R. and I.K., prepared the map of crustal thickness, assembled the measured GF values from the continental shelf of Greenland and prepared and described the materials related to the model setup and thermal state of the Greenland lithosphere. B.S. prepared and described the materials related to existing plume track reconstructions and contributed to the design of Supplementary Information. J.V.J. tested the GF map using his high-resolution Greenland ice sheet model VarGlaS. M.K.K. performed the analysis of the observed gravity data. All authors contributed to discussions and interpretations of the results.

Additional information

The authors declare no competing financial interests.

386 **Code and data availability**

387 All data and the components of the coupled 3-D ice sheet-lithosphere model are available in a
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Figure captions

Fig. 1. Predicted GF [mW/m^2] at 5 km depth below bedrock surface. GF was corrected for crustal heat production using a parameterization of radiogenic heat sources (see Methods). Modeled thermal state of the GIS and lithosphere calibrated by in-situ data shown by orange/black triangles (filled - ice cores, unfilled - bedrock borehole measurements) and black/white crosses^{1,4}, diamonds² and stars³ (basal melting from radar and ice core measurements). Deep ice core locations¹⁹: CC, NEEM, NGRIP, GRIP, GISP2 and Dye3. Measured basal ice temperatures and GF from bedrock boreholes (1-7) presented in Tables S4-S5. White curves outline ice sheet and coastal margins.

Fig. 2. Geophysical data indicating lithosphere anomalies beneath Greenland. a) S-wave velocity model of the North Atlantic region⁵ shown for the Greenland region at 120 km depth⁵, colour-mapped for percentage velocity anomaly. Areas of hotspot-related magmatism are hatched and labeled for age³⁰. Iceland hotspot track reconstructions⁸⁻⁹ are shown as continuous lines for 0-60 Ma and dashed lines prior to 60 Ma (see Figure S8 caption). b) P-wave velocity model of the circum-Arctic region⁷ shown for north-central Greenland at 150 km depth, colour-mapped for percentage velocity anomaly. Black and orange triangles mark ice core and bedrock borehole locations as in Figure 1.

Fig. 3. Predicted basal thermal state of the present-day GIS. a) Modeled basal ice temperature below the pressure-melting point [$^{\circ}\text{C}$], with superimposed potential active hydrological routes adopted from a subglacial topographic study³ (red curves, see Full Methods, M2). Areas coloured white are where our model predicted melting at ice sheet base. Triangles mark ice core locations. b) The reconstructed geothermal anomaly (contours) superimposed on the observed surface ice velocity⁵ (colour-mapped) of the north-eastern GIS [m/a] shows that the head of the North-Eastern Greenland Ice Stream (labeled by NEGIS) is located in the area of the highest GF values (above 90 mW/m^2).

Methods

M1. Model description and forcing

Description: Our modelling strategy uses a 3-D fully coupled thermomechanical model of the GIS and the lithosphere¹⁶. The ice component is implemented using the 3-D finite-difference ice sheet model (ISM) SICOPOLIS based on the shallow ice approximation and the rheology of an incompressible, heat-conducting, power-law fluid described by Glen's flow law³¹. Numerical solutions of mass, momentum and energy balance equations describe ice dynamics and thermal evolution of the GIS. The model is polythermal and allows formation of temperate ice at the ice sheet's base, overlain by a thick layer of cold ice. Mass- and energy-flux conditions at the interface between cold and temperate ice are realized through the solution of the Stefan problem³¹. Surface melting and refreezing are calculated using a temperature index³² and a meltwater retention³³ methods. Basal sliding is described by a Weertman-type sliding law³⁴. The parameters of the ISM (Table S1) were calibrated using an iterative approach described in Section M2 to attain the best possible fit with the observed ice thickness. The lithospheric model is implemented using the 3-D finite-volume thermo-mechanical code Lapex 3D³⁵⁻³⁶ incorporating a non-linear temperature- and stress-dependent visco-elasto-plastic rheology with parameters consistent with laboratory measurements (Table S2). The lithosphere model includes the upper and lower crust and the lithospheric mantle and adopts a pressure-temperature-dependent law for thermal diffusivity in both the lithospheric mantle and the crust³⁷. The bedrock surface is constructed using the most recent compilation of ice-penetrating radar measurements²⁰. The thickness of the crust across north-central Greenland is based on CRUST1.0³⁸, regionally adjusted to fit the estimates from S-receiver functions³⁹ and gravity data⁴⁰. The crust is subdivided into two parts of equal thickness with different thermal properties: the felsic crust with higher radiogenic production and the mafic crust with lower radiogenic production⁴¹. Here we

employ a uniform distribution of radioactive elements within the upper crust, and mean crustal heat production of $0.3 \mu\text{W}/\text{m}^3$ estimated in our previous study for central Greenland¹⁶ in agreement with bedrock borehole measurements from western Greenland^{16,42}. Our previous studies^{16,35-36,43} describe the 3-D ice sheet and lithosphere model components in more detail.

Boundary conditions: The ice sheet and lithosphere components are coupled through boundary conditions, requiring continuity of internal energy and normal stress at the exchange boundary¹⁶ using the methodology of Greve³¹. The hydrostatic pressure at the base of the ice sheet is transmitted to the lithospheric model as a loading that produces a dynamic response in the lithosphere. The resulting surface subsidence or uplift is then passed back to the ISM as a correction to the bedrock topography.

The lower boundary of the thermal lithosphere is defined as the depth where the asthenospheric potential temperature reaches 1300°C ¹⁵. The Winkler boundary condition that implies zero viscous drag forces and hydrostatic normal-to-surface stress is prescribed at the lower boundary of the model box. Free slip boundary conditions (the normal-to-boundary component of velocity vector is equal to zero) are set for the upper 50 km at the side boundaries, whereas the remaining boundaries are open for in-out flow. No conductive heat exchange is allowed at these boundaries, i.e., the thermal gradient is equal to zero.

The coupled model is driven from above by time-evolved temperature and precipitation forcing over the period of large-scale glaciations in Greenland, which are assumed to have initiated in the Mid-Pliocene⁴⁴. Climate history is inferred using an empirical relation⁴⁵ to combine surface temperature records from ice cores with precipitation. The air temperature forcing uses the combined GRIP-EPICA surface temperature record^{16,45-46} applied as a time-varying spatially uniform offset from the present-day air temperature distribution across Greenland, corrected for the monthly lapse rates inferred from in-situ measurements⁴⁷. The

precipitation field across Greenland is derived at each time step by applying a scaling to the present-day precipitation rate⁴⁸ depending on the temperature offset relative to the present. The global sea level forcing is derived from the SPECMAP marine $\delta^{18}\text{O}$ record⁴⁹. Prior to the onset of large-scale glaciations 3 Ma, we initialize the Greenland lithosphere model to a thermal equilibrium with a surface temperature of 0°C ⁴⁴ at the ice-free upper boundary. The components of the coupled model together with their boundary conditions are schematically illustrated in Figure S1.

Discretization: Simulations are performed with a horizontal resolution of 10 km. The ISM and the thermal component of the lithospheric model are run with a time step of 1 year, whereas the mechanical component of the lithospheric model uses a time step of 100 years. The vertical resolution is non-uniform and provides grid densification towards the ice-bedrock interface in both lithosphere and ice sheet model components. Computational grids adopted by the SICOPOLIS and Lapex 3D codes coincide at the interface surface (in the nodes where temperature is evaluated). The vertical grids within cold-ice and temperate-ice columns include 81 and 11 points, respectively⁵⁰. Vertical resolution of the lithospheric model component is 1 km in the upper crust and 5 km below. Temperature distribution within the upper 5 km of the crust is calculated on a fine sub-mesh including 161 vertical grid points densifying towards the lithosphere surface.

M2. Model calibration

Throughout the modelling procedure we apply a multi-step calibration of the ice-lithosphere model against magnetic and seismic data, observations of the present-day GIS and GF estimates from the bedrock temperature measurements (see section M3). Major steps of model calibration are schematically shown in Figure S2.

Stage I: The 1300°C isotherm depth is first derived from a 1-D model of ice and lithosphere¹⁶ using the Curie depths (580°C) from satellite magnetic data¹⁷ and seismic lithosphere

thickness from S-receiver functions^{18,51} as constraints. The resulting non-linear evolution equation for vertical advection and diffusion is solved with finite differences, using the procedure described in our previous study¹⁶. The thickness and structure of the crust are taken to be identical to those adopted by the 3-D ice-lithosphere model (see Section M1).

Stage II: The preliminary map of the 1300°C isotherm depth obtained from Stage I is then used to define a lower thermal boundary in a 3-D GIS-lithosphere model. From a reference simulation of the GIS-lithosphere history spanning 3 million years we estimate the deviations from the observed present-day ice thickness²⁰ and balance ice velocity⁵². As a result we also derive the states of the GIS and lithosphere for the time slice corresponding to 100 ka, which are then used as initial conditions at Stage III⁵³.

Stage III: We run a suite of simulations starting from the initial condition (100 ka) to select general parameters of the ISM (basal sliding coefficient, ice flow enhancement factors, degree-day factors for snow and ice, daily temperature standard deviation and temperature-dependent snow-rain fractionation of precipitation) in order to achieve the best possible fit with the observed present-day ice sheet thickness²⁰ and balance velocity⁵² and to derive our intermediate maps of GF distribution and basal ice temperatures across north-central Greenland. At this stage we calibrate the GIS model component using an adaptive random search algorithm developed for optimization of nonlinear systems with many parameters⁵⁴⁻⁵⁵.

To reduce the computation time, main stages of the process have been parallelized following a strategy applied to the parameter search using coupled simulations with increasing horizontal (10-20 km) and temporal (1-10 years) resolution, thereby gradually narrowing permissible regions for each parameter. Here we use the following objective function to measure the goodness of the fit of the ice thickness and surface speed to the observations:

$$J(\alpha) = \sqrt{W_H S_H + W_v S_v}, \quad (1)$$

$$\text{where } S_H = \sum_{H_{obs}(x,y) \geq H_{thresh}} \left(1 - \frac{H(x,y)}{H_{obs}(x,y)}\right)^2, \quad (2)$$

$$S_v = \sum_{H_{obs}(x,y) \geq H_{thresh}} \left(1 - \frac{v(x,y)}{v_{obs}(x,y)}\right)^2, \quad (3)$$

where $H(x, y)$ and $H_{obs}(x, y)$ are the computed and observed ice thickness, and $v(x,y)$ and $v_{obs}(x,y)$ are computed and balance ice speed, respectively.

The fit is only evaluated where the present-day ice thickness exceeds 1.5 km ($H_{thresh} = 1.5$ km), since the focus of this study is on the inland areas where GF is one of the major factors shaping subglacial thermal conditions. In addition this results in a minimal influence of the deficiencies of the shallow ice approximation on our choice of the general parameters of the ISM component⁵⁶. Due to higher significance of the fit between the modelled and observed ice thickness for the reconstruction of basal ice temperatures in the targeted areas, unequal weights of $W_H = 0.78$ and $W_v = 0.22$ have been empirically chosen for calibration.

Using this approach we calibrate model parameters that have the strongest influence on the modelled present-day ice thickness and ice flow pattern. Here we refrain from making assumptions about spatial variability in such parameters as basal sliding coefficients and ice flow enhancement factors, since observational data are currently insufficient to support such assumptions. We therefore search for the best-fit single values of relevant parameters within the ranges adopted from existing literature that are commonly applied to the modelling of the large-scale characteristics of the GIS. The only exception is the daily temperature standard deviation parameter in a temperature-index method, which has recently been reported highly variable across Greenland⁵⁷⁻⁵⁸ and strongly dependent on variations in surface temperature⁵⁹⁻⁶⁰. We have tested the performance of the two existing temperature-dependent parameterizations of daily temperature standard deviation⁵⁹⁻⁶⁰ and concluded that the use of the latter parameterization⁶⁰ over the Holocene period yields better results for the present-day GIS thickness. Since the existing temperature-dependent parameterizations of daily temperature standard deviation are inferred from the present-day observations and their applicability to glacial periods has not yet been demonstrated, our calibration strategy

includes the search of a best-fit daily temperature standard deviation parameter in the period prior to the Holocene interglacial within the range of previously reported constant values. The ranges of tested parameter values (initial permissible regions) are provided in Table S3.

Stage IV: After the calibration of the modelled ice thickness and ice velocity we evaluate the agreement between the model and available direct constraints from the ice sheet and bedrock (GF and ice core temperature measurements, basal melt locations from radar soundings, and inland regions of high ice velocity, see Figure 1 and Tables S4 and S5) and outline the locations/areas that require corrections to the GF estimates. Again, we only use those constraints from the ice sheet that fall within the area with the present-day ice thickness above 1.5 km, for which the ISM parameters are calibrated at Stage III. In particular, this is done to exclude observational data falling within the zones where surface meltwater delivery to the ice sheet bed⁶¹ and ocean-induced variations in glacier dynamics and subglacial hydrology⁶² may have significant effects on the basal thermal regime of the present-day GIS. For the areas where the dynamic features are poorly captured after the calibration procedure at Stage III, we apply a fairly restrictive tuning method. In such areas local adjustments of the initial 1300°C-isotherm depth are limited to a maximum correction of $\pm 15\%$ to the modelled Curie depth, which is within the range of anticipated errors in the estimates from the satellite magnetic data⁶³ (see M3). Due to the diverse nature of available constraining data, the calibration process could not be fully automated. Across ice-covered areas, we have set up a correspondence between each direct constraint from the ice sheet and the modelled horizontal ice velocity within the grid cell where the constraint is located. For GF measurements from the bedrock the velocity value has been set to zero. The constraints have been sorted according to the corresponding velocity value in order to account for the growing influence of the horizontal advection on the thermal regime of the neighbouring areas towards the ice

585 sheet margins. The calibration has therefore been organized starting from data points with
586 minimal velocity values.

587 The GF estimates derived from Stage III are adjusted to fit observations over each outlined
588 area through successive perturbations to the preliminary map of the 1300°C isotherm depth
589 from Stage II leading to local increases/decreases in subglacial heat flow, modelled basal ice
590 temperature and vertical temperature gradients. The perturbations are performed across the
591 neighbourhood of each data point representative of the resolution of the magnetic data¹⁷ used
592 at Stage I (see M3). Following a simple under-relaxation procedure, only a fraction of the
593 correction value necessary to fit each individual constraint is retained, depending on the ice
594 flow velocity value within the grid cell where the correction was estimated:

$$595 \quad H_n^L(x, y) = H_{n-1}^L(x, y) + \alpha(H_n^{L*}(x, y) - H_{n-1}^L(x, y)), \quad (4)$$

596 where $\alpha = (1 - \frac{v(x,y)}{2v_{max}})$, v_{max} is the maximum absolute value of the horizontal ice flow
597 velocity in the areas subject to corrections, and $H_n^{L*}(x, y)$ and $H_{n-1}^L(x, y)$ indicate the 1300°C
598 isotherm depths, which are estimated to fit the surface constraint for the iteration n and
599 obtained from the previous iteration ($n-1$), respectively.

600 Overlapping corrections are combined using a weighted average, with the weights inversely
601 proportional to the distances to the locations of the constraining data. The correction map is
602 then smoothed using a low-pass filter. Stages II – IV are repeated until the process converges
603 to the best-fit solution with all constraints using updated maps of 1300°C isotherm depths
604 within individual threshold values established for each type of constraint.

605 The final series of simulations is run in order to introduce final adjustments at the locations
606 where the smoothing procedure, or interference between perturbations over neighbouring
607 areas, affected the fit with observations.

608 **Stage V:** At the last stage we infer the potential subglacial hydrology beneath the north-
609 central GIS from the hydrology network calculated by [ref. 3] using the hydraulic potential

equation of [ref. 64] and the approach of [ref. 65] for routing subglacial meltwater over the hydraulic potential surface. We have superimposed these potential hydrological routes on the reconstructed basal ice temperature of the present-day GIS. Among them, the routes that fall within the areas of predicted basal ice melting have been selected as the most probable routes of currently active subglacial hydrology (shown by solid red curves in Figure 3a). We have also retained the potential hydrological routes that fall within the areas with the ice base close to the pressure-melting point (dashed red curves in Figure 3A) where the presence of meltwater is probable but may not be retrieved by our model due to insufficient horizontal resolution (see M1) that acts as a filter of high-frequency signals present in the original bedrock topography data set²⁰.

M3. Description of model constraints

At Stage I we use estimates of Curie depths¹⁷ from satellite magnetic data and lithosphere thickness from seismic data^{18,51} to derive our initial 1300°C isotherm depths. The Curie depth map was inferred with a horizontal resolution of a few hundred km and an uncertainty of about $\pm 15\%$ ⁶³. The estimates of seismic lithosphere thickness are provided as average values over eight areas of variable size¹⁸ and along S-N profiles in central Greenland⁵¹. Most of the average values are derived across the areas with the dimensions of about 500 km (S-N direction) by 200 km (W-E direction).

At Stage III the model is calibrated versus ice thickness from radar soundings²⁰ and balance ice velocity⁵². Ice thickness is provided with a horizontal resolution of 1 km (Figure S3), although this resolution may not locally be reached due to uneven distribution of radar measurements across Greenland²⁰. The uncertainty in the observed ice thickness mostly exceeds 100 m, with the highest uncertainty of more than 150 m occurring in East Greenland and along the GIS margin²⁰. Following the approach described in [ref. 52], we determine balance velocity by minimizing the difference between balance and observed surface speed,

635 using accumulation and its associated uncertainty as a control variable. Its distribution is
636 given on an unstructured grid densifying towards the areas of rapid flow, with an average
637 horizontal resolution of 2 km. Balance, rather than observed velocity is used for its continuity
638 around the ice divide and lack of noise in regions of low speed. To enable a one-to-one
639 comparison between the modeled and observed fields, we have smoothed the observational
640 fields by assigning an average value to each model grid cell.

641 At Stage IV we calibrate our model versus in-situ measurements of basal ice temperature and
642 GF and basal ice melt from radar soundings. The uncertainties in ice core measurements are
643 low (e.g., 0.0045°C for GISP2⁶⁶), whereas GF estimates are likely less reliable, since most of
644 the GF values have been derived from relatively shallow boreholes (<1 km depth) and have
645 not been corrected for paleoclimate signal^{42,67-68}. To constrain the areas of melting beneath
646 the GIS we use three datasets derived from ice-penetrating radar measurements¹⁻³
647 (schematically shown in Figure 1). The first dataset¹ comprises estimates of melt rates
648 beneath the north-central GIS from an interpretation of the internal ice layering. To date, this
649 is the only dataset that includes quantitative analysis of basal melt rates across a large sector
650 in Greenland. The estimated rates may be corrupted by the assumption of equilibrated climate
651 conditions and simplified treatment of the horizontal flow¹ but the inference of basal melt
652 locations is relatively robust. The second dataset² hypothesizes the presence of subglacial
653 water based on an empirical relation between relative reflection intensity and thawed/frozen
654 interfaces⁶⁹. Comparison of the first and second datasets across the area included in both
655 studies reveals comparable large-scale patterns of basal melt, with local discrepancies in the
656 predicted melt locations. This may be partly explained by high sensitivity of the method used
657 in the second study to the uncertainties in the bed roughness^{2,69}. In addition, the empirical
658 relation uses a somewhat arbitrary threshold to distinguish between melting and frozen areas.
659 Indeed, the authors admit that their inferred subglacial meltwater is not always consistent

with ice core measurements (for example, subglacial meltwater is found in the vicinity of the Camp Century (CC) ice core where basal temperature of -13°C has been measured, see Table S4). The third dataset³ is based on an analysis of the reflections in the radar soundings used to detect basal units of refrozen meltwater, which can be indirectly linked to subglacial melting in the vicinity of these areas. Although the exact locations of subglacial melt cannot be directly inferred from this dataset, here we assume that the identified basal units are situated in a close proximity to the hypothesized subglacial melt (within the same grid cell). Over the overlapping areas we assign higher weights to the constraints from the first dataset.

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