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Three dimensional modelling of fractured and faulted reservoirs: Framework and Implementation

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Abstract

Modelling of coupled physical processes in fractured and faulted media is a major challenge for the geoscience community. Due to the complexity related to the geometry of real fracture networks and fault systems, modelling studies have been mainly restricted either to two dimensional cases or to simplified orthogonal fracture systems consisting of vertical and horizontal fractures. An approach to generate three dimensional meshes for realistic fault geometries is presented. The method enables representation of faults in an arbitrary incline as two dimensional planes within a three dimensional, stratified porous matrix of a generic geometry. Based on a structural geological model, the method creates three dimensional unstructured tetrahedral meshes. These meshes can be used for finite element and finite volume numerical simulations. A simulation of a coupled fluid flow and heat transport problem for a two layered porous medium cut by two crossing faults is presented to test the reliability of the method.

Keywords: fault systems, fractured reservoirs, thermal hydraulic coupling, finite element method, numerical simulation, 3D mesh generator

1 1. Introduction

The objective of this paper is to describe the influence of fractures and faults on fluid flow and transport properties in fractured and faulted reservoirs. In principle, faults may represent preferential pathways for fluids, or can act as a geological barrier. These two options depend essentially on the origin and orientation of the faults in relation to the recent and paleo stress field (Barton et al., 1995; Gudmundsson, 2001; Moeck et al., 2008; Scheck-Wenderoth et al., 2008; Magri, 2010).

In general, fractured reservoirs can be handled in two ways. The reliability of hydraulic prop erties of fractured reservoirs is connected to the size of a potential representative elementary

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volume (REV) (Bear, 1972; De Marsily, 1986). The representative elementary volume (REV) 10 is the smallest volume over which a measurement can be made yielding a value representative 11 of the whole. To completely represent fractures and faults in reservoirs a REV is not sufficient. 12 Below the REV, the relevant parameter is not defined and the material must be treated as hetero-13 geneous with a high variability of its properties. Above the REV the material can be considered 14 as a statistically homogeneous and ergodic medium and can be modelled as an "equivalent ho-15 mogeneous" medium. An overview concerning this problem, commonly referred to as "the scale 16 effect," and the corresponding concepts to model the hydraulic flow is given by Guéguen et al. 17 (1996). The description of fracture models and their characteristic parameters has been achieved 18 with various theoretical approaches. Several methods have been developed to solve the sophis-19 ticated problem of transferring the complex structure of natural rocks to adequate, equivalent 20 models. Such methods include the deterministic fracture networks (Kolditz, 1995a,b; David, 21 1993), fractal fracture networks (Kosakowski, 1996; Acuna and Yortsos, 1995) and stochastic 22 fracture networks (Cacas et al., 1990b,a; Bruel et al., 1994; Wollrath, 1990; Zimmermann et al., 23 2000). 24

In all areas of geo-energy research, (e.g. CO_2 sequestration and storage, shale gas and geother-25 mal energy) the development of adequate reservoir and deposit models are of primary concern, 26 while studying the dynamic behaviour during reservoir utilisation. Evaluating the response of 27 geological deposits during CO₂ sequestration and storage (Ketzin site; e.g. Juhlin et al. (2007)), 28 shale gas extraction (Barnett shale; e.g. Gale et al. (2007)) or geothermal heat recovery (Groß 29 Schönebeck site; e.g. Blöcher et al. (2010)) requires an understanding of the complex three di-30 mensional geometry of the deposits. This geometry is difficult to assess, because the scale of 31 numerical and experimental investigation alters the size of the measured parameters. Upscaling 32 is an ongoing relevant issue (e.g. Lock et al., 2004; Zimmermann et al., 2003; McDermott et al., 33 2006). In case their size exceeds the correspondent REV, faults and fractures have to be treated 34 as discrete objects in a reservoir model. Therefore, geometric modelling and mesh generation 35 was the subject of several previous studies (Blessent et al., 2009; Kalbacher et al., 2007). We 36 developed a 3D finite element model with unstructured tetrahedral meshes for matrix properties 37 with embedded 2D discrete surfaces representing the faults and fractures. 38

The paper is organised as follows: After describing the general modelling techniques applying 3D geological structures and 2D planar surfaces to obtain a combined 3D mesh, we give an example of such a system with two geological layers and two dipping fault systems. This mesh is then used for a coupled thermal-hydraulic simulation. Finally, the results of this model are presented and discussed.

44 **2.** Description of model techniques and methods

Understanding and predicting physical processes occurring in complex fractured geological 45 systems requires numerical models capable of simulating the coupling between the processes 46 involved in their realistic three dimensional geological framework. The present paper describes 47 a direct approach to generate unstructured tetrahedral meshes suitable for finite element or finite 48 volume numerical simulations of coupled processes for complex faulted natural geological sys-49 tems. The procedure is fully automated in a C++ source code written by the authors and provides 50 3D meshes that can be directly imported by existing numerical software. In the following, the 51 different steps of the method are schematically illustrated for a relatively simple case geometry 52 consisting of two geological layers cut by a system of two intersecting faults. 53

The first step is to integrate the geological structures defining the geometry of the unstructured model (Figure 1). The input data required are files of scattered data points (x-y-z coordinates) of the layer interfaces (Figure 1a). The scattered data are read and then interpolated to triangular surfaces in 3D space. For this purpose, we used an algorithm which combines a two-dimensional Delaunay triangulator to calculate x-y values (Shewchuk, 2002) and inverse distance weighting (IDW) interpolator to calculate z-values, see Figure 1b.

In the second stage, faults are implemented in the model (Figure 2). Faults are represented as two dimensional planar structures embedded in a three dimensional geological boundary volume. A multiple regression of the scattered data points describing the geometry of the fault (Figure 2a) is performed to find the best fitting plane of the set of points. The theory behind the multiple regression algorithm can be found in Rinne (2008). After projecting the points onto the plane, the convex hull describing the outer geometry of the fault plane is calculated based on a modified version of Graham's algorithm (Graham, 1972) as described in O'Rourke (1998), see Figure 2b.

Locations of the intersections between the geological surfaces and the convex hulls defining the faults are then calculated (Figure 3a). To represent the trace of the fault in the face of each geological surface, the location of the nodal points of the nearest triangles to the intersection segment is shifted to exactly match the line describing the trace of the fault (Figure 3b).

The final three dimensional Delaunay mesh is generated using the TetGen¹ program devel-71 oped at the Weierstraß Institute for Applied Analysis and Stochastic (WIAS) (Si, 2008). TetGen 72 generates adaptive tetrahedral meshes suitable for numerical methods, such as finite element or 73 finite volume methods. For meshing purposes, all three dimensional domains must be defined by 74 their boundaries by means of surface meshes resulting in piecewise linear complexes (PLC), see 75 Figure 4. In order to represent the fault planes as PLCs intersecting facets during the meshing 76 process, crossing of faces has to be avoided. For this purpose, calculated intersection segments 77 between the geological surfaces and the fault planes are added to the fault polygons. 78

Figure 5a and Figure 5b illustrate the final three dimensional mesh generated by the TetGen program. A constrained Delaunay triangulation along the fault plane is imposed to represent the geometry of the fault facets (Figure 5c).

A case-study based on this geometry for a thermo-hydraulic (T-H) problem is presented in the 82 remainder of this paper. For modelling, the numerical simulator OpenGeoSys² is used (Wang 83 et al., 2009; Watanabe et al., 2010). OpenGeoSys is an open source finite element simulator 84 used for the solving of thermal, hydraulic, mechanical and chemical (T-H-M-C) processes in 85 fractured porous media, developed in cooperation between the Department of Environmental In-86 formatics of the Helmholtz Centre for Environmental Research (UFZ, Leipzig), the TU Dresden, 87 the Federal Institute for geosciences and natural Resources (BGR, Hannover), the Paul-Scherrer 88 Institute (PSI, Villigen, Switzerland), the University of Kiel and the University of Edinburgh. 89 TetGen output files are exported to OpenGeoSys format by using the pre-processing software 90 GINA4³. 91

¹http://tetgen.berlios.de/

²www.opengeosys.net

³GINA Version 2.1.5 A Pre- and Postprocessing Tool for the Scientific Program System OpenGeoSys, Copyright 2005-2009, Herbert Kunz, Stilleweg 2, 30655 Hannover, Germany, herbert.kunz@ bgr.de

32 3. Description of the sample model

93 3.1. Model geometry

To show the applicability of the previously generated finite element mesh, a three dimensional T-H simulation was performed. The model volume consists of two sub-horizontal geological layers, including two dipping faults (Figure 6). The horizontal north-south and east-west extensions are 200 m, resulting in a horizontal model area of 40.000 m². The two geological layers are vertically bordered by three curved surfaces. The elevation of top, middle and bottom surface is $55 \text{ m} \pm 5\text{ m}$, $0 \text{ m} \pm 7 \text{ m}$ and $-45 \text{ m} \pm 5 \text{ m}$, respectively. Therefore, an average thickness of 55 m for layer 1 and 45 m for layer 2 is established (Table 1).

Both faults are penetrating the two geological layers. Fault 1 has a length of 233 m and is striking North-East, with dip coordinates of 316.7°; 80.6°. Fault 2 has a length of 184 m and is oriented perpendicular to fault 1, having dip coordinates of 225°; 63.2° (Table 2).

104 3.2. Initial and boundary conditions

During the simulation, a general flow field from the South to the North is generated. For 105 this purpose, Dirichlet (or first-type) boundary conditions for pressure are set along the southern 106 and northern boundaries. According to the definition of hydrostatic pressure, the pressure at the 107 southern border is constant at $p(x, y = -100 \text{ m}, z) = \rho gz + 1.75E+06$ Pa and at the northern border 108 at $p(x, y = 100 \text{ m}, z) = \rho gz + 1.25E+06 \text{ Pa}$ (Figure 7a), where ρ [1000 kg/m³], g [9.81 m/s²] and 109 z denotes the fluid density, gravitational acceleration and height of liquid column, respectively. 110 An average hydraulic gradient $\nabla h = 5E+05$ Pa / 200 m = 0.25 from the South to the North is 111 provided. For the remaining domain, a pressure value of 1.75E+06 Pa is initialized. 112

To generate an inflow of hot and cold water from the southern border, Dirichlet boundary conditions for temperature are also applied. Along the southern border, temperature increases from 40°C to 80°C, in going from West to the East resulting in a temperature profile of T (x, y = -100 m, z) = 0.2° C/m * x + 60°C (Figure 7b). For the remaining domain, the initial temperature is set to 60°C.

118 3.3. Parametrisation

¹¹⁹ To assure a variation of the hydraulic properties, the upper geological layer was modelled ¹²⁰ twice as conductive as the lower layer (Table 1). The permeability *k* of layer 1 is set to 2E-14 m² ¹²¹ and the porosity ϕ to 0.15. For layer 2 the permeability k is set to 1E-14 m² and the porosity ϕ ¹²² to 0.08. The storage of both layers is derived from the bulk compressibility β [1/Pa] of the rock ¹²³ and the embedded fluid. Assuming fissured rocks, the storage is set to 7E-10 1/Pa.

The hydraulic properties of the faults vary as well (Table 2). The permeability of fault 1 is set to 1E-08 m² and that of fault 2 to 5E-09 m². The fault transmissivity is defined as the product of the fault permeability *k* and aperture *a*. To ensure a high contrast between fault transmissivity and matrix conductivity, the aperture of both faults is set to 0.05 m. To provide free fluid flow in the faults, a porosity value of 1.0 is chosen. The storage in the faults is due to the fluid compressibility only and $\beta = 4.6E-10$ 1/Pa is assigned.

To observe the most significant changes of the temperature field a simulation time of 145 years is chosen.

132 4. Results

The results are presented in two parts. The first part displays the primary results for fluid pressure, velocity and temperature field of the total domain. The second part will show the pressure, velocity and temperature evolution through time of three observation points within the faults. After starting the simulation, the pressure and velocity field of the model domain change due to the chosen boundary conditions. After approximately one month a steady state for pressure and velocity field is achieved (Figure 8).

Due to the fact that the implemented faults do not cut the southern and northern borders of the 139 model, matrix flow is predominant in these areas. Therefore, the highest pressure gradients are 140 at the northern and southern borders of the model (Figure 8a). In proximity to the cutting faults, 141 the isobars (surfaces of constant pressure) are sub-horizontal due to high flow rates within the 142 faults. Maximum Darcy velocities of v = 1E-04 m/s can be observed inside the faults (Figure 143 8b). Despite low pressure gradients, high flow rates occur in the fault planes. High values of 144 fluid velocity are the result of the relative high transmissivity of the faults with respects to the 145 surrounding domain. 146

Figure 8b shows the stationary flow field. As described above, highest flow velocities can be 147 observed in the fault planes. The applied pressure boundaries force a regional flow field from 148 the South to the North. The average velocity at the southern and northern regions is 1E-07 m/s, 149 with maximum inflow to the faults from the South. In the rest of the domain, outflow from 150 the faults into the rock matrix is pronounced. In the central part of the model, faults act as the 151 predominant flow paths. In contrast, low velocities (less than 1E-08 m/s) characterize the eastern 152 and western boundaries. An additional important fact is that at the southern edge of fault 1 and 153 fault 2, backward flow from the North to the South occurs. Pressure equalisation within the faults 154 results in higher matrix pressure at this area. This causes drainage of the rock matrix by the fault 155 system. 156

¹⁵⁷ Figure 9a-9d shows the 45°C, 55°C, 65°C and 75°C contours at four different time stages.

Before stationary field conditions for pressure and velocity are reached, conductive heat trans-158 fer does not affect the initial temperature field significantly (Figure 9a). After achieving the 159 stationary pressure and velocity field, convective heat transfer (advection and diffusion) becomes 160 predominant. The cold water front ($T = 55^{\circ}C$) enters fault 1 after approx. 4 months (Figure 9b). 161 Due to the geometry of fault 1 with respects to the southern boundary of the domain, cold water 162 enters fault 1 in the upper part. After 35 years, (Figure 9c) cold water from fault 1 and hot water 163 from fault 2 are mixed at the fault intersection. The final temperature field (Figure 9d) shows an 164 average temperature of $T = 55^{\circ}C$ in the northern part which is less than the mean initial temper-165 ature of 60° C. The depression from the mean value is caused because fault 1 is more conductive 166 than fault 2, which drives higher amounts of cold water into the system. 167

For a detailed observation of the pressure, velocity and temperature evolution inside the two faults, three observation points were set (Figure 10a).

All three observation points are located at the interface between the two geological layers. 170 Observation point 1 is located at the edge of fault 1 and has an elevation of 5.12 m. Observation 171 point 2 is located at the edge of fault 2 and has an elevation of -3.18 m. Observation point 172 three is located at the intersection of both faults with an elevation of 0.0 m. After starting the 173 simulation the pressure increases at all observation points (Figure 10b). As shown for observation 174 point 3 (Figure 10c), the initial magnitude of the velocity is due to vertical flow only. The 175 observed downward flow is forced by the initial pressure conditions in combination with the 176 chosen pressure boundary. Therefore, an initial increase of fluid pressure is observed. After 1 177

month, a stationary pressure and velocity field is reached, as indicated by the horizontal lines
 in Figure 10b-10c. Differences between the three observation points are due to their specific
 elevation.

The vertical component of velocity decreases over time from 3E-02 m/s to 1E-08 m/s, and the 181 horizontal flow from the South to the North with velocities between 1E-05 m/s and 1E-04 m/s 182 becomes dominant. As mentioned before, the cold water reaches the fault system at the edge of 183 fault 1 (Figure 10d) after approx. 4 month. After an additional 17 months, cooling at observation 184 point 3 begins. At the same time, hot water reaches fault 2 first. Due to the lower transmissivity 185 of fault 2, the hot water reaches the intersection point after 10 years, and cooling at observation 186 point 3 stops. Higher amounts of cold water enter the fault intersection (observation point 3) 187 from the more conductive fault 1, causing temperature to decrease to 55°C. This corroborates the 188 observation of the temperature field for the total domain. 189

190 5. Discussion

Potential fluid flow along faults depends on the current stress regime of the reservoir. For 191 a normal faulting stress regime, faults have high shear stress and high slip tendency. At the 192 transition of normal to strike slip faulting, the potential fluid flow along these critically stressed 193 faults increases. For strike slip faulting, a reactivation of faults with high slip tendency is possible 194 (Moeck et al., 2008). Currently, faults are represented by planar polygons in 3D space with 195 constant properties for aperture and permeability. Further, the presented sample model does not 196 integrate a mechanical coupling. This restriction was made to keep the sample model simple and 197 is not due to limitations of the applied finite element simulation software. OpenGeoSys provides 198 the possibility of a mechanical coupling, and the hydraulic properties of discrete features can 199 be adjusted in space and time depending on the stress state. These important dependencies of 200 fracture and fault transmissivity can be mapped and modelled (Warpinski et al., 2008; Walsh 201 et al., 2008) and/or determined by laboratory experiments (e.g. influence of asperity creep on 202 fracture permeability by Cuisiat et al. (2002)). The integration of the functional relation between 203 stress state and fault transmissivity will result in a better approximation of the natural systems. 204

205 6. Conclusions

The presented modelling techniques, methods and the case-study describe the technical work-206 flow from scattered structure geological data to the final finite element simulation. These tech-207 niques and methods can be applied for fractured porous media, including fault systems. Since 208 the complexity of the geometric system increases rapidly with increasing numbers of fracture 209 and faults, the applied techniques and methods must be tested by means of future applications 210 including more discrete features than in the case-study. Geo-energy research related topics, e.g. 211 CO₂ storage, shale gas extraction and geothermal heat recovery can be benefit from these tech-212 niques and methods. The advantage is that dipping structures can be integrated into a 3D body 213 representing a porous media, and interaction between discrete flow paths and rock matrix can be 214 simulated. Further, the complete workflow is captured by open-source software. The integra-215 tion of discontinuities within the geological layers by normal, reverse, and listric faults (curved 216 normal faults) is ongoing work. 217

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224 References

- Acuna, J., Yortsos, Y., 1995. Application of fractal geometry to the study of networks of fractures and their pressure
 transient. Water Resour. Res. 31 (3), 527–540.
- Barton, C. A., Zoback, M. D., Moos, D., 1995. Fluid flow along potentially active faults in crystalline rock. Geology
 23 (8), 683–686.
- 229 Bear, J., 1972. Dynamics of Fluids in Porous Media. American Elsevier, New York.
- Blessent, D., Therrien, R., MacQuarrie, K., 2009. Coupling geological and numerical models to simulate groundwater
 flow and contaminant transport in fractured media. Computers & Geosciences 35 (9), 1897–1906.
- Blöcher, M. G., Zimmermann, G., Moeck, I., Brandt, W., Hassanzadegan, A., Magri, F., 2010. 3D numerical modeling
 of hydrothermal processes during the lifetime of a deep geothermal reservoir. Geofluids.
- Bruel, D., Cacas, M., Ledoux, E., de Marsily, G., 1994. Modelling storage behaviour in a fractured rock mass. Journal of
 Hydrology 162 (3–4), 267–278.
- Cacas, M. C., Ledoux, E., de Marsily, G., Barbreau, A., Calmels, P., Gaillard, B., Margritta, R., 1990a. Modeling fracture
 flow with a stochastic discrete fracture network: Calibration and validation 2. the transport model. Water Resources
 Research 26(3), 491–500.
- Cacas, M. C., Ledoux, E., de Marsily, G., Tillie, B., Barbreau, A., Durand, E., Feuga, B., Peaudecerf, P., 1990b. Modeling fracture flow with a stochastic discrete fracture network: Calibration and validation 1. the flow model. Water
 Resources Research 26(3), 479–489.
- Cuisiat, F., Grande, L., Høeg, K., 2002. Laboratory testing of long term fracture permeability in shales. SPE/ISRM Rock
 Mechanics Conference, 20-23 October 2002, Irving, Texas, 10.
- 244 David, C., 1993. Geometry of flow paths for fluid transport in rocks. J. Geophys. Res. 98 (B7), 12267–12278.
- 245 De Marsily, G., 1986. Quantitative Hydrogeology. Academic Press, Inc., Orlando, FL.
- Gale, J. F. W., Reed, R. M., Holder, J., 2007. Natural fractures in the Barnett Shale and their importance for hydraulic
 fracture treatments. AAPG Bulletin 91(4), 603–622.
- Graham, R. L., 1972. An efficient algorithm for determining the convex hull of a finite planar set. Information Processing
 Letters 1 (4), 132–133.
- Gudmundsson, A., 2001. Fluid overpressure and flow in fault zones: field measurements and models. Tectonophysics
 336 (1-4), 183–197.
- ²⁵² Guéguen, Y., Gavrilenko, P., LeRavalec, M., 1996. Scales of rock permeability. Surveys in Geophysics 17, 245–263.
- Juhlin, C., Giese, R., Zinck-Jørgensen, K., Cosma, C., Kazemeini, S. H., Juhojuntti, N., Lüth, S., Norden, B., Förster, A.,
 2007. 3D baseline seismics at Ketzin, Germany: The CO2SINK project. Geophysics 72 (2), B121–B132.
- Kalbacher, T., Mettier, R., McDermott, C., Wang, W., Kosakowski, G., Taniguchi, T., Kolditz, O., 2007. Geometric
 modelling and object-oriented software concepts applied to a heterogeneous fractured network from the Grimsel rock
 laboratory. Computational Geosciences 11(1), 9–26.
- Kolditz, O., 1995a. Modelling flow and heat transfer in fractured rocks: Conceptual model of a 3-D deterministic fracture
 network. Geothermics 24 (3), 451–470, hot Dry Rock (HDR) Reservoir Modelling Activities within Europe.
- Kolditz, O., 1995b. Modelling flow and heat transfer in fractured rocks: dimensional effect of matrix heat diffusion.
 Geothermics 24 (3), 421–437, hot Dry Rock (HDR) Reservoir Modelling Activities within Europe.
- Kosakowski, G., 1996. Simulation von Strömung und Wärmetransport im variszischen Grundgebirge: Vom natürlichen
 Kluftsystem zum numerischen Gitternetzwerk. VDI Verlag Reihe 7, Nr. 304, 124.
- Lock, P. A., Jing, X., Zimmerman, R. W., 2004. Comparison of methods for upscaling permeability from the pore scale
 to the core scale. Journal of Hydraulic Research 42, 3–8.
- Magri, F., 2010. Deep geothermal groundwater flow in the Seferihisar-Balçova area, Turkey: results from transient
 numerical simulations of coupled fluid flow and heat transport processes. Geofluids.
- McDermott, C. I., Lodemann, M., Ghergut, I., Tenzer, H., Sauter, M., Kolditz, O., 2006. Investigation of coupled hy-
- draulic geomechanical processes at the KTB site: pressure-dependent characteristics of a long-term pump test and elastic interpretation using a geomechanical facies model. Geofluids 6 (1), 67–81.

- Moeck, I., Schandelmeier, H., Holl, H. G., 2008. The stress regime in a Rotliegend reservoir of the Northeast German
 Basin. International Journal of Earth Sciences 98 (7), 1643–1657.
- 273 O'Rourke, J., 1998. Computational Geometry in C, 2nd Edition. Cambridge University Press.
- 274 Rinne, H., 2008. Taschenbuch der Statistik., 4th Edition. Verlag Harri Deutsch.
- Scheck-Wenderoth, M., Krzywiec, P., Maystrenko, Y., Zühlke, R., Froitzheim, N., 2008. Permian to Cretaceous tectonics
 of Central Europe. In McCann, T. (Ed): Geology of Central Europe. Geological Society Special Publication, London
 27, 2999–1030.
- Shewchuk, J. R., 2002. Delaunay refinement algorithms for triangular mesh generation. Computational Geometry: The ory and applications 22(1–3), 21–74.
- Si, H., 2008. Three dimensional boundary conforming Delaunay mesh generation. PhD. Thesis. Ph.D. thesis, Technische
 Universität Berlin, Institut für Mathematik.
- Walsh, R., McDermott, C., Kolditz, O., 2008. Numerical modeling of stress-permeability coupling in rough fractures.
 Hydrogeology Journal 16, 613–627.
- Wang, W., Kosakowski, G., Kolditz, O., 2009. A parallel finite element scheme for thermo-hydro-mechanical (THM)
 coupled problems in porous media. Computers & Geosciences 35 (8), 1631–1641.
- Warpinski, N., Mayerhofer, M., Vincent, M., Cipolla, C., Lolon, E., 2008. Stimulating unconventional reservoirs: maximizing network growth while optimizing fracture conductivity. SPE Unconventional Reservoirs Conference, 10-12
 February 2008, Keystone, Colorado, USA, 19.
- Watanabe, N., Wang, W., McDermott, C. I., Taniguchi, T., Kolditz, O., 2010. Uncertainty analysis of thermo-hydro mechanical coupled processes in heterogeneous porous media. Computational Mechanics 45(4), 263–280.
- Wollrath, J., 1990. Ein Strömungs- und Transportmodell für klüftiges Gestein und Untersuchungen zu homogenen Er satzsystemen. PhD. Thesis. Ph.D. thesis, Universität Hannover.
- Zimmermann, G., Burkhardt, H., Engelhard, L., 2003. Scale dependence of hydraulic parameters in the crystalline rock
 of the KTB. Pure and Applied Geophysics 160, 1067–1085.
- Zimmermann, G., Körner, A., Burkhardt, H., 2000. Hydraulic pathways in the crystalline rock of the KTB. Geophys. J.
 Int. 142, 4–14.

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Table 1: Geometrical attributes and porous medium properties of geological layers.

property	unit	layer1	layer2
average thickness t	[m]	55	45
porosity ϕ	[-]	0.15	0.08
storage β	[1/Pa]	7E-10	7E-10
permeability k	$[m^2]$	2E-14	1E-14

Table 2: Geometrical attributes and medium properties of faults.

property	unit	fault1	fault2
dip direction	[°]	316.7	225
dip	[°]	80.6	63.2
length <i>l</i>	[m]	233.5	183.8
aperture a	[m]	.05	.05
porosity ϕ	[-]	1	1
storage β	[1/Pa]	4.6E-10	4.6E-10
permeability k	[m ²]	1E-8	5E-9



Figure 1: Workflow of finite element mesh generation: scattered data points resulting from structural geological modelling (1a) and triangulated interfaces of geological layers (1b).



Figure 2: Workflow of finite element mesh generation: scattered data points describing the faults geometry (2a) and final convex hull of the outer fault polygons (2b).



Figure 3: Workflow of finite element mesh generation: calculating faults-layers intersection (3a) and re-arrangement of the nodal position of the triangular elements of the geological surfaces to match the trace of the intersecting fault (3b).



Figure 4: Workflow of finite element mesh generation: creating a PLC of the model domain.



Figure 5: Workflow of finite element mesh generation: final 3D tetrahedral mesh.



Figure 6: Sample model consisting of two geological layers cut by a system of two crossing faults.



Figure 7: Pressure (7a) and temperature (7b) boundary conditions of the sample model. The pressure boundaries involve a general flow from the South to the North. The temperature boundary generates an inflow of 80° C hot water at the south-east and 40° C cold water at the south-west corner.



Figure 8: Simulated steady pressure (8a) and velocity field (8b) achieved after approx. 1 month.



Figure 9: Temperature contour plots (45°C, 55°C, 65°C and 75°C isosurfaces) at four different time stages.



Figure 10: Location of three observation points within the fault faces (10a); Simulated pressure (10b) and temperature (10d) values at these observation points and simulated velocity components (10c) at observation point 3.