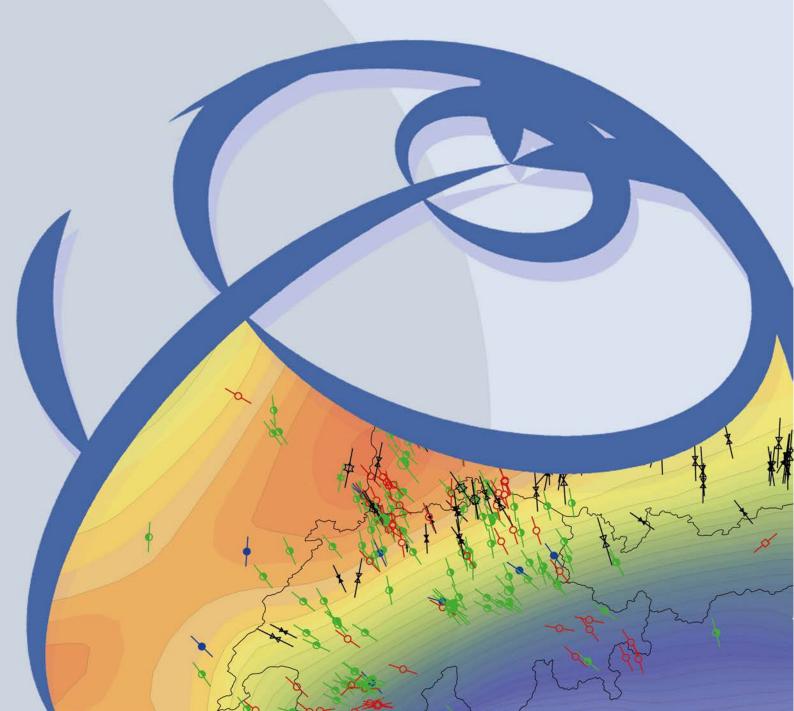


WSM Technical Report 17-01

Manual of the Tecplot 360 Add-on GeoStress

Dietrich Stromeyer and Oliver Heidbach



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Manual of the Tecplot 360 Add-on GeoStress

Dietrich Stromeyer and Oliver Heidbach GFZ German Research Centre for Geosciences, Potsdam, Germany



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Abstract

For the visualization and analysis of the stress field from 4D thermo-hydro-mechanical (THM) numerical model results two main technical steps are necessary. First, one has to derive from the six independent components of the stress tensor scalar and vector values such as the orientation and magnitude of the maximum and minimum horizontal stress, stress ratios, differential stress. It is also of great interest to display e.g. the normal and shear stress with respect to an arbitrarily given surface. Second, an appropriate geometry should be given such as cross sections, profile e.g. for borehole pathways or surfaces on which the model results and further derived values are interpolated. This includes the three field variables temperature, pore pressure and the displacement vector.

To facilitate and automate these steps the add-on *GeoStress* for the professional visualization software Tecplot 360 EX has been programmed. Besides the aforementioned values derived from the stress tensor the tool also allows to calculate the values of Coulomb Failure Stress (CFS), Slip and Dilation tendency (ST and DT) and Fracture Potential (FP). *GeoStress* also estimates kinematic variables such as horizontal slip, dip slip, rake vector of faults that are implemented as contact surfaces in the geomechanical-numerical model as well as the true vertical depth. Furthermore, the add-on can export surfaces and polylines and map on these all availble stress values.

The technical report describes the technical details of the visualization tool, its usage and exemplifies its application using the results of a 3D example of a geomechanical-numerical model of the stress field. The numerical solution is achieved with the finite element software Abaqus version 6.11. It also presents a number of special features of Tecplot 360 EX in combination with *GeoStress* that allow a professional and efficient analysis. The Add-on as well as the example and input files used in this manual are published by Stromeyer and Heidbach (2017) and the table below gives an overview of these files with a short explanation.

File Name	Explanation	Page
example.odb	db Abaqus output file with model results that is loaded into Tecplot 360	
example.plt	Binary Tecplot format where the Abaqus results are stored	5
example.lay	Layout file that is controlling how the *.plt file is visualized	5
GeoStress_win64.dl GeoStress_lin64.so	The library compiled for Windows 64 and Linux 64 operating system format, respectively	13
tecplot.add	Edited Tecplot file where additional libraries have to be stated	13
topograhy_nodes_only.txt	ASCII input file of the model surface nodes in order to calculated the value True Vertical Depth (TVD)	18
FP_plastic_properties.txt	ASCII input file to calculate the Value Fracture Potential (FP)	23
<pre>fault_1_N.txt, fault_1_S.txt fault_2_N.txt, fault_2_S.txt</pre>	ASCII input file with nodes and elements that belong to a contact pair e.g. to calculate the relative displacement	38
external_surface.txt	ASCII input file with nodes and elements of an external arbitrary surface on which model results are mapped	42
external_polyline.txt	ASCII input file with nodes of an external arbitrary polyline on which model results are mapped	44
3D_View_Z_Displacement.sty	Definition of a certain view style on a model result	45
macro_example_RSR.mcr macro_example_RSR_edited.mcr	Marco files that contain a number of Tecplot commands	46
delta_K.eqn displacements.eqn	Pre-defined mathematical operations that can be loaded in order to derive from the existing variables new values	47

1 Introduction

1.1 Motivation and objectives

With the development of high-resolution 4D geomechanical numerical models that simulate the 3D stress tensor and its spatio-temporal changes due to natural (e.g. plate tectonics, earthquakes, erosion, sedimentation) and man-made processes (e.g. fluid injection/production, heat extraction, mining) the efficient and user-friendly visualisation of the model results became the most time consuming step within the model workflow. Typically, there are three issues that arise during the interpretation of the model results, i.e. in particular the stress tensor analysis:

- (1.) The visualization capabilities provided in the post-processing tools of the commercial finite element packages do not provide scalar and vector values such as the tectonic stress regime, the orientation of maximum horizontal stress or stress ratios required in geosciences. Furthermore, the derivation of normal and shear stress with respect to arbitrary surfaces is not possible without major effort and internal programming in the post-processing codes.
- (2.) The output figures are mainly based on screen shots. Thus, the combination with other data is limited and the quality of the figures that are produced by the software is mostly not acceptable for publication purposes. Furthermore, the access of the values in ASCII files for further post processing and/or combination with other data (e.g. from a cross section through the values including the coordinates) is either not comfortable or even not possible.
- (3.) The internal interpolation schemes are hardly documented, often inefficient and limited when it comes to the analysis of e.g. relative displacement along pre-existing faults in a model (simulated by so-called contact surfaces).

To significantly speed up the analysis as well as to increase the quality and flexibility of the model result analysis *GeoStress* has been programmed as an add-on to the commercial visualization software Tecplot 360 EX (in the following we always refer to the version 2015 R2). Also, the add-on *GeoStress* is independent from the incorporated finite element solver. Tecplot 360 EX is dedicated for the analysis and visualization of unstructured data that come from commercial finite element software packages, fluid dynamic codes and other numerical solvers. The data loader of Tecplot 360 EX can read the binary files from the leading commercial finite element codes (e.g. Abaqus or Ansys) and provides a reader for ASCII data. Tecplot 360 EX allows a professional programming of add-ons in C or Fortran 90 and access to all model variables, details of the mesh and the incorporated interpolation schemes. The output can be ASCII, images in user-defined resolution postscript, vector files and movies in different output formats. The add-on is explicitly made for the analysis of the stress tensor and displacement vector, but Tecplot 360 EX can also handle the results of thermo-hydromechanical (THM) models and visualize the temperature and pore pressure field.

After this introduction, the report is followed by three parts. Chapter 2 provides a brief introduction into the basic functionality of Tecplot 360 EX with an emphasis on the key terms that are used in the add-on *GeoStress* description and the accompanying application examples. For further details, we refer to the manuals of Tecplot 360 EX. In Chapter 2 we also describe the installation of the add-on *GeoStress*. However, the report does not provide information on the geomechanical-numerical modelling workflow or the basic of the meshing of a volume into

finite elements and the numbering of nodes and elements. For details on these issues we refer to publications such as Reiter and Heidbach (2014) or Hergert et al. (2015).

Chapter 3 presents the functionality and usage of *GeoStress*, explains the physical and mathematical background and gives application examples from a 3D geomechanical-numerical model of the potential siting area for high-level radioactive waste Nördlich Lägern (NL) in Switzerland. Details of the NL model setup are presented in the NAGRA report NAB 13-88 (Heidbach et al., 2013). Finally, Chapter 4 presents a number of additional Tecplot 360 EX applications in a geoscientific context that can potentially accelerate the analysis procedure significantly.

1.2 Stress term definitions

In geoscientific and rock engineering literature, there is no agreement on stress term definitions. Thus, a brief description is given in Table 1.3-1 on how stress terms are used in this report.

Tab. 1.3-1:	Definition of stress terms.

Since there is no strict definition of stress terms (e.g. Engelder, 1992; 1994; Jaeger et al., 2007; Schmitt et al., 2012), a brief definition of the stress terms used in this report is given.

Term	Symbol	Definition/Comment
in-situ stress state	-	Undisturbed natural (virgin) stress state. In particular, the in-situ stress is the sum of all natural stress contributions and natural processes that influence rock stress state at a given point.
disturbed in-situ stress state	-	Denotes that the in-situ stress is disturbed due to man-made changes such as impoundment, drilling, tunnelling, mining, fluid stimulation, reservoir depletion, or re-injection of waste water to name a few.
principal stresses	S ₁ , S ₂ , S ₃	The symmetric stress tensor can always be transformed into a principal axes system (Jaeger et al., 2007). The three remaining non-zero components in the diagonal of the matrix are the principal stresses where S_1 is the largest and S_3 the smallest ($S_1 \ge S_2 \ge S_3$).
differential stress	$S_{d} = S_{1} - S_{3}$	Difference between the largest and the smallest principal stress.
effective stresses	S'	Effective stresses S' are total stresses S minus pore fluid pressure $p_f.$
vertical stress	Sv	The magnitude of S_v is the integral of the overburden load. Only at the Earth surface S_v is one of the principal stresses; at greater depth S_v can deviate from a principal stress orientation.
magnitude and orientation of maximum and minimum horizontal stress	S _{Hmax} , S _{hmin,} S _{Hazi}	S_{Hmax} und S_{hmin} are the principal stresses of the 2D horizontal part of the 3D stress tensor with $S_{Hmax} \ge S_{hmin}$. Their orientation is uniquely defined by the angle clockwise from north. Assuming that S_V is a principal stress S_{Hmax} and S_{hmin} are principal stresses as well. S_{Hazi} is the orientation of S_{Hmax} in the 2D horizontal.
stress regime	-	Relates to stresses: The stress regime is an expression of the relative magnitudes of the principal stresses. It can be expressed as a con- tinuous value using the Regime Stress Ratio (RSR) with values between 0 and 3 (Simpson, 1997). For further details see section 3.2.

Term	Symbol	Definition/Comment
tectonic stresses	-	According to Engelder (1992) tectonic stresses are the horizontal components of the in-situ stress state that deviate from a given reference stress state (e.g. uniaxial, lithostatic). In particular, a reference stress state implies that $S_H=S_h$. However, definitions in the literature are not consistent. Tectonic stress must not necessarily equal the deviatoric stress which is the non-isotropic part of the stress tensor (the isotropic part is the mean stress S_m or one third of the trace of the of stress tensor $S_m = 1/3(S_{XX}+S_{YY}+S_{ZZ}) = 1/3(S_1+S_2+S_3)$. This is only true when one assumes that the reference stress state is lithostatic ($S_{Hmax}=S_{hmin}=S_V$ with the assumption that S_V is a principal stress).
tectonic regime	-	Relates to fault kinematics: Thrust faulting, normal faulting and strike-slip after Anderson (1905). Only when faults are optimally oriented in the stress field the stress regime is coincident with the tectonic regime (Célérier, 1995). Normal faulting: $S_V > S_{Hmax} > S_{hmin}$; Thrust faulting: $S_{Hmax} > S_{hmin} > S_V$; Strike-slip: $S_{Hmax} > S_{hmin}$.

2 Data visualisation with Tecplot 360 EX

2.1 Introduction

The following explanations are accompanied by an example using a geomechanical-numerical model of a potential siting area for high-level radioactive waste in Northern Switzerland (Heidbach et al., 2013). The model has several lithological layers with different elastic rock properties and the model volume is cut by two faults that strike approximately E-W (Fig. 2.1-1). After loading the initial equilibrated stress conditions due to gravity, horizontal displacement boundary conditions are applied to add the tectonic stresses. The model is shortened in N-W direction by 12 m and stretched in E-W direction by 1 m at each side. The Abaqus model result file (*.odb) contains four increments in one Abaqus step in which the displacement boundary conditions are step-wise increased. Since the model is purely elastic with Coulomb friction at the implemented faults, the increments are not time steps. Thus, the *Solution Time* given as 0.25, 0.5, 0.75 and 1.0 are arbitrary dimensionless numbers. E.g. in increment 0.25 the model is shortened by 3 m in N-S direction and pulled at the eastern and western boundary by 0.25 m each, respectively.

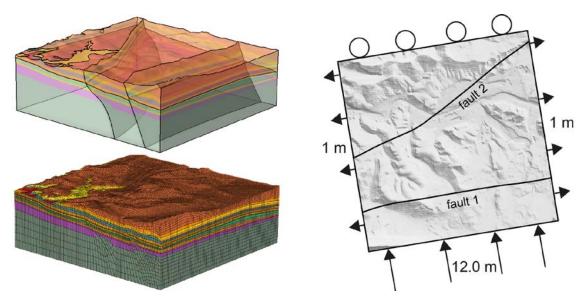


Fig. 2.1-1: Geometry, mesh and boundary conditions of the example model. Upper left figure shows the lithological layering and the fault location that cut the model into three blocks. Lower left figure shows the model discretization into finite elements. The figure to the right shows the total displacement boundary conditions applied at the southern, western and eastern model boundaries. The circles on the northern boundary denote that no displacement is allowed perpendicular to the model boundary.

Further technical details of the model setup and interpretation of the results can be found in the report NAB 12-88 from Heidbach et al. (2013). The Abaqus results are provided in the file *example.odb*. The Tecplot-files are named accordingly *example.lay* and *example.plt*.

2.2 Basic concept and terminology of Tecplot 360 EX

This section gives a brief introduction for the Tecplot 360 EX key words *Zone, Set of Zones, Time Strand,* and *Solution Time*. These terms are essential for the understanding how Tecplot 360 EX organizes the visualization of the model results. For further information, we recommend to read the Tecplot 360 EX manuals.

The graphical user interface of Tecplot 360 EX has four main areas (Fig. 2.2-1). The menu bar on the top offers all functions. Below the menu bar the tool bar offers several buttons for fast access to the key functions of Tecplot 360 EX. In the central large window Tecplot 360 EX displays the results of the selected *Zone* of your current analysis in frames. Different views or time steps of the model results can be displayed in several frames. The side bar on the left provides an easy access to the most common plot controls. The functions in the side bar depend on the plot type of the active frame. For 2D or 3D Cartesian plot types the *Zone Style dialog box* displayed in Fig. 2.2-2 can be used to select the *Zones* that are shown in the active frame. For XY and Polar line plots the graphic is controlled by the mapping layer dialog box.

In general, the whole model data set is structured in Tecplot 360 EX in two levels: *Zones* and *Set of Zones*. Each *Set of Zones* contains several *Zones*. *Zones* can be grouped to a *Set of Zones* by assigning them to the same *Time Strand* value which is automatically done when you load your Abaqus odb-file. E.g. the *example.odb* has four increments that are assigned to the same *Time Strand* and displayed in chronological consecutive order according to their assigned *Solution Time* and thus the four increments are grouped in one *Set of Zones* with four *Zones*. Note that the value of the *Time Strand* is not related to the modelling time which is stored in the variable *Solution Time*. In this sense the *Time Strand* is an identifier that controls which *Zone* (e.g. all increments of the model) are grouped into a *Set of Zones*. When e.g. a cross section is generated through the 3D model volume all variables are interpolated onto the cross section and stored in a new *Set of Zones* with a new *Time Strand* number. The new *Set of Zones* given in the example consists of four *Zones*.

Fig. 2.2-3 and Fig. 2.2-4 show how cross sections over time are extracted. For this procedure enable the *Slices* option from the side bar (turn off *Contour* and *Mesh* in the side bar. Then choose from the menu bar the option *Data/Extract/Extract Slices Over Time* (Fig. 2.2-3). With the *Zone Style…* dialog from the side bar the first *Set of Zones* (*Zones* 1-4) can be turned off (Fig. 2.2-3). To actually see the four newly created *Zone* with a new *Time Strand* number the user can open *Data/Edit Time Strands…* from the menu bar and change the time strands of every newly created *Zone* therein. The new *Set of Zones* contains all *Zones* of the model. Again, each chronological and geometrical entity in each step of the Abaqus analysis is one *Zone*.

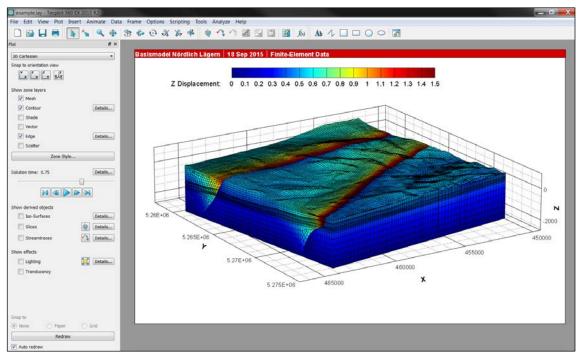


Fig. 2.2-1: Graphical user interface of Tecplot 360 EX.

The menu bar on the top offers the whole spectrum of functions within Tecplot 360 EX. The side bar on the left controls the plots generated.

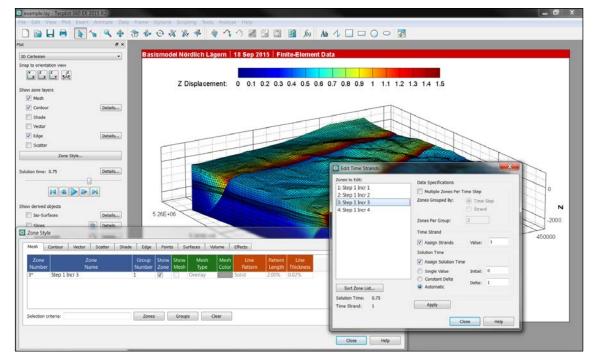


Fig. 2.2-2: Relation between Zone, Set of Zones, Time Strand and Solution Time.

Each time increment of the Abaqus analysis is in Tecplot one *Zone*. Several *Zones* can be grouped into one a *Set of Zones* by assigning to them the same *Time Strand* value. In the example, all four increments have the value *Time Strand*=1 which means that they are displayed consecutively according to their *Solution Time*. The figure displays the increment 3 of the Abaqus step 1 with the *Solution Time* 0.75.

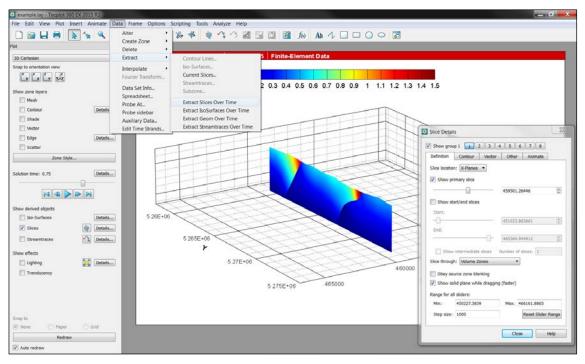


Fig. 2.2-3: Creation of a cross section through the model.

Use the *Slices* option from the side bar (turn off Contour and Mesh in the side bar) with options as indicated in the *Slice Details* dialog box on the right.

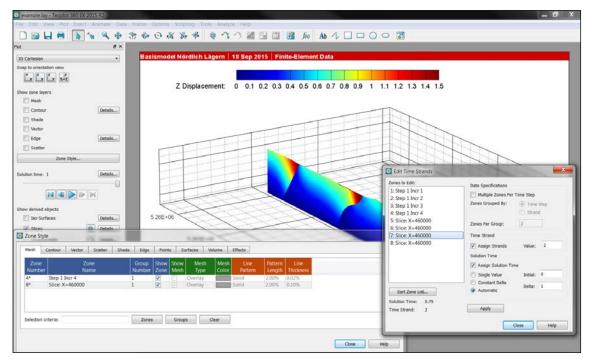


Fig. 2.2-4: Creation of a new Set of Zones and editing its Time Strand value.

Open the Zone Style... in the side bar and turn off the first *Set of Zones* (*Zones* 1-4). Then go to the menu bar and choose *Data-Edit Time Strands*... and you will see that you created four new *Zones* grouped into a new *Set of Zones* with a new (here 2) *Time Strand* value.

2.3 The Add-on *GeoStress*

The add-on *GeoStress* detects the main geometry data of the model (total number of nodes and elements) from the first *Zone*. You can also load a second model, i.e. a second model data set into Tecplot 360 EX, but the add-on *GeoStress* would not recognize this second new set.

GeoStress needs at minimum the following variables from the output file of the finite element solver: The three geometry variables for the location of the element nodes (X, Y, Z), the six components of the stress tensor (*SXX, SYY, SZZ, SXY, SYZ, SZX*) and the three components of the displacement vector at the nodes (*X Displacement, Y Displacement, Z Displacement*). Note that the components of the stress tensor in the commercial finite element packages are not provided at the nodes but at the integration points of the elements. Tecplot 360 EX has to interpolate these using the element description of the individual element types of the software packages. Thus, Tecplot 360 EX (release 2015 R2) usually cannot load the result files from the latest version of the commercial software packages. E.g. for Abaqus the highest version of the odb-file that can be loaded is v6.11.

The add-on *GeoStress* either adds further variables to the existing first *Set of Zones* or it adds a new *Set of Zones* to the model data set and interpolates all variables to the new *Set of Zones*. The recommended general workflow using *GeoStress* is the following:

- 1. Import the Abaqus odb-file (or the output file from your software or use the general data loader in the case your software package output file is not supported).
- 2. Generate with *GeoStress* all new variables in the first *Set of Zones*. Note that new or updated variables using *GeoStress* are not updated in *Set of Zones* (e.g. cross sections or external surfaces) that were generated before that update/new generation.
- 3. Generate new *Set of Zones* (e.g. cross sections or external surfaces) either with *GeoStress* or using the functionality of Tecplot 360 EX.

2.4 Saving Tecplot 360 EX format and output formats

2.4.1 Tecplot file formats *.*lay* and *.*plt*

To save the current view settings of all frames the menu bar offers to save the layout with *Save Layout* or *Save Layout As...*. The **.lay*-file saves the current view settings, but the time-consuming loading procedure of the **.odb*-file has to be performed again. The **.lay*-file saves only the plot view settings of Tecplot 360 EX, but not the re-structuring of the data from the **.odb*-file.

To reduce the loading time of the model result file the loaded data can be saved in the binary **.plt*-file format of Tecplot 360 EX. This is done with the menu bar *File/Write Data File...* and choosing there the data type section the *Tecplot Binary Data Writer (Current) (*.plt)* option. In the dialog box displayed in Fig. 2.4-1 the user can control which Abaqus steps, variables and other information from the binary **.odb*-file will stored in the **.plt*-file format. The **.lay*-file is then linked to the **.plt*-file.

Write Data File Options	X		
Details to Save			
✓ Text			
Geometries			
Custom Labels			
✓ Field Data			
Data Sharing Linkage (If Possible)			
▼ Face Neighbor Information Generated	by Tecplot		
ASCII Options			
	at 🔿 Point		
	Block		
Zone(s):	Variable(s):		
1: Step 1 Incr 1	1: X		
2: Step 1 Incr 2	2: Y		
3: Step 1 Incr 3	3: Z		
4: Step 1 Incr 4	4: AC_YIELD 👻		
· · · · · · · · · · · · · · · · · · ·			
Associate Layout with Newly Saved Data File OK Cancel Help			

Fig. 2.4-1: Dialog box for saving the results in the Tecplot *.*plt*-file format.

The user can select which *Zone* (Abaqus time step) is stored. Note that it is recommended to link the current *.lay-file with the *.*plt*-file with the tick box on the bottom.

2.4.2 Figure formats

Saving the active frame as a figure the option *File/Export*... from the menu bar is used. Here the user can choose between three raster image formats (png, tiff, jpeg, eps) and two vector image formats (wmf, eps). For the *.eps-format one can either store the file as an image with the wanted resolution in dots per inch (dpi) or as a vector format (Fig. 2.4-2). The two vector formats (wmf and eps-vector) can be quite large e.g. for 3D views of the model results including the mesh. Each line and each element face displayed on the 3D view is one vector.

🙆 Export	×	🙆 Export	×
Export format: PNG Color 		Export format: EPS	Color
Region Current Frame		Render type:	Image ○ Vector
		<u>R</u> egion:	Current Frame
Use width of image on screen		Re <u>s</u> olution (dpi):	150
Enter width: 3000		Extra precision:	0
Enter width.		Force extra sorting for all 3	D frames
Antialiasing		EPS preview image settings	
Supersample factor (2-16): 3		<u>T</u> ype: TIFF ▼ Wie	dt <u>h</u> : 128
		<u>D</u> epth: On/Off ▼ Hei	ght: 128
Convert to 256 colors			
OK Cancel Help		ОК	Cancel Help

Fig. 2.4-2: Dialog box for saving model results as a figure.

Note that the default setting of the figure resolution is the width of the screen. To enhance the quality, enter the width (here 3000 pixel). Note that you can choose for the postscript output*.*eps* both, a raster image or a vector format. The vector format can be quite extensive e.g. when you save a 3D view including the mesh information.

2.4.3 Movie formats

The model results can also be saved as movies in different formats (Fig. 2.4-3). There are two different ways to generate a movie. Either the active frame is animated over the *Solution Time* (*Animate/Time...* in the menu bar) or different views (e.g. rotate the 3D plot view of the model result) within the active frame are saved and Tecplot 360 EX interpolates between these views (*Animate/Key Frame Animation...* in the menu bar).

The two consecutive appearing dialog boxes for the first approach are displayed in Fig. 2.4-3 on the left and the centre dialog boxes. When *Destination/To file* is selected on the left dialog box the dialog box in the centre of Fig. 2.4-3 appears where the movie output format and the individual setting of the format can be controlled. Note that each time step is a *Zone* within Tecplot 360 EX. The model time is stored in the variable *Solution Time* within Tecplot 360 EX. Its content is given by the time defined in the Abaqus model which is in general given in seconds. In elastic calculation, it is not a time, but an arbitrarily number given to each increment.

The other way to generate a movie is to store consecutively several different views of the activate frame within the dialog box on right of Fig. 2.3-3. Tecplot 360 EX interpolates between the different frames and generates a movie that is either saved in a file or displayed on the screen.

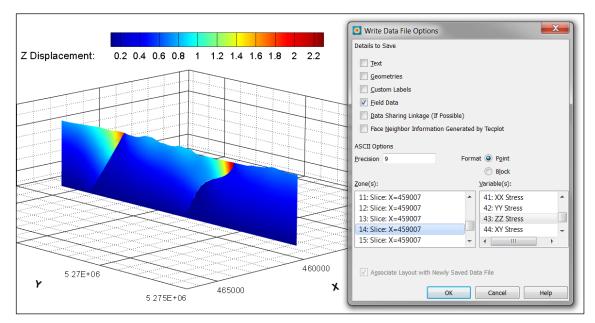
		🔯 Key Frame Animation
	Export	Eile Options
Time Animation Details Start time: 0.25 End time: 2 Time step skip: 1 Destination: To file	Export format: AVI Color AVI Region Curren MPEC-4 Raster Metafile Use width of image on screen Enter width: 1290 Antialiasing Supersample factor (2-16): 3	View 1 Append View 2 Insert View 3 View 4 Update View 5 Apply View 7 View 8 Delete Glear
Animate to File	Use multiple color tables	View Name: View 1
	Animation speed (frames/sec): 30	Frame Count: 30
		Destination: To File
Close Help	OK Cancel Help	Animate All Selected Close Help

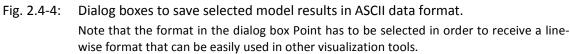
Fig. 2.4-3: Dialog boxes for saving model results as a movie.

Left/Centre: When *Destination To File* is selected the dialog box in the centre appears where format and other movie settings are determined. Right: The alternative way to generate a movie is the interpolation between different views in the current frame.

2.4.4 ASCII data output format

Independent from the current active frame or *Zone* the model results can be exported into an ASCII file format using the menu bar *File/Write Data File...*. Choose the data type *Tecplot ASCII Data Writer (current) (*.dat)* and provide an output data file name. With the resulting dialog box (Fig. 2.4-4) the user can choose from which *Zone* (e.g. a certain slice at a certain time step of the model; see Fig. 2.3-4) which variable is written to the ASCII file. To create a line-wise output of the data choose the *Format Point* toggle.





2.5 Installation of the Tecplot 360 EX add-on *GeoStress*

The add-on *GeoStress* is a shared library compiled for a 64-bit Windows platform (*GeoStress_win64.dll*) and a Linux platform (*GeoStress_lin64.so*) for the Tecplot 360 EX 2015 release R2. In order to install the add-on the appropriate library file has to be copied into the execution directory of Tecplot 360 (../bin). Furthermore, you have to edit the file *tecplot.add* that is located in the Tecplot 360 EX installation directory. The following lines must be added at the end of the file:

\$!LoadAddon "GeoStress_win64
for Windows and
\$!LoadAddon "GeoStress_lin64"

(without prefix "lib") for Linux. When you start Tecplot 360 EX you will find the new add-on *GeoStress* is available under the menu bar *Extras*. There are other useful add-ons provided in the Internet platform Tecplot Talk (*www.tecplottalk.com*). The installation is like the one described above. However, most of these add-ons are not yet compiled for the version Tecplot 360 EX 2015 R2 that was released in July 2015.

2.6 Loading of the Abaqus odb- and inp-files

Tecplot can load three different Abaqus file types: The *.*fil* and the *.*odb* output file format as well as the *.*inp* input file format from Abaqus, e.g. in order to import into the analysis further geometries. Tecplot 360 EX can also load the output files from other commercial finite element software packages such as Nastran or Ansys. In principal, the add-on *GeoStress* should work with all kind of finite element output files, but it has not been tested. The basic information

that is expected from *GeoStress* are the three coordinates of the nodes (*X*, *Y*, *Z*), the six components of the stress tensor (*SXX*, *SYY*, *SZZ*, *SXY*, *SXZ*, *SYZ*) and the three components of the displacement vector (*X displacement*, *Y displacement*, *Z displacement*). Note that *GeoStress* cannot be used for 2D model results since most calculations are based on the 3D stress tensor.

Organisieren • Neuer	Ordner			• 🗌 🔞	
E Desktop	Name	Änderung	gsdatum	Тур	
S Zuletzt besucht	example_1.odb	20/09/20	13 13:50	ODB-Datei	1
🞇 Bibliotheken					L
Dokumente					
I Musik					
Judeos					
K Computer					
tindows7_OS (C:					
I DATEN (E:)					
🚷 Lenovo_Recovery 👻	•				F.
Dateina	me: example_1.odb	▼ [A]	BAQUS Outpu	it Database (🔻	
		Help	Open 🔽	Abbrechen	
			Open		
			Open usin	g Advanced Opt	ions

Fig. 2.6-1: Loading Abaqus odb-files.

Default loading is without advanced loading options. It is recommended not use the advanced loading options to avoid problems that may arise during the analysis using *GeoStress* (see text for further explanation).

The dialog box for loading odb-files Tecplot 360 EX offers to use advanced options (Fig. 2.3-1). However, the option *Subdivide Zone by Components* or *by Elements Type* can lead to limits when the add-on *GeoStress* is used. This option will put components and/or all elements with the same material property assignments for each time step into a separate *Zone*. This would be comfortable since e.g. individual lithological layers can be displayed individually over time, but *GeoStress* expects that all elements and nodes that exist in the model are defined in the first *Set of Zones* of the model data set (see also section 3.1 for further details).

🔯 Load ABAQUS Output Database (FEA) File
File plot\Abschlussbericht\Example_Modell_NL\BM_new.odb
Subdivide Zones
Select Zones and Varia by Element Type
✓ Auto Assign Strand IDs for Zones
Add Zones to Existing Strands
OK Cancel Help

Fig. 2.6-2: Advanced loading options for Abaqus odb-files.

When *Subdivide Zone* is selected the elements with the same material property assignments (each element set) are put for each time step into a separate *Set of Zones* leading to limits with the add-on *GeoStress* as it expects that the whole model is located in the first *Set of Zones*.

3 User interface of the add-on *GeoStress*

The user interface of the add-on *GeoStress* is opened in the menu bar under *Extras* and appears as a dialog box with seven different tab cards (Fig. 3.1-1). The dialog box of the add-on *GeoStress* starts with the page *General* which is in particular important during the first application of *GeoStress* on a newly loaded model output file. The other six tab cards of *GeoStress* group the functions regarding values derived from the stress tensor, Fracture Potential (*FP*), Coulomb Failure Stress (*CFS*), Slip and Dilation Tendency (*ST* and *DT*), Internal Surfaces and External Surfaces as well as Polylines. Details and handling of these tab cards are described in the following sections 3.1-3.7 of this chapter. In the first five tab cards, new variables are calculated and provided for the first *Set of Zones*. Only the options in page six and seven generate both new variables and new *Zone* (*Set of Zones*) on which all variables are interpolated.

3.1 General settings

The first page of the add-on *GeoStress* is the General Setting. The page has five sections (Fig. 3.1-1). In particular, the setting of the stress and plot scaling values is important as this has an impact on the variable calculation in the other tab cards.

eneral	Stress	FP	CFS	ST/DT	Int. surfaces	Ext. surfaces/polylines
Orienta	tion in nort	th, east,	vertical d	own	G	eo-coordinates
		Trend		Plunge		North (N)
X ax	es	90.000	1	0.000		
Y ax	05	0.000		0.000		V East (E)
						Vertical down (V)
Z ax	es	0.000		-90.000		Calculate
		A	djust			Calculate
Stroce er	caling facto				Plot scaling fa	stor
50,655,50	Jaimy Tacto		-1.000e	•06	Flot Scaling Ta	ctor 1.000e+00
True ve	ertical dept	n (TVD)				
	Load t	opograp	hy			Calculate

Fig. 3.1-1: Page General.

The five sections of this page control the orientation of the coordinate system, the stress and plot scaling factor and the calculation of the variable True Vertical Depth (TVD).

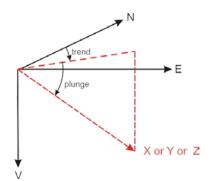
3.1.1 Orientation in North, East and Vertical down

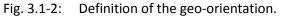
Most of the new variables that are calculated with *GeoStress* require a reference to a geoorientated coordinate system {N (north), E (east), V (vertical down)}. The transformation from the modelling system {X, Y, Z} to {N, E, V} is described by the trend and plunge of the X-axis, Y-axis and Z-axis respectively in the geo-system. The trend is given as a 360° angle measured clockwise from *N*. The plunge can be between -90° and 90°. A positive plunge indicates that an axis points downwards (Fig. 3.1-2).

The default orientation is X=E (90; 0), i.e. the trend of the X-axis is 90° from the North direction, Y=N (0; 0), i.e. the trend of the Y-axis is the North direction and Z=-V (0; -90), i.e. z-values downwards are positive. The add-on offers to re-orient the coordinate system, i.e. to re-orient the six components of the 3D stress tensor and to make sure that the positive X-, Y-, Z-axes are oriented in North (N), East (E) and Vertical down (V) direction. An input is only required for the X- and Y-axes. The Z-axes is then determined automatically by *GeoStress* because it is overdetermined by four given variables. Press the Adjust button to adjust the system. This procedure does not change the X-axes, but finds a Y-axes in the (former) XY plane close to the input of Y but perpendicular to the X-axes. Iterate a few times if one of the two variables (Y-trend or Y-plunge) should be fixed exactly.

3.1.2 Geo-coordinates

Enable any of the check boxes and press the *Calculate* button if the node coordinates are required in the {N, E, V} system. Please note that the node coordinates describe (by default) the deformed geometry of the model (see chapter "Post-processing Finite Element Data" of the Tecplot user manual) and therefore the derived geo-coordinates too.





The trend is defined as the angle between the north direction and the coordinate axis, the plunge is the angle between horizontal projection of an axis and its dip.

3.1.3 Stress scaling factor

In contrast to the geosciences community the commercial finite element software packages define compression negative. The default settings in the in the stress scaling factor dialog box is -1.000e-06 which changes the stress state to compression positive and it converts the units of the stress variables from Pascal (Pa) in the Abaqus *.odb-file to Mega Pascal (MPa). Note that units for the original six stress tensor components from the *.odb-file (XX Stress, XY Stress, etc.) are not changed, but only the values that are derived with *GeoStress*. Furthermore, the units for the cohesion values expected in the tab cards *FP* (Fracture Potential), *CFS* (Coulomb Failure Stress) and Slip/Dilation Tendency (*ST/DT*) are expected in the same unit as defined in the general setting of the add-on.

3.1.4 Plot scaling factor

The output of a model also includes the deformation of the geometry due to the individual displacement of the nodes. In order to exaggerated small deformations, the user can set the plot scaling factor. This is done when the *.odb file is loaded for the first time. In the appearing dialog box (Fig. 3.1-3) the tick box *Deform Plots by Factor* changes the plot scaling factor; the default value of Tecplot 360 EX as well as for the add-on *GeoStress* is 1. This value can also be changed using the menu bar Tools/FEA Post-Processing, but once the output file is saved as a *.plt file the plot deformation factor cannot be changed anymore. The user has to make sure that the finally stored plot scaling factor that is used from Tecplot 360 EX is consistent with the post scaling factor to be given in the *GeoStress* add-on in the first page with the general setting. If this consistency is not given the calculation of the new variable *True Vertical Depth* (*TVD*) and the kinematic estimates on the faults would be wrong. This is necessary since *TVD* is calculated for each step and therefore a variable that changes over time due to the deformation of the geometry.

FEA Post-Processing	—X
Deform Plots by Factor: Animate Plot	1
Animate Deformation	On Screen 🔻
Number of Steps:	10
Number of Cycles:	1
	Animate
Derive Variables Derive:	
Von Mises Stress/Stra Principal Stresses/Stra Vector Magnitude	
From:	
	Add to Data Set
	Close Help

Fig. 3.1-3: Plot scaling factor setting in Tecplot 306 EX.

The Plot scaling factor chosen within Tecplot 360 EX must be consistent with the setting in the general page. Otherwise the calculation of relative displacement and the *True Vertical Depth (TVD)* is not correct.

3.1.5 True vertical depth (TVD)

The variable *TVD* is the true depth below the surface of the model geometry. It has the same units as the model (usually meters). As stated in the previous section *TVD* also considers the deformation and thus the plot scaling factor used by Tecplot 360 EX and the add-on *GeoStress* must be consistent. The value of *TVD* is always calculated at the end of each time step; i.e. the *TVD* value of the first time-step (first *Zone*) is the one at the end of the first Abaqus increment and thus contains already deformations from the model.

To perform the calculation *GeoStress* needs an input as a **.txt*-file where the original numbering of all nodes that are located at the surface of the model are provided. The format of this input file is given in the following example.

Example:

```
** _ABAQUS_Input_Deck_Generated_by_HyperMesh_Version_12.0.0.85
** _Generated_using_HyperMesh-Abaqus_Template_Version_12.0
**
*NODE
____100239,__681815.55544868,__268163.90825397,__407.77080517579
____100243,__684885.07511532,__268705.14852239,__363.795577031
____100247,__684577.50712194,__268650.91587525,__450.55165463753.
**
```

Lines that start with ** are comments and can be inserted before or after the block of data. The key word **NODE* is compulsory and indicates the start of the read in of the data. Each data line starts with the original node number optional followed by the node coordinates. However, *GeoStress* reads in only the numbering of the nodes and not their coordinates since Tecplot 360 EX knows the link between the nodes (variable *Node UserID*) and their coordinates (variables *X*, *Y*, *Z*). Field separator can be a blank, tab stops or comma. For safety reasons, it is recommended to finalize the read in of data with a comment line.

3.1.6 Application examples

In order to calculate the variable *TVD* the file *topography_nodes_only.txt* located in the folder Geometry has to be loaded using the button Load topography on the general page of input (Fig. 3.1-1). The calculation is performed for each increment of the model considering also the changes of the *TVD* with time. For high-resolution models with many nodes at the model surface (i.e. the topography nodes) and lots of increments the *TVD* calculation can be quite time-consuming.

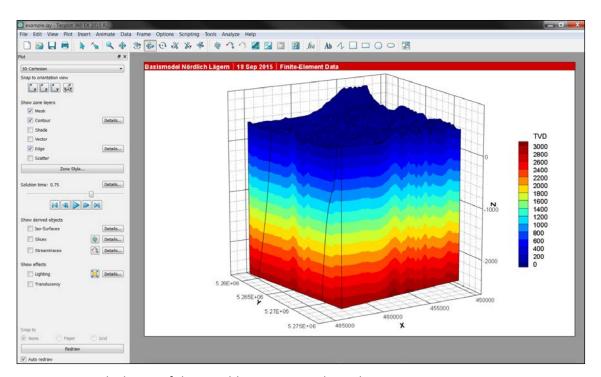


Fig. 3.1-4: Calculation of the variable True Vertical Depth *TVD*.The plot shows the *TVD* with five times exaggeration in the vertical in increment 0.75.Note that the *TVD* is reflecting the topography.

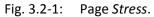
3.2 Stress value calculations

3.2.1 Theory and background information

The page *Stress* (Fig. 3.2-1) offers the calculation of a wide range of stress variables that are derived from the six components of the stress tensor. An overview as well as details and explanation of the different variables that are calculated on this page are summarized in Table 3.2-1. The page is divided in two parts. The upper area provides all information on the principal stresses S_1 , S_2 and S_3 and variables derived from these principal stresses. Furthermore, it offers to calculate from the stress tensor components the *Regime Stress Ratio* (*RSR*) that is a continuous scale for the visualization of the stress regime (Simpson, 1997). The lower part offers a range of stress variables and stress ratios for the horizontal and vertical stress components.

The selected variables are calculated for the whole model volume and each time step. However, when e.g. a cross section is extracted over time (example is described in Fig. 2.3-3 and Fig. 2.3-4 in section 2.3) only the existing variables are interpolated onto these geometries after they are generated with *GeoStress* and stored in the Tecplot 360 EX plt-file format. Note that new variables that are calculated with the equations option are not stored in the plt-file, but only on the lay-file. Thus, it is recommended to calculate first all new variables that are needed for the whole model volume and to store these explicitly in the *.plt file and then create new *Zone*.

🧕 GeoStress						X
General	Stress	FP	CFS	ST/DT	Int. surfaces	Ext. surfaces/polylines
Princip	al stress					
V Ma	agnitude/orie	entation	(S1, S1t	r, S1pl, S2,	S2tr, S2pl, S3, S3	tr, S3pl)
✓ Me	ean stress ((S1+S2-	+S3)/3)		Differential	stress (S1-S3)
▼ St	ress ratio ((52-S3)/	(S1-S3))		🔽 Regime stre	ess ratio (RSR)
Horizor	ntal and vert	ical stre	ess			
V Ma	agnitude/azi	muth (S	SHmax, SI	Hazi, Shmin	, SV)	
SH	lmax orienta	tion ve	ctor (SHx,	, SHy, SHz)		
V Dif	ferential str	ess (SH	Imax-Shr	nin)		
🗸 St	ress ratios (SHmax/	/Shmin, S	Hmax/SV, S	hmin/SV, 0.5(SHn	nax+Shmin)/SV)
				Calcu	late	
						Close



The page is divided in two parts. The upper area provides all variables related to the three principal stresses and the *Regime Stress Ratio* (*RSR*). The lower part provides a range of stress variables related to the horizontal and the vertical stress.

Tab. 3.2-1:Overview of stress variable calculations with *GeoStress* page *Stress*.The first column shows the variable as it appears in the variable list in Tecplot 360 EX. The
second column gives an explanation or background information.

Variable	Definition/Comment
S1, S2, S3	Magnitudes of the three principal stresses (the stress unit depends on the choice in the general settings of the first page of <i>GeoStress</i>).
S1tr, S1pl S2tr, S2pl S3tr, S3pl	Orientation in terms of trend (tr) and plunge (pl) in degrees of the three principal stresses in the System $\{N, E, V\}$ as defined in the general settings of the first page of GeoStress (see Fig. 3.12).
(\$1+\$2+\$3)/3	Mean stress. Note that $(S1+S2+S3)/3 = (Sxx+Syy+Szz)/3$ since this is one of the three invariants of the stress tensor.
S1-S3	Differential stress as the difference between the largest (S1) and the smallest principal stress (S3).
(S2-S3)/(S1-S3)	Stress ratio. When <i>S1-S3</i> =0 the stress state is lithostatic (sometimes also called isotropic) and (<i>S2-S3)/(S1-S3</i>)=1.
RSR	The Regime Stress Ratio (<i>RSR</i>) is calculated after the formula given in Simpson (1997) and provides a continuous scale for the stress regime. The <i>RSR</i> is basically a combination of the Andersonian stress regime index n (Anderson, 1905; 1951) and the stress ratio <i>SR</i>
	$RSR = (n + 0.5) + (-1)^{n}(SR - 0.5) n = \begin{cases} n = 1 \text{ if } Shmin \le SV \le SHmax \\ n = 2 \text{ if } SV \le Shmin \le SHmax \\ n = 0 \text{ otherwise} \end{cases}$
	where $SR=(S2-S3)/(S1-S3)$. The RSR variable ranges from radial extension (RSR=0) over normal faulting (RSR=0.5), strike-slip (RSR=1.5) and thrust faulting (RSR=2.5) to constriction (RSR=3), including the transitional stress regimes of transtension (RSR=1) and transpression (RSR=2).
SHmax, SHazi Shmin, SV	Magnitude of the vertical stress SV and maximum and minimum horizontal stress <i>SHmax</i> and <i>Shmin</i> , respectively. <i>SHazi</i> is the orientation of <i>SHmax</i> in degrees from North and lies between 0-180° due to the bipolar character of stress orientations.
SHx, SHy, SHz	The three components of the vector of the <i>SHmax</i> orientation <i>SHazi</i> with respect to the Cartesian coordinate system { <i>X</i> , <i>Y</i> , <i>Z</i> }. Note that <i>SHz</i> should be zero and that only the two components <i>SHx</i> and <i>SHy</i> are needed to plot with Tecplot 360 EX the SHmax orientation as a vector. Note that these components are given in the old coordinate system to allow Tecplot 360 EX to plot the vector.
SHmax-Shmin	Horizontal differential stress.
SHmax/Shmin SHmax/SV Shmin/SV 0.5(SHmax+Shmin)/SV	Various stress ratios. If <i>Shmin</i> =0 the ratio <i>SHmax/Shmin</i> =-999, if <i>SV</i> =0 the other three ratios are set to -999.

3.2.2 Application examples

The following two figures show the results of the horizontal stress difference S_{Hmax} - S_{hmin} (Fig. 3.2-1) and the Regime Stress Ratio RSR (Fig. 3.2-2), respectively.

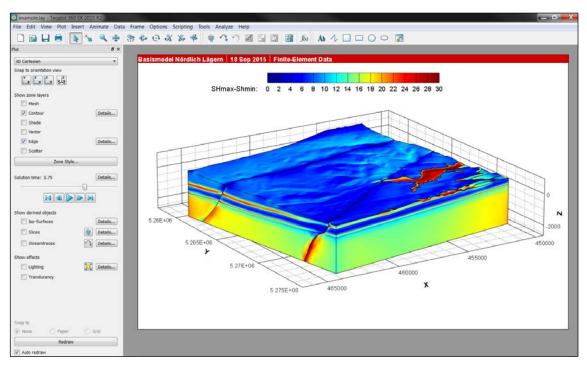


Fig. 3.2-2: Contour plot of the horizontal stress difference $S_{Hmax} - S_{hmin}$.

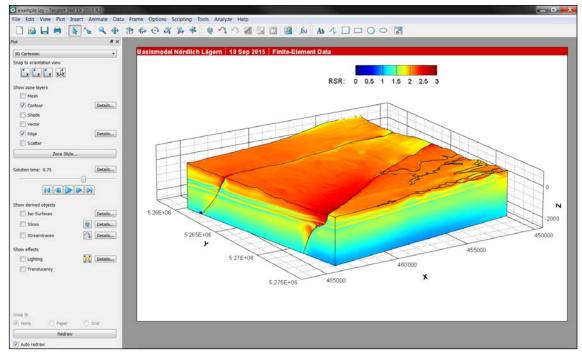


Fig. 3.2-3: Contour plot of the Regime Stress Ratio (RSR).

3.3 Fracture potential

3.3.1 Theory and background information

The Fracture Potential (*FP*) is described by Connolly and Cosgrove (1999) and expresses the ratio of the actual maximum shear stress (S1-S3)/2 in the model and the critical value of acceptable shear stress from an empirical failure criterion. It thus quantifies how far the actual stress state is away from failure, i.e. the generation of fractures in a rock mass subjected to stress. This definition holds only for shear failure which is considered here since the crust is generally in a compressional state of stress.

The critical differential stress used in *GeoStress* is based on the Navier-Coulomb criterion and hence dependent on the internal coefficient of friction μ_i of the rock and the cohesion *C*. These two parameters have to be specified in the *GeoStress* settings in order to calculate the *FP* for a given stress state. The units of the values have to be in agreement with the units given in the *GeoStress* page *General setting* (Fig. 3.1-1). In particular *FP* is a relative measure for the Coulomb shear failure criterion in a volume with a given stress state:

$$FP = \frac{actual\ maximum\ shear\ stress}{acceptable\ shear\ stress}$$

It is calculated on the optimal oriented plane and it is defined as the ratio with the following definitions of the actual and the acceptable maximum shear stress:

actual maximum shear stress = $\frac{1}{2}(S1 - S3)$

acceptable maximum shear stress = $\left(\frac{C}{\tan\phi} + \frac{1}{2}(S1 + S3)\right)\sin\phi = C\cos\phi + \frac{1}{2}(S1 + S3)\sin\phi$

C is the cohesion, ϕ the friction angle ($tan\phi = \mu_i$) and *S1* and *S3* are the largest and smallest principal stress, respectively.

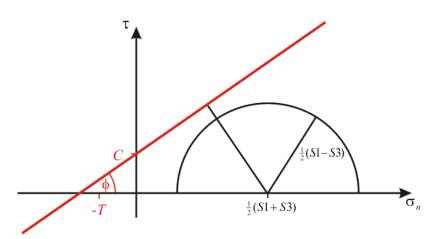


Fig. 3.3-1: Coulomb failure in a 2D plane.
 C is the cohesion, T the tensional strength, φ the friction angle, τ is the shear stress and σ_n the normal stress of the optimal oriented plane.

Under specific circumstances the calculation of the *FP* can result incorrect values. E.g. when the differential stress *S1-S3* is very small and *S3* negative the fault would not fail in shear (Mode II), but in opening/dilation (Mode I) due to the tensional stresses (and the tensional strength). To account for these special cases the following rule is applied:

$$FP = \begin{cases} -999 & \text{if } \frac{1}{2}(S1+S3) \le -T & \text{(tensile fracture)} \\ -9999 & \text{if } -T < \frac{1}{2}(S1+S3) \le \frac{C}{\tan\phi} & \text{(undefined)} \\ \frac{1}{2}(S1-S3)/(C\cos\phi + \frac{1}{2}(S1+S3)\sin\phi) & \text{otherwise} \end{cases}$$

where *T* is the tensional strength of the rock. This value can be set in the *GeoStress* page for the *FP* calculations (Fig. 3.2-2). Again, the user of the add-on is responsible that the used units are consistent.

The *FP* values can be calculated either with homogeneous rock properties for the whole model (upper section of the *FP* page) or with individual values for each rock material of the model (lower section of the *FP* page). The individual material values (C, ϕ and T) for an element node are calculated as the mean value of all elements that share this node. The material definition of the elements is given in the variable *Material ID* and is provided by Abaqus and thus also given as a variable in Tecplot 360 EX. The assignment of the variable *Material ID* to the material properties is done with a text file (*.txt). This file is uploaded with the button *Load Parameter* in the graphical user interface.

Example:

```
****
     ** Values for plasticity (friction angle (2nd column), cohesion
** (3rd column in MPa), tensile strength (4th column in MPa) for
** model NL. First column is the internal numbering of the material
** ID from Tecplot 360 EX. However, the numbering is not related
** to the order of the material definitions in the Abaqus input file.
*FD
6 38 10 5
               Molasse and Quaternary Cover
8 50 20 5
               Upper Malm
1 40 8 5
               Wildegg Formation
7 30 8 5
               Upper Dogger
10 23 4 5
               Opalinus Clay
3 30 8 5
               Lias and Upper Middle Keuper
2 34 28 5
               Gipskeuper
9 45 23 5
               Upper Muschelkalk
5 40 20 5
              Middle and Lower Muschelkalk
4 40 30 5
               Pre-Mesozoic Basement
                                *****
```

The key word **FP* is compulsory right before the data lines. Comments are indicated with **; the end of data to read in has to be denoted with a comment **. In column 1 the *Material ID* is defined, in column 2 the *friction angle* ϕ , in column 3 the *cohesion C* and in column 4 the *tensional strength T*. Each line can be completed by an optional comment. The field separator can be a blank, comma or tab stop.

GeoStress						
General	Stress FF	CFS	ST/DT	Int. surfaces	Ext. surfaces/polylines	
Fracture	potential (FP)	for uniform f	racture par	ameters		
	Friction angle	30.000				
	Cohesion	10.000			Calculate	
Ter	sile strength	5.000				
Fracture	potential (FP)		fracture pa	rameters	Calculate	

Fig. 3.3-2: Page *Fracture Potential*.

The FP can be calculated either with homogeneous rock properties (upper section) or individual values for each rock type in the model (lower section).

3.3.2 Application examples

Fig. 3.3-3 shows the calculation of the Fracture Potential with one cohesion and friction angle for the whole model volume. Fig. 3.3-4 displays the material ID number that is needed to create the file that connects the *Mat ID* with variable cohesion and friction angle for each individual geomechanical unit of the model. Then Fig. 3.3-5 shows the resulting *FP* values.

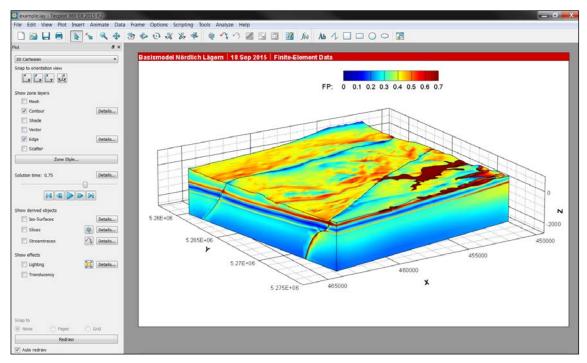


Fig. 3.3-3: Calculation of the Fracture Potential with homogeneous rock properties.

D Cartesian	Ø X	
D Cartesian	Pastow add Minute	ich Lägern 07 Nov 2015 Finite-Element Data
ap to orientation		
IY IZ IZ	Contour & Multi-Coloring Details	× #########
	55: Material ID - 1 2 3 4 5 6 7 8	Material ID: 1 2 3 4 5 6 7 8 9 1011
w zone layers	Levels and Color Bands Lines Labels Legend	
Mesh	Contour levels	
Contour	1:1 * 65 Set Levels	
Shade Vector	2:2	
Edge	3:3 Add Level 0	
Scatter	5:5 Ramove Selected	
Judenten	6:6	
_	7:7 8:8 Min: 1 Max: 10	O Zone Style
tion time: 0.	0.0	
		Mesh Contour Vector Scatter Shade Edge Points Surfaces Volum
	Color map options	
R	Color map options	Zone Zone Group Show Show Contour Floo
	> < < < < < < < < < < < < < < < < < <	Number Name Number Zone Contour Type By
v derived obje		Number Name Number Zone Contour Type By 3 st Step 1 Incr 3 1 2 2 2 Primary value fload - CT-Morester 1 Lines
w derived obj	Modern + 😹	Number Name Number Zone Contour Type By 3 ¹ Step 1 Incr 3 1 V V Primary value fload. (1) Meredia 1 Lines Flood
v derived obje Iso-Surface Slices	Image: Color map distribution method Color cutoff	Number Name Number Zone Contour Type By 3* Step 1 Incr 3 1 D1 D2 Primary value from the Ch. Mered the Flood Lines and floo
w derived obje Iso-Surface Slices	Image: Color mag distribution method Color cutoff @ Banded Continuous Cutor tabove: 7.75	Number Name Number Zone Contour Type By 3 ⁴ Step 1 Incr 3 1 D1 D2 Primary value figure 1CH. Mental till 4 III III D2 Primary value figure 1CH. Mental till Lines 4 III OP Primary value figure 1CH. Mental till Primary value figure 1CH. Mental till
v derived ob Iso-Surface Slices Streamtre	Image: Second	Number Name Number Zone Contour Type By 3* Step 1 Incr 3 1 D1 D2 Primary value from the Ch. Mered the Flood Lines and floo
v derived obji Iso-Surfaci Slices Streamtrei v effects Ughting	Image: Color range distribution method Color cutoff Image: Color cutoff Image: Color cutoff Image: Color cutoff Image: Cutoff color cu	Number Name Number Zone Contour Type By 3 ⁴ Step 1 Incr 3 1 D1 D2 Primary value figure 1CH. Mental till 4 III III D2 Primary value figure 1CH. Mental till Lines 4 III OP Primary value figure 1CH. Mental till Primary value figure 1CH. Mental till

Fig. 3.3-4: Visualization of the Material ID number.

To get the correct Fracture Potential values a file that links the *Mat ID* number, cohesion and friction angle for each unit must be provided. Use the Primary value flood to display for each unit the number correctly.

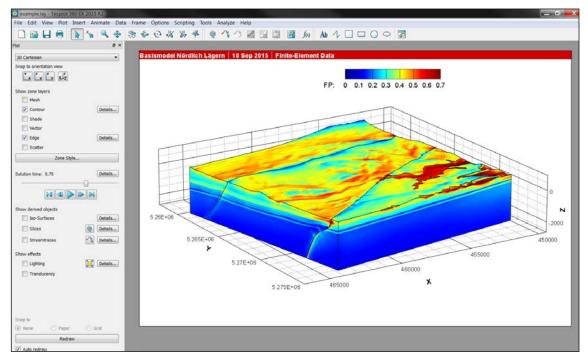


Fig. 3.3-5: Plot of the Fracture Potential with inhomogeneous rock properties. Note the difference to the results displayed in Fig. 3.3-3 where a homogeneous rock property values for the cohesion and the friction angle is used.

3.4 Coulomb failure stress

3.4.1 Theory and background information

The Coulomb failure stress (CFS) for a given fault or segment of a fault is the difference between the shear stress τ and the Coulomb stress $tan(\phi)\sigma_n - C$

$$CFS = \tau - \tan(\phi) \sigma_n - C$$

where τ is the shear stress on a plane that represents a fault or a segment of a fault, $tan(\phi)$ is the static friction coefficient μ expressed with the tangent of the friction angle ϕ , σ_n the normal stress and *C* the cohesion. The shear stress is defined on the fault given by its strike and dip in a priori selected rake direction; the latter is essential to assign the correct sign of the shear stress on the fault. The Coulomb failure stress is the resistance to this shear stress. Thus, negative values quantify how far the actual stress state is away from failure. Values close to zero would indicate that the fault is critically stressed and positive values would indicate that the fault would slip to release the excess of shear stress. Note that like slip tendency CFS provides only valid information about potential failure on one specific plane. Furthermore, in contrary to slip tendency CFS is also dependent on the rake vector. Hence its significance is limited to a specific focal mechanism on a specific plane.

However, the commonly used definition of CFS does not distinguish between compression and tension and thus, when the normal stresses become sufficiently negative the faults would not fail in shear (Mode II) but in dilation, i.e. opening (Mode I). Thus, *GeoStress* assigns CFS=-999 in the case when the normal stress σ_n is a tension (negative sign) and exceeds the given tensile strength $T(-\sigma_n \ge T)$.

GeoStress						
General Stres	ss FP CFS	ST/DT	Int. surfaces	Ext.	surfaces/polylines	
- Failure plane p	arameters					
Strike	25.000		Friction and	gle	30.000	
Dip	90.000		Cohesi	on	5.000	
Rake	0.000		Tensile streng	th	5.000	
User selected :	zones tive differential Could	omb failure st	tress (D_CFS_C)			
			1	c	top 1 Incr 2	•
			Second zor		tep 1 Incr 3 tep 1 Incr 4	
First zo	Step Lincr					
First zo	Step 1 Incr 3 Step 1 Incr 4				•	~
First zo			ate		<u> </u>	Ŧ

Fig. 3.4-1: Page Coulomb Failure Stress.

The page is divided into three sections. In the upper section the orientation of fault plane parameter is stated for which the Coulomb failure stress is calculated and the properties of the fault plane. In the second section the user can select to calculate the total *CFS* and the differential *CFS* (D_CFS_S) between all *Zones*. In the lower section the user select two *Zones*. Between these the cumulative differential *CFS* (D_CFS_C) is estimated.

Fault plane parameters

GeoStress defines strike, dip and rake following the conventions by Aki and Richards (1980). Fault strike is the direction of a line created by the intersection of a fault plane and a horizontal surface. It can range from 0° to 360° relative to North. Strike is always defined such that a fault dips to the right side of the trace when moving along the trace in the strike direction. Thus, the hanging-wall block of a fault is always to the right, and the footwall block to the left. This is important because the rake which defines the (potential) slip direction is defined as the movement of the hanging wall relative to the footwall block. The fault dip is the angle between the fault and a horizontal plane and ranges from 0° for a horizontal fault to 90° for a vertical fault. Rake is the direction a hanging wall block moves during rupture, as measured on the plane of the fault. It is measured relative to fault strike, ±180°. For an observer standing on a fault and looking in the strike direction, a rake of 0° means that the hanging wall (or the right side of a vertical fault) moves away from the observer in the strike direction (left lateral motion). A rake of ± 180° means the hanging wall moves toward the observer (right lateral motion). For any rake $> 0^{\circ}$ and $< 180^{\circ}$, the hanging wall moves up, indicating reverse motion on the fault; for any rake $< 0^{\circ}$ and $> -180^{\circ}$ the hanging wall moves down, indicating normal motion on the fault.

Calculation of different CFS values

The calculation of *CFS* values is divided into two sections *All Zones* and *User selected Zones*. The Coulomb failure stress *CFS* and the single difference in Coulomb failure stress (*D_CFS_S*) can be calculated for all *Zones* of the 3D model (Fig. 3.4-1). The *D_CFS_S* is the difference of *CFS* between successive *Zones* (model steps) and it is assigned to the latter *Zone*. Thus D_CFS_S is zero for the first *Zone* and has a value for all other *Zones*. *D_CFS_S* is flagged by -999 for a node if at least one of the single *CFS* values of the node is flagged by -999.

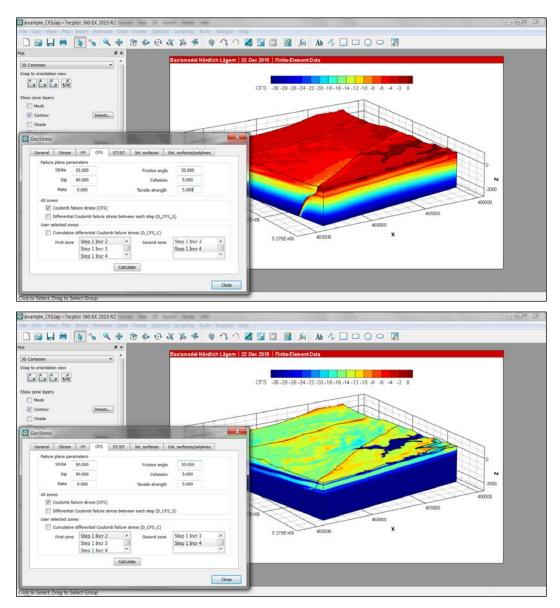
The lower section allows the user to define between which *Zones* (model steps/increments) the cumulative differential Coulomb failure stress (D_CFS_C) is calculated. The D_CFS_C variable is zero for the selected First *Zone* and then increasing from step to step until the Second *Zone* is reached. Positive differential *CFS* values (single and cumulative) indicate that the stress state has changed from one step to the next towards failure, i.e. the fault (with the given orientation, dip and rake) has been brought closer to failure. Vice versa negative differential *CFS* values indicate that the fault has been brought further away from failure.

3.4.2 Application examples

Figure 3.4-2 shows the Coulomb failure stress *CFS* in MPa as a contour plot for the model volume. The *CFS* values in the upper figure are calculated for vertical faults (dip=90°) with a strike of 25°N and a rake direction of 0°. This orientation is almost optimal oriented in the given stress field. In the lower figure the *CFS* values are calculated for vertical faults as well, but with a strike of 90°N. Here the resulting values are significantly lower since for E-W striking faults the S_{Hmax} orientation is almost perpendicular to the fault which increases the fault normal stress and decreases the shear stress on the fault in comparison to the first calculation in the upper figure. However, the interpretation of the resulting colour distribution has to be done with care. E.g. the higher *CFS* values near the fault that are implemented in the model do not indicate that the fault is closer or further away from failure. The calculation of the *CFS* values in this example has nothing to do with the strike and dip of the fault that is implemented in the model. Figure 3.4-3 shows the differential Coulomb failure stress *D_CFS_S* between successive steps. Since the displacement boundary conditions between two steps are similar the two figures look very

similar except local stress changes due to the fault reactivation. Figure 3.4-4 shows the cumulative differential Coulomb failure stress D_CFS_C between two user selected Zones. The D_CFS_C values are increasing from one step to the next. The values mostly positive and thus indicate that vertical sinistral strike-slip faults that strike 25°N are brought closer to failure.

Note that if you change the geometry of the fault plane (strike, dip, rake) or the fault properties (friction angle, cohesion, tensile strength) in the upper section and re-calculate any of the offered three *CFS* values (*CFS*, *D_CFS_S*, *D_CFS_C*) by pressing calculate button, the results in all frames are changing on the fly. This enables you to perform a fast and efficient analysis of your models results. Note that the fault parameter setting in this page does not affect the calculations of the other *GeoStress* tab cards (and vice versa).





The upper figure shows the absolute *CFS* value in MPa calculated for vertical faults (dip=90°) that strike 25°N. In the lower figure the *CFS* is calculated with the same values, but the strike has changed to 90°. In both cases the rake direction is 0°

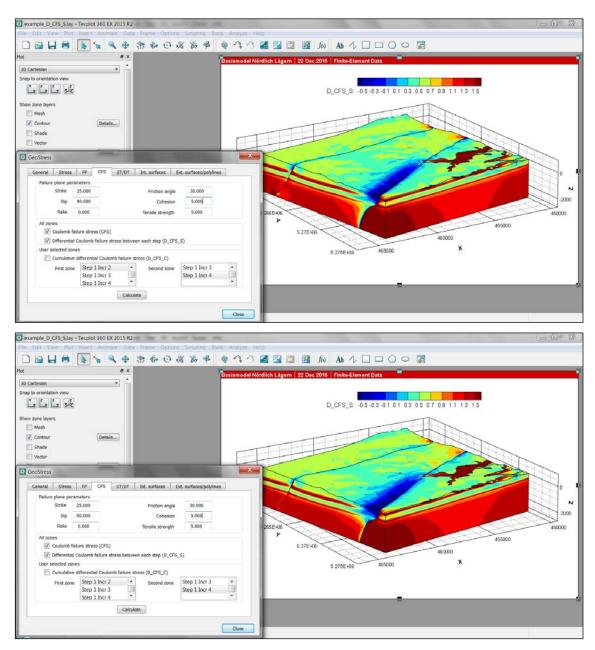


Fig. 3.4-3: Single differential Coulomb failure stress between all model steps.

The upper figure shows the D_CFS_S values in MPa for Step 1 lncr2 - Step1 lncr1. The lower figure shows D_CFS_S in MPa for Step 1 lncr4 - Step1 lncr3. The value of D_CFS_S that is presented in a *Zone* is always the difference to the previous *Zone* and it is written in the second *Zone*.

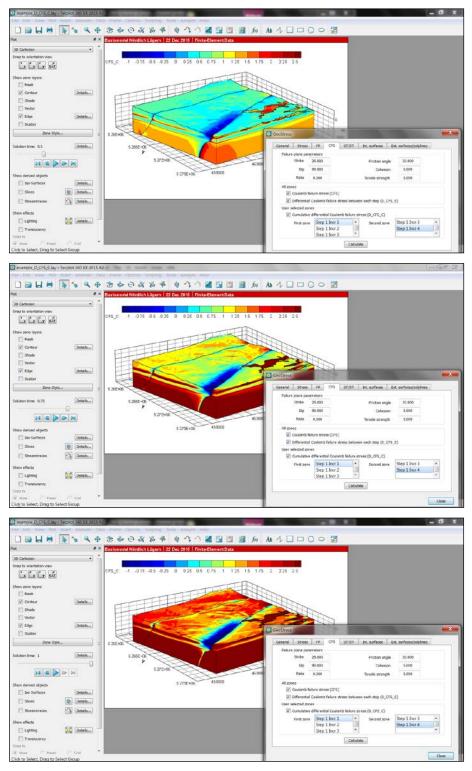


Fig. 3.4-4: Cumulative differential Coulomb failure stress between model steps.

The figures show the *D_CFS_C* in MPa for three steps. The upper figure shows *D_CFS_C* for Step1 Incr2 – Step 1 Incr1, the middle one for Step1 Incr3 - Step 1 Incr2 and the lower one for Step1 Incr4 - Step 1 Incr3. Thus, the value of *D_CFS_C* that is presented in a *Zone* is always the difference to the selected first *Zone*.

3.5 Slip and dilation tendency

3.5.1 Theory and background information

The slip tendency *ST* value is a measure for the relative tendency of a pre-existing fault to reach re-activation by shear failure (Mode I) in the given 3D stress condition. *ST* on a fault is defined as the ratio of the maximum shear stress τ_{max} to normal stress σ_n normalised by the internal coefficient of friction μ that is expressed as tan(ϕ) where ϕ is the friction angle. Taking also into account the cohesion *C* the *ST* value can be defined as:

$$ST = \frac{\frac{\tau_{max} - C}{\sigma_n}}{\tan \phi}$$

A ST value close to zero indicates stable faults, whereas ST values close to one refer to critically stressed faults that are mature for re-activation. For $\sigma_n \leq 0$ we assign ST = -999 for the same reasons stated in the previous section. When compatibility to Neves et al. (2009) is wanted, the user must set $\phi = 45^{\circ}$ and C=0.

The dilatation tendency *DT* is a measure for the relative tendency of a pre-existing fault to dilate based on the 3D stress condition. It is defined as:

$$DT = \frac{S1 - \sigma_n}{S1 - S3}$$

For S1-S3 = 0 the stress state is lithostatic, i.e. the magnitudes of the three principal stresses are equal and DT = 1. For the fault plane parameter, the same convention holds on as explained in the previous section 3.4. The only difference is that the rake information is not needed and neither the value of the tensile strength.

Calculation of ST and DT values

The calculation of *ST/DT* is divided into the sections *All Zones* and *User selected Zones* (Fig. 3.5-1). In the first section the variables are estimated for all *Zones* (model increments/steps). Besides the absolute values for *ST/DT* the differential value between consecutive *Zones* can be estimated. The resulting variables D_ST_S and D_DT_S are written in the second *Zone*, i.e. in the first *Zone* of the model these values are zero. The variable D_ST_S or D_DT_S are flagged by -999 for a node if at least one of the single *ST/DT* values of the node is flagged. Furthermore, the value of the rake of τ_{max} (*ST_rake*) of the potential slip on the failure plane is determined.

The lower section allows the user to define between which *Zones* (model steps/increments) the cumulative differential slip or dilation tendency (D_ST_C , D_DT_C) is calculated. The D_ST_C/D_DT_C variables are zero for the selected first *Zone* and then increasing from step to step until the second *Zone* is reached. Positive differential *ST/DT* values (single and cumulative) indicate that the stress state has changed from one step to the next and that the fault is relatively closer to failure. Vice versa negative differential *ST/DT* values (single and cumulative) indicate that the fault has been brought relatively further away from failure. Note that the *ST/DT* values are relative measures and that even an increase in *ST/DT* can occur when the absolute distance to the failure envelope has increased.

General	Stress	FP	CFS	ST/DT	Int. surfaces	Ext. si	urfaces/polylines	
-Fault p	lane parar	neters						
Strike		11.000		Fric		riction angle 30.000		
	Dip	11.000			Cohes	sion	5.000	
√		slip/dilat		_rake, DT) ncy betweer	n each step (D_ST	_S, D_D	T_S)	
User s	Differentia elected zor	l slip/dilat nes	ion tende	ncy betweer	n each step (D_ST ncy (D_ST_C, D_D		T_S)	
User so	Differentia elected zor	l slip/dilat nes e different	ion tende	ncy between lation tender		T_C)	ep 1 Incr 2	*
User so	Differentia elected zor Cumulative	l slip/dilat nes e different Step :	ion tende tial slip/di	ncy between	ncy (D_ST_C, D_D	T_C)		•
User so	Differentia elected zor Cumulative	slip/dilat nes different Step Step	ion tende tial slip/di 1 Incr 1	ncy between lation tender	ncy (D_ST_C, D_D	oT_C) Ste	ep 1 Incr 2	• •

Fig. 3.5-1: Page *Slip and* Dilation *tendency*.

The page is divided in three sections. In the upper section the properties and orientation of the fault plane are stated for which the slip- and dilation tendency (ST/DT) is calculated. In the middle section slip and dilation tendency are calculated as well as the rake of the potential slip (ST_rake) and the difference of slip and dilation tendency between each model step (D_ST_S/D_DT_S). In the lower section the cumulative difference of these values (D_ST_C and D_DT_C) between two Zones selected by the user is calculated.

3.5.2 Application examples

Figure 3.5-2 shows the *ST* values as a contour plot. Both *ST* values are calculated for vertical faults with a strike of 25°N almost optimally oriented in the given stress field. The upper figure is for *Solution Time* 0.75 (increment 3) and the lower one for *Solution Time* 1.0 (increment 4).

Note that the interpretation of the resulting colour distribution is potentially misleading. E.g. the higher or lower ST or D_ST values near the faults that are implemented in the model do not indicate that the fault has been brought relatively closer or further away from failure. The calculation of the ST values is not based on the geometry of the faults that are implemented in the model, but to generic faults that are almost perpendicular to them. Thus, the resolved shear and normal stresses are very different.

If the user changes the parameter of fault settings or the rock properties and re-calculate e.g. the *ST* values, the results in all frames are changing on the fly. This enables the user of *GeoStress* to perform a fast and efficient analysis of the model results.

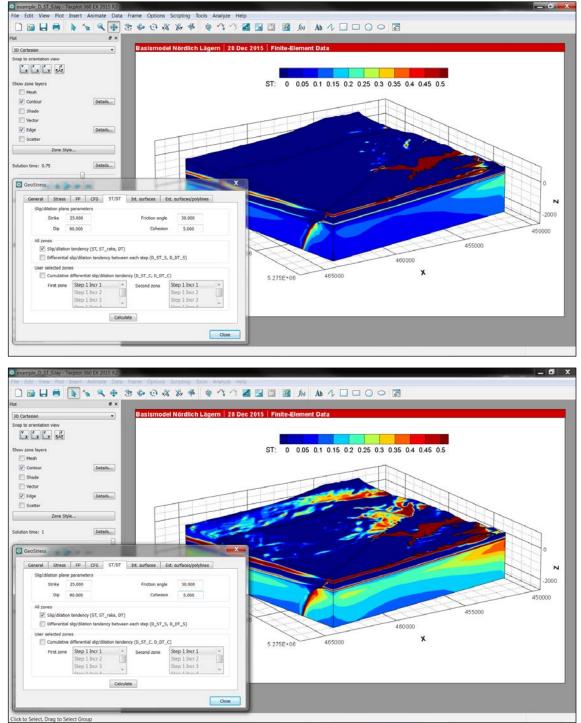


Fig. 3.5-2: Slip tende

-2: Slip tendency calculation. Both figures show the ST value calculated for vertical faults (dip=90°) that strike 25°N. The

Both figures show the S7 value calculated for vertical faults (dip=90°) that strike 25°N. The upper figure displays the ST value at *Solution Time* 0.75 (increment 3), the lower figure at *Solution Time* 1.0 (increment 4).

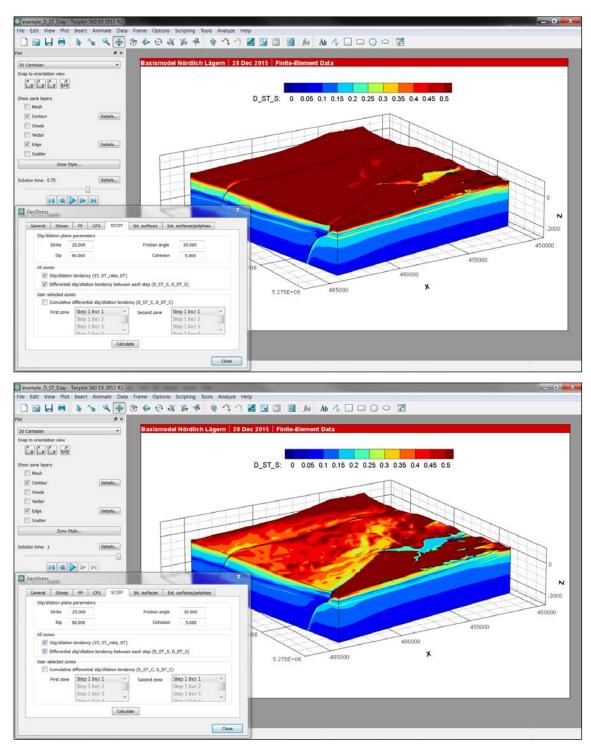
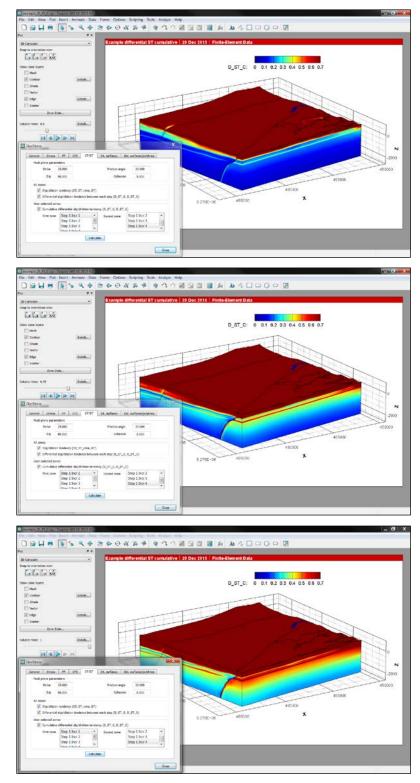


Fig. 3.5-3: Differential slip tendency between all *Zones*.

The upper figure shows D_DT_S in MPa for Step 1 Incr3 - Step1 Incr2. The lower figure shows D_ST_S in MPa for Step 1 Incr4 - Step1 Incr3. The D_ST_S values are always the difference to the previous *Zone* and written into the second *Zone*.



- Fig. 3.5-4: Cumulative differential slip tendency between the user defined *Zones*.
 - Figures show the D_ST_C in MPa for three steps. The upper figure shows D_ST_C for Step1 Incr2 Step 1 Incr1, the middle one for Step1 Incr3 Step 1 Incr2 and the lower one for Step1 Incr4 Step 1 Incr3. The value of D_ST_C that is presented in a *Zone* is always the difference to the selected first *Zone* and cumulative value.

3.6 Internal Surfaces

Generally, the add-on *GeoStress* distinguishes between two surface types: Internal and External. Internal surfaces are the ones that are implemented in the geomechanical-numerical model where relative sliding could occur. In Abaqus these surfaces are so-called contact surfaces. The potential sliding along these surfaces changes the stress field at the interface and in its vicinity. In contrast to this the external surfaces are generic and they are explicitly not part of the geomechanical-numerical model. They are used to visualize the model results and derived variables at desired 2D regions. This option is described in section 3.7.

With the page *Internal Surfaces* the user can map all variable that exist at the nodes of the finite element mesh including the variable that have been generated with *GeoStress* onto the internal surface. The geometry of these surfaces has to be imported from a text file with a format that will be described below. This import generates a new set of *Zones* for this geometry only and the results can be displayed over time (increments/steps) on these surfaces without showing the whole volume. For internal surfaces the user can also estimate the fault slip, i.e. the relative displacement of the blocks (Fig. 3.6-1).

GeoStress		
General Stress FP (CFS ST/DT Int. surfaces	Ext. surfaces/polylines
Internal surface		
Load geometry Normal and shear stres Internal surface (slip) Moving block	s (Normal CStress, Shear CStress, Reference block	Calculate
fault_1_N	fault_1_N	
TOUT_T_N	rount_1_iv	
fault_1_S	fault_1_S	
		Calculate
fault_1_S	fault_1_S	Calculate
fault_1_S fault_2_N fault_2_S	fault_1_S fault_2_N	
fault_1_S fault_2_N fault_2_S	fault_1_S fault_2_N fault_2_S	

Fig. 3.6-1: Page Internal Surfaces.

The page is divided into two sections. In the upper section the geometry files (*.txt) of the internal surface has to be loaded and the shear and normal stresses are calculated. In the lower section the relative movement between the two blocks of an internal contact can be estimated.

3.6.1 Internal surfaces represented as pairs of contact surfaces

In Abaqus the relative movement of blocks along a fault is implemented with a pair of contact surfaces. These so-called internal surfaces are made of faces of 3D finite elements within the 3D model geometry. A contact surface is a non-linearity of the model where the stress field changes due to the displacement along this surface. However, Tecplot 360 EX does not provide sufficient information about the geometry of the internal surface and thus it has to be imported again. This input file that describes the faces and nodes on the internal surface must

have the exact same node numbering and element definition as in the Abaqus model. Only element faces that are described with three or four nodes are accepted.

Example of the geometry input file for internal surfaces

```
**_ABAQUS_Input_Deck_Generated_by_HyperMesh_Version__:_12.0.0.85
** _Generated _using _HyperMesh-Abaqus _Template _Version _: _12.0
++
*NAME__fault_1_S
*NODE
_____974791, ___683685.31005814, ___276833.62794856, ___134.70187273715
_____978455, ___684980.76375911, ___277172.53241215, __84.299970524759
*ELEMENT, TYPE=S3
*ELEMENT, TYPE=S4
**
```

The structure of the input file *.txt must contain the following three key words: *NAME, *NODE, *ELEMENT, TYPE=S4 (or S3).

- Letters and/or numbers that follow the key word *NAME determine the name of the new *Zone* that is generated in Tecplot 360 EX, but only the first 25 characters are used.
- After the key word *NODE follows the original node numbering from the finite element mesh of the model and the coordinates of the nodes. The coordinates are in fact not used since Tecplot 360 EX knows from all original node numbering the coordinates. Field separators can be comma, tabs or blanks.
- After the key word *ELEMENT, TYPE=S3 (or S4) the (original) element-node assignments using the previously given nodes has to be provided.
- Comment line must begin with ** and the input file must end with a comment line.

Normal and shear stresses (variables *Normal Stress* and *Shear Stress*) can be estimated for the individual segments i.e. the element faces that define the contact surfaces. *GeoStress* calculates the normal vector of the element face from its nodes and estimates from the stress tensors at the nodes a mean stress tensor. In this context, the term element means only the appropriate face of a 3D element. Using the normal vector and the mean stress tensor *GeoStress* resolves the *Normal Stress* and *Shear Stress* and stores them as element face centred variables.

Abaqus also provides for contact surfaces the shear and normal stress in the *.odb output file. These variables are named *CPRESS* (Normal Stress), *CSHEAR1*, *CSHEAR2* and *CSHEAR3* (the three components of the shear vector given in a local coordinate system; *CSHEAR3* points into the normal vector of the element face and is zero). Tecplot 360 EX is loading these Abaqus

variables and renames them to *Contact Pressure* for the normal stress component, and *X Contact Traction, Y Contact Traction* and *Z Contact Traction* for the three shear vector components. The Z Contact Traction is zero whereas the other two components describe the shear stress on the fault segment. *GeoStress* uses also these values and renames them to the variables *Normal CStress* and *Shear CStress*.

The values from Abaqus and *GeoStress* can deviate from each other since Abaqus is using probably directly the stress tensor values from the integration points or the results from the equilibrium solution procedure for the contact surface. Thus, at surfaces with high curvature or with kinks the deviation can be larger. However, in these cases the artefacts that are generated at these kinks are much larger (and unrealistic) than the deviation between the two approaches. Furthermore, Tecplot 360 EX (version 2015 R2) is not reading the *Contact Pressure* variable correctly. It is only provided for the first contact surface, but not for other contact surface in the model. In general, the determined values from *GeoStress* should be slightly smoother than the values from Abaqus, but the deviations are clearly within the high numerical uncertainties of the implementation of faults as contact surfaces.

Fault slip

In the list boxes *Moving block* and *Reference block* the imported two surfaces of a contact pair can be used to calculate their relative displacements. One side is assigned to the *Moving block* and the other to the *Reference block*. Note that it is compulsory for the calculation of the fault kinematic that the surface normal (the normal for each element face that defines the surface) is facing outward from the contact surface pair. The orientation of the normal is determined through the order of element-node assignment according to the right-hand rule in the input file. In chapter 4 we present a way to check the orientation of the normal vectors in Tecplot 360 EX and in HyperMesh. *GeoStress* is calculating the following kinematic variables:

- X Slip, Y Slip and Z Slip: Vector (in the {X, Y, Z}-System) of the relative displacement of the moving block with respect to the reference block. This is needed from Tecplot 360 EX in order to display the slip vector in the Tecplot system.
- *Dip Slip*: Downwards oriented slip component on the surface.
- *Strike Slip*: Is given on the fault in direction of the strike slip component.
- *Slip Rake*: Slip direction on the surface (see failure plane variable for the definition of strike and rake).

These variables are stored in the *Zones* of the *Reference block*. Each increment is presented in one *Zone* and thus, if an increment is given for a special model time, fault slip rates can be derived. In chapter 4 we show how a fault slip variable can be determined in Tecplot 360 EX using the option Data/Alter/Specify Equations...

3.6.2 Application examples for internal surfaces

In order to generate the results displayed in Figure 3.6-2 (*Normal Stress*) and Figure 3.6-3 (*Dip Slip*) the geometry of the two surfaces that define the contact pair in the example model are provided in the geometry folder with the names fault_1_S.txt, fault_1_N.txt, fault_2_S.txt and fault_2_N.txt.

Fig. 3.6-2 shows that the normal stress is increasing with depth, but it also shows that this increase is not linear due to the curvature of the fault and due to the displacement boundary condition that is producing different tectonic stresses on the individual segments of the fault.

Fig. 3.6-3 shows that the dip slip also is not equally distributed over the surface of the fault. The dip slip is displayed on the southern surface. I.e., the values displayed show the displacement in dip slip direction with respect to the fixed northern block.

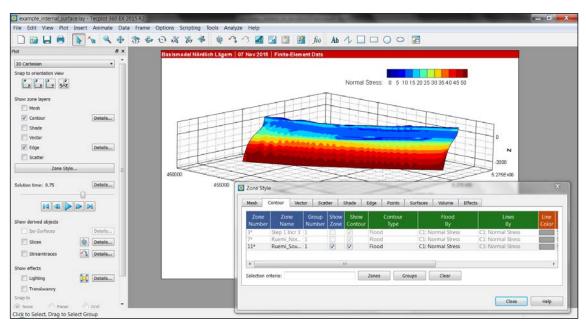


Fig. 3.6-2: Normal stress distribution on an internal surface.

The *Normal stress* is calculated for each increment on the surface. Note that the *Normal Stress* does not exist in the model volume, but only for the *Zones* where the internal and external surfaces are stored.

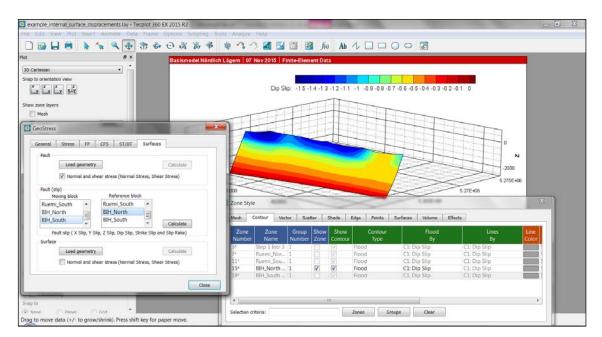


Fig. 3.6-3: Dip slip distribution on an internal surface.

The *Dip slip* is calculated for each increment on the surface. Note that the *Dip Slip* does not exist in the model volume, but only for the *Zone*s where internal surfaces are stored. External surfaces cannot have a relative displacement as they are not part of the model.

3.7 External surfaces and polylines

With the page *External Surfaces/Polylines* the user can map all variable that exist at the nodes of the finite element mesh including the variable that have been generated with *GeoStress* onto external surfaces or polylines. Note that an external surface has no impact on the model results since it was not present as a contact surface during computation. In that sense, it is a generic potential fault on which the model results are interpolated. The same holds on for a polyline that represents e.g. a planned borehole drilling path way.

The page is divided into two sections (Fig. 3.7-1). In the upper section an external surface can be loaded. In addition to the interpolation of all variable from the model volume the user can calculate the *Normal Stress* and *Shear Stress* as well as the values for Slip and dilation tendency (*Slip_T, Dilation_T*) and the Coulomb failure stress (*Coulomb_FS*) using the given fault plane parameter and the maximum shear stress values. Note that these fault plane parameters are only used for the calculation of the new variable for this fault. The values for slip and dilation tendency as well as for the Coulomb failure stress estimated in the other tab cards of *GeoStress* are not updated. In the lower section a polyline geometry can be imported and all values from the volume are interpolated on this line. For both geometries, new *Zones* are generated and can be displayed separately.

The geometry of the surface or polyline has to be imported from a text file with a format that will be described below. This import generates a new set of *Zones* for this geometry only and the results can be displayed over time (increments/steps) on these surfaces without showing the whole volume. I.e. for each increment the map variable can be displayed on the surface.

🦲 GeoStress							X
General	Stress	FP	CFS	ST/DT	Int. surfaces	Ext. surfaces/polylines	
Extern	al surface						
	Load geo]		Character	Calculate	
				-	rmal Stress, Shea , Dilation_T)	n Stress)	
				tress (Coul	omb_FS)		
	Fa	ilure pa	rameter -		30.000		
				n angle ohesion	10.000		
			Tension		0.000		
- Extern	al polyline Load geo	metry	1			Calculate	
						1	Class
							Close

Fig. 3.7-1: Page External Surfaces/Polylines.

The page is divided in two sections. In the upper section, external surfaces can be loaded in order to interpolate all values on these and to calculate for these normal and shear stresses, slip and dilation tendency (*Slip_T, Dilation_T*) as well as Coulomb failure stress (*Coulomb_FS*) using the given failure parameter. Note that these values are different from the ones calculated in the other tab cards. In the lower section an external polyline (e.g. representing a borehole pathway) can be loaded. For both geometries, new *Zones* are generated and all stress values are interpolated on these.

3.7.1 External surfaces for result visualisation

External surfaces are geometries that are not a part of the model. Thus, they are only used in order to display a posteriori variables from the model volume onto these surfaces. The format of the surface description is the same as for the internal surface except that only finite element meshes with triangles are allowed.

Example of the geometry input file for external surfaces

```
**_ABAQUS_Input_Deck_Generated_by_HyperMesh_Version_: 12.0.0.85
** Generated using HyperMesh-Abaqus Template Version : 12.0
* *
*NAME_External_Fault
*NODE
..... 982773,... 688871.28373095,... 276072.97816205,... -251.6813894955
.... 982774, 688795.9964581, . 276139.08833193, -259.2988903596
..... 982775,... 688719.20629053,... 276203.53128934,... -265.8293048217
.... 982776, 688640.90023015, 276266.34877857, -271.4864931561
...... .
.... 982777, 688562.55565372, 276328.72343553, -278.5207494841
.... 985820,... 684864.61374959,... 277905.62713435,... -987.984092963
 __ 985821,<u>_</u> 682612.87832328,<u>_</u> 277777.36569695,<u>_</u> -893.3797783981
*ELEMENT, TYPE=S3
.... 761142,.... 985816,.... 985670,.... 985821
.... 761141,.... 985636,.... 985821,.... 985670
.... 761140,.... 985430,.... 985504,.... 985820
.... 761139,.... 985509,.... 985820,.... 985504
..... 755302,..... 982878,..... 982879,..... 982880
.... 755301,.... 982868,.... 982869,.... 982870
```

Three key words determine the structure of the text file *.txt: *NAME, *NODE, *ELEMENT, TYPE=S3.

- Letters and/or numbers that follow the key word *NAME determine the name of the new *Zone* that is generated in Tecplot 360 EX, but only the first 25 characters are used.
- After the key word *NODE follows directly the node numbering of the model mesh and the coordinates of the nodes. Field separators can be commas, tabs or blanks.
- After the key word *ELEMENT, TYPE=S3 the element-node assignments, i.e. the definition of the element of the previously given nodes has to be provided.
- Comment line must begin with ** and the input file must end with comment line.

The variables for the normal stress and the shear stress (*Normal Stress, Shear Stress*) are calculated using the normal vector of the 2D surface element and the mean of the stress tensor at the face nodes. They are determined from the original Abaqus stress components *SXX, SYY, SZZ, SXY, SYZ* and *SZX* by the Tecplot 360 EX interpolation procedure. Note that the output variable *Normal Stress* and *Shear Stress* are 2D element centred variables.

3.7.2 External polyline for result visualisation

External polylines are also geometries that were not part of the model. Thus, they are only used to display a posteriori variables from the model volume onto these lines. The format of the polyline description is described in the following.

Example of the geometry input file for external polylines

```
*NAME Polyline_12345

** any comment

*NODE

1, 458195.00 ,5266455.00, 0.00

2, 458198.78 ,5266457.18, -0.00

900, 460360.06 ,5267705.00, -2495.64

901, 460360.06 ,5267705.00, -2500.00

**
```

Two key words determine the structure of the text file *.txt: *NAME and *NODE.

- Letters and/or numbers that follow the key word *NAME determine the name of the new *Zone* that is generated in Tecplot 360 EX, but only the first 25 characters are used.
- After the key word *NODE follow in each line the node numbering and the coordinates
 X, Y, Z of the nodes. Field separators can be tabs, commas or blanks.
- Comment lines must begin with ** and the input file must end with a comment line.

All nodal variables that exist in the model are interpolated onto the polyline.

3.7.3 Application example for external surfaces and polylines

To generate the results displayed in Figure 3.7-2 the geometry of an external surface is provided in the geometry folder with the name external_surface.txt. For the visualization of the shear stress the newly created *Zone* is activated in the *Zone Style* dialog box and the other *Zones* must be deactivated.

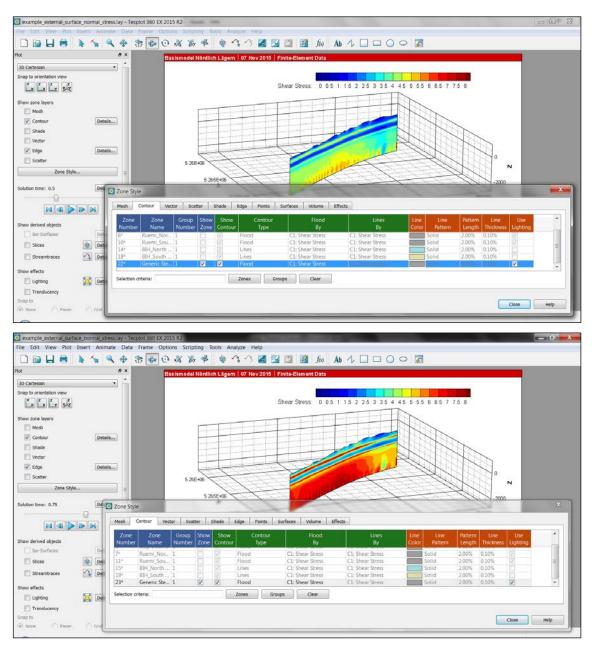


Fig. 3.7-2: Shear stress distribution on an external surface.

The *Shear Stress* is calculated for each increment on the surface. The upper figure is for *Solution Time* 0.5 (Step1 Inc2), the lower figure shows the results for *Solution Time* 0.75 (Step1 Inc3). Note the *Shear Stress* does not exist in the model volume, but only for the *Zones* where internal and external surfaces are stored.

3.7.4 Application example for external polylines

To generate the results displayed in Figure 3.7-2 the geometry of an external polyline is provided in the geometry folder with the name external_polyline.txt. For the visualization of the vertical stress S_v as an example the newly created *Zone* is activated in the *Zone Style* dialog box. To display the values the mesh colour of the polyline must be changed from a single colour to Multi 1 colour setting (see Fig. 3.7-2). Furthermore, the line thickness of the mesh should be increased to 1.5% and the Edge display option should be turned off.

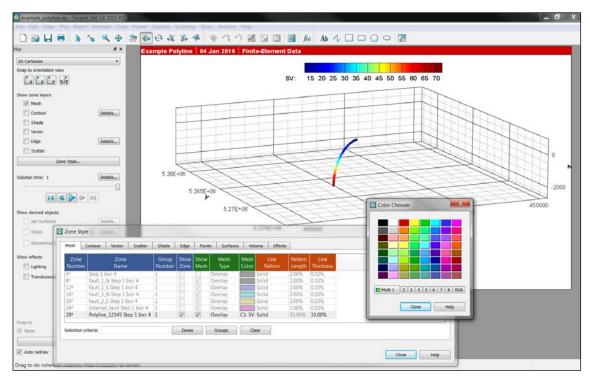


Fig. 3.7-3: Vertical stress along an external polyline.

The vertical stress S_v is calculated for each increment along the polyline. The figure shows the SV for the fourth *Solution Time* 1.0 (Step1 Inc4).

4 General tips for Tecplot 360 EX usage

This chapter presents several specific functionalities of Tecplot 360 EX that are probably useful for the analysis of geomechanical-numerical models. Furthermore, workflows are presented with examples how to further accelerate the analysis of model results.

4.1 Using Tecplot 360 EX layouts, Frame Styles and Macros

These three options are helpful to generate and load very fast a certain view on your data for a pre-defined variable for specific increment of a specific *Zone*.

Layout files

The layout file stores the actual view on your data as it appears on the screen using the menu bar File/Save Layout As... The view can contain several frames from different increments and set of *Zones*. The file simply links the view parameter to the *.plt file where the model results are stored in the Tecplot 360 EX format.

Frame Styles

A view of a single frame (the active one) can be stored in a file as a so-called *Frame Style* to apply the chosen settings to another model. It serves as a template to reproduce the view with all details of the setting. An example is given in the file with the name $3D_View_Z_Displacement.sty$. However, unfortunately the displayed variable – here the z component of the displacement - is not called with the variable name in the frame style description, but with the variable number that is attached to each model variable.

The following lines show the first lines of the *.sty file. The command to generate a contour plot I is followed in the next line by the option VAR=49 which is variable number but not the name of the variable.

The numbering of the variables can differ and depends on the Tecplot 360 EX analysis procedure of the user. Thus, when another model is loaded, but the order of the data analysis is different, the numbering of the variables changes as well and the *.sty-file would not produce the correct view results as it uses strictly the variable number that might have changed. The only way to avoid this is to load the individual model runs always in the same way and to generate in the same order the variable with *GeoStress*. The dialog box from the menu bar Data/Data Set Info. Tecplot 360 EX provides the user with the variable numbers that are assigned to each variable name (Fig. 4.1-1). When the number of the created variable is not correct anymore, the user can edit the *Frame Style* by changing the number.

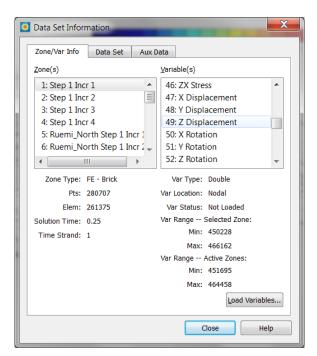


Fig. 4.1-1: Data set information dialog box.

Note that the numbers assigned to the model variable can change from one model to the next. The numbers are given in the order the variables are loaded or generated within Tecplot 360 EX (and the add-on *GeoStress*).

Macros

A macro is quite similar to a *Frame Style*, but even more powerful. The user can insert any commands that are provided by Tecplot 360 EX to analyse and display the model results. Using the menu bar *Scripting/Record Macro....* Tecplot 360 EX records all steps you are performing until you finish the recording. The generated *.mrc file looks very similar to the *.sty files as it uses the same header and same Tecplot 360 EX commands. In the example provided with the name *macro_example_RSR.mrc* the view from the z displacement view in the previous example is changed to a 3D view of the RSR value. Again Tecplot 360 EX is using the variable number instead of the variable name (RSR has the variable number 71 in the example).

```
#!MC 1410
$!VarSet |MFBD|='C:\Program Files\Tecplot\Tecplot 360 EX 2015 R2'
$!PICK ADDATPOSITION
X = 3.77792915531
Y = 1.37261580381
CONSIDERSTYLE = YES
$!SETCONTOURVAR
VAR = 71
.....
$!RemoveVar |MFBD|
```

However, in contrast to the *.sty file the choice of the variable can be changed using instead of the line VAR = 71 the command *\$!GETVARNUMBYNAME |MyVar| NAME="RSR"*. This edited version of the macro is provided in the file *macro_example_RSR_edited.mcr*. Note the macro is using the variable name instead of the variable number.

4.2 Write ASCII data from a surface

Tecplot 360 EX allows exporting for any *Zone* or set of *Zones* ASCII data of the model variable results using the menu bar *Tools/Write Data As Formatted Text*. The dialog displayed in Fig. 4.2-1 shows that the user has the full control on what is exported in which format. Of course, also the variables calculated with *GeoStress* are accessible.

💽 Write Data as Text File					
Choose Frames	Include Frame Names				
 Active Frame Selected Frames All Frames 	1 Basismodel Nördlich Läg				
Choose Zones All	Choose Variables All				
Generic Step 1 Incr 3 🔺	81:SHmax/SV - Best				
Generic Step 1 Incr 4	82:Shmin/SV - Best				
	82·0 5/SHmay-Shmin)/SV - F ∢ III ►				
Value Separator	Change Variable Format				
	Other Text				
Comma	Include Zone Names				
 Tab Space 	Include Var Names				
O Other	Include Text				
OK Cancel Help					

Fig. 4.2-1: Write Data as Text File dialog box. Note that the user can control for which *Zone* (increment, geometry) which variable is written to the ASCII output file.

4.3 Calculation of new variables with equations

From the existing variable in the model the user can calculate further variables using the menu bar *Data/Alter/Specify Equations...*. The user can either type in the equations in the dialog box that appears (Fig. 4.3-1) or load the equations from a *.eqn file. Examples are provided in the two files *delta_K.eqn* and *displacements.eqn*.

An example of the format is given below. Variables that exist in the model are stated in curly brackets. Tecplot 360 EX also provides a wide range of functions that can be integrated in the equations. Note that it is possible to alter variables in only one *Zone* (append the *Zone* number in square brackets) but it is not possible to create a new variable in only one *Zone*. More details are given in the Tecplot 360 EX user manual.

```
#!MC 1400
# Created by Tecplot 360 build 14.0.2.33360
$!ALTERDATA
EQUATION = '{ATVD} = ABS({TVD})+0.1'
$!ALTERDATA
EQUATION = '{K_OCR} = 0.6*(0.58*(1+(650/{ATVD}))**0.42)+0.4'
$!ALTERDATA
EQUATION = '{Delta_K} = {Shmin/SV}-{K_OCR}'
```

Specify Equations						x
Equation(s)						
						* III *
Data Set Info						ons
Default Equation Modifiers						
Zones to Alter		Index Ran	iges			
1: Step 1 Incr 1			Start	End	Skip	
2: Step 1 Incr 2	Ξ	I-Index	1	Mx	1	
3: Step 1 Incr 3		J-Index	1	Mx	1	
4: Step 1 Incr 4		-				
5: Ruemi_North Step 1 Incr 1		<u>K</u> -Index	1	Mx	1	
6: Ruemi_North Step 1 Incr 2 - New var data type: Auto -					•	
All Active None New var location: Auto						•
Compute Close Help						

Fig. 4.3-1: Write Data as Text File dialog box.

Note that the user can control for which *Zone* (increment, geometry) which variable is written to the ASCII output file.

4.4 Calculation of the normal vector of surfaces

The following workflow presents how to generate and visualize the normal vector of surfaces in the model. Go to the menu Analyse/Calculate Variables and select there the function Grid K Unit Normal (Vector) in the appearing dialog box (Fig. 4.5-1). Choose for the *New Var Location = Cell Center* and turn off the button *Calculate on Demand* in order to store the calculated variable. Press the button Calculate in order to calculate the three components *X Grid K Unit Normal, Y Grid K Unit Normal, Z Grid K Unit Normal* of the unit vector of all geometries (Fig. 4.5-2).

Calculat	e		X
Name	Grid K Unit Normal (vect	Select	
Normalize	e with Respect To	No Normalization	•
New Var I	Location	Cell Center	-
Calcul	late on Demand		
		Calculate	
		Close	Help

Fig. 4.4-1: Dialog box for calculation of variables.

This tool box offers a huge range of functions that can be applied. For further details see the Tecplot 360 EX manual.

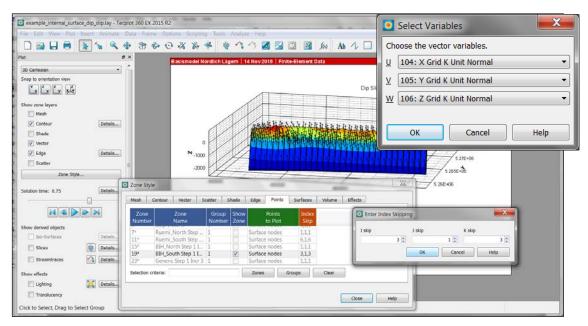


Fig. 4.4-2: Visualization of the normal vector of surfaces.

Upper right dialog box shows how to choose the three components of the vector to be displayed. As the number of vectors can be rather large Tecplot 360 EX offers the possibility to display a reduced number of vectors. This is controlled in the *Zone Style*.... on the page Points with the Index Skip. The dialog box on the right bottom shows the I and K direction only every third vector should be displayed.

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