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Sensitivities of injection rates for single well CO₂ injection into saline aquifers

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1 **1 Title**

2 Sensitivities of injection rates for single well CO₂ injection into saline aquifers

3

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10 **3 Abstract**

11 This paper investigates methods to predict potential injection rates of CO₂ into a saline aquifer and
12 analyses the sensitivities of the input parameters. Geological parameters are based on conditions at
13 the European CO₂ Onshore Research Storage and Verification Project in Ketzin, Germany and varied
14 within an acceptable range. Two injection regimes for CO₂ are analysed: pressure controlled injection
15 and power plant controlled injection, where the CO₂ flux depends on the load curve of a 600 MW_{net}
16 lignite power plant. The results are determined with a numerical model and compared to an
17 analytical solution with constant pressure injection. The injection rates depend mainly on the
18 geological setting and only slightly on technical parameters. Aquifer permeability and thickness show
19 approximately linear sensitivity and have a dominant impact. Depth is also of high importance, but
20 the impact is more complex and is based on geothermal temperature and hydrostatic gradient, which
21 affect viscosity, compressibility and caprock stability. Vertical anisotropy is insensitive. The difference
22 in the mean rate between constant pressure injection and power plant controlled injection is 8 %.
23 Peak injection rates are 29 % above mean injection rates, which shows that the reservoir can
24 effectively dampen rate variations. The analytical solution predicts the highest injection rates, the
25 lowest temporal variability and decreasing rates with injection duration. The numerical solution
26 predicts a stronger temporal variability and the rates increase with duration. In the initial phase the
27 differences between the methods add up to a factor of 1.45.

28 Keywords: CCS, injection, sensitivity, Ketzin, saline aquifer, analytical, numerical, well, rate

4 Introduction

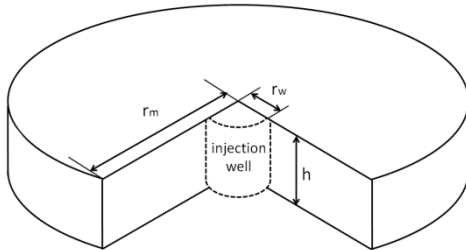
Carbon capture and storage (CCS) is a potential method for the reduction of CO₂ emissions into the atmosphere and is believed to help mitigate global warming (IPCC 2005). The complete CCS chain consists of the separation of CO₂ from industrial and energy-related sources, transport to a storage location and long-term isolation from the atmosphere by sequestration in geological formations. Implementation of the CCS technology on the scale needed to achieve a significant impact on the reduction of CO₂ emissions requires knowledge of available CO₂ storage capacity, which is addressed in several studies (e.g. Bachu and Adams 2003, Kopp et al. 2009, Holloway 2009, Bachu et al. 2007). However, only a few studies quantify the impact of geological and technical parameters on the potential injection rates (e.g. Nordbotten et al. 2005, Mathias et al. 2009a) and these are based on analytical solutions. Nevertheless, these rates are essential for the design and operation of injection schemes. Their sensitivities depend on input parameters, which can be calculated by analytical solutions and numerical simulations. We compare both, and while analytical solutions provide fast and robust results, compared to numerical simulations they are more limited in capturing physical processes. In the present case the limitations include the assumptions of a sharp phase interface, incompressible CO₂ and a temporally invariant CO₂ injection flux. However, in the present application both methods do not consider other potentially relevant processes, such as interactions between multiple injection wells, non-isothermal effects or the limited extent of the reservoir.

To our knowledge, currently no study has estimated the potential injection rates into a deep saline aquifer taking into account the temporal variability of a CO₂ stream produced from the operation of a power plant.

In this study we perform numerical simulations to define sensitivities of potential injection rates taking into consideration a realistic power plant CO₂ load curve. The model simulates isothermal injection of CO₂ into a saline aquifer with an infinite extent. The well boundary is considered at the aquifer elevation, while the processes in the well itself are described by Nimtz et al. (2010). The storage formation is a saline aquifer whose geological parameters are constructed to match those occurring at the injection site Ketzin, Germany (Schilling et al. 2009). The simulation, which is carried out with these parameters, serves as a central point for the sensitivity analysis. The sensitivities are calculated by sequential variation of the parameters injection pressure, aquifer permeability and thickness, well diameter, vertical anisotropy and compressibility. From this sensitivity functions are derived, which can be applied to calculate the change in the potential injection rate depending on the corresponding parameter values. Furthermore simulations are carried out to assess the impact of

1 CO₂ compressibility and hysteresis of relative permeability. Using this procedure the most sensitive
2 input parameters are identified and differences between analytical and numerical solutions are
3 demonstrated.

4 5 Material and Methods



5
6 **Figure 1: Model domain of the numerical models. The model is 2-D radially symmetric, r_w is the radius of the**
7 **injection well, r_m the radius of the model domain, h denotes the thickness of the aquifer. Except for the**
8 **injection well all boundaries are no flow.**

9

10 5.1 Numerical Model

11 The simulations are based on a 2D radially symmetric aquifer (Figure 1). In the radial direction the
12 domain is discretised with 100 cells. The first cell has a lateral extent of 1 m, with the extent of the
13 next cell increasing by a factor of 1.043, resulting in a radius of 100 km. In the vertical direction the
14 model is discretised by 25 cells using uniform spacing. The aquifer has no dip. The fully penetrating
15 injection well is located at the centre of the domain. The properties of CO₂ are adapted from Altunin
16 (1975), brine properties from Battistelli et al. (1997) and the partitioning of CO₂ and brine is
17 calculated according to Spycher and Pruess (2005). Outer boundary conditions are no flow, while it is
18 ensured that the aquifer emulates infinite extent (see below). Simulations are isothermal and carried
19 out with the simulator E100 Version 2008.2 (Schlumberger 2009).

20 5.2 Analytical Solution

21 Mathias et al. (2009a) provide an analytical solution for the injection pressure p . The solution
22 represents the injection of CO₂ into an infinite brine aquifer with a sharp interface between both
23 phases. The aquifer is homogeneous and only a single permeability can be applied for both CO₂ and
24 brine. For each phase a viscosity can be specified, but the application of compressibility is limited to
25 brine and rock while CO₂ is assumed to be incompressible. The solution includes Forchheimer flow
26 for the CO₂ phase. It is not possible to simulate a power plant controlled injection regime. The

1 solution is developed for constant rate injection but nevertheless, a slightly variable rate for constant
 2 injection pressure is determined by iteration with sufficient accuracy. The pressure slightly increases
 3 during the injection period and consequently the maximum pressure is reached at the end of the
 4 period. For a shorter duration a higher mass flow is possible. A quasi transient mass flow is calculated
 5 as a sequence of maximum injection rates with a shorter duration. The difference in the cumulative
 6 mass flows between both approaches is less than 1 %. This difference in the cumulative injection
 7 mass is corrected by scaling the time to the cumulative mass injection.

8

9 5.3 Simulation parameters

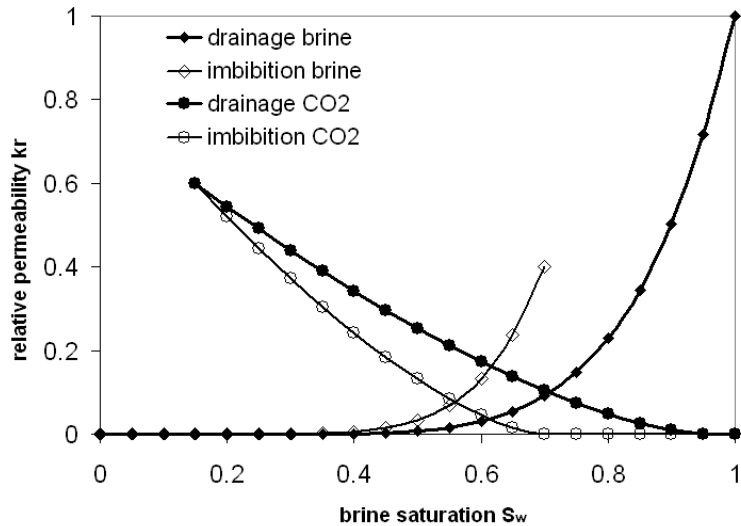
10 The parameter set is constructed to mimic the conditions at the Ketzin test site, provided in Table 2.
 11 The formation properties permeability and compressibility of $7.2 \times 10^{-5} \text{ bar}^{-1}$ are taken from Wiese et
 12 al. (2010). Formation thickness and porosity are derived from Norden et al. (2010). The vertical
 13 anisotropy is estimated based on permeability values from Norden et al. (2010).

14 The relative permeability formulation follows the Corey approach (1954)

$$k_{ri}(S_i) = K \left(\frac{(S_i - S_{i,residual})}{(1 - S_{i,residual} - S_{j,residual})} \right)^{n_i} \quad \text{Equation 1}$$

15 With k_{ri} as the relative permeability of phase i, K as (saturated) permeability, S_i the actual saturation
 16 of phase i, $S_{i,j,residual}$ the residual saturation of the respective phase and n_i a dimensionless exponent.
 17 The phase i may represent either CO_2 or brine and therefore j represents the other phase. For
 18 parameterisation the values listed in Table 1 were used. These are mean values from the parameter
 19 range proposed by Schepernisse and Maas (2009) based on measurements of sandstone cores at the
 20 Ketzin test site.

21 The resulting relative gas permeabilities for residual gas saturation differ for drainage and imbibition.
 22 For consistency both values are set to 0.6. The other parts of the curves are scaled proportionally.
 23 The resulting relative permeabilities (Figure 2) are applied to the model. The capillary pressure is
 24 simulated in the same way for drainage and imbibition and follows Equation 2 with S_w as the wetting
 25 phase saturation and the parameter values $a= 0.096$, $b= 0.125$ and $n= -0.989$.



1

2 **Figure 2: Relative permeabilities of brine and CO₂. Residual brine saturation is 15%.**

$$p_c = \left(\frac{S_w - b}{a} \right)^n \quad \text{Equation 2}$$

3 The PVT properties of CO₂ change with depth. For the applied geothermal and hydraulic gradient
 4 (Table 2) between 642 m and 1000 m density and viscosity increase up to 134 % and 114 %,
 5 respectively, while the increase between 1000 m and 2000 m is only 5 % and 10 %, respectively. The
 6 depth of 1000m is chosen as the central point because here the PVT properties are separated in a
 7 high variation region for shallower conditions and a low variation region for deeper conditions. Since
 8 saline aquifers frequently have a lower salinity than at Ketzin the salinity was slightly decreased to
 9 the round number of 20 %. The permitted injection overpressure at Ketzin is 22.9 bar (Köhler, 2009),
 10 so a feasible (round number) pressure of 20 bar is adopted at the central point.

11 The CO₂ load curve is adapted from a basic load 600 MW_{net} lignite power plant with 4 blocks. The
 12 base length is 365 days, which is repeated for a time series of 20 years. The maximum and minimum
 13 rates are 29 % above and 50 % below the mean annual rate, respectively.

14 For comparison with the analytical solution numerical simulations with incompressible CO₂ are
 15 carried out. For these cases and for the analytical solutions PVT properties for both phases are
 16 adapted to meet the equilibrium conditions of the aquifer.

17

5.4 Characteristic injection rates

For all solutions the injection rate $\dot{m}(t)$ is time variant. Characteristic injection rates are calculated with Equation 3 to ensure comparability. Depending on the limits t_1 and t_2 different characteristic rates are obtained.

$$\bar{\dot{m}}_i = \frac{1}{t_2 - t_1} \int_{t_1}^{t_2} \dot{m}_i(t) dt \quad \text{Equation 3}$$

The times t_1 and t_2 define the respective interval and $\bar{\dot{m}}_i$ is the characteristic injection rate. The mean injection rate for the numerical solution is denoted $\bar{\dot{m}}_{num,cp}$ for constant pressure injection, $\bar{\dot{m}}_{num,pp}$ for power plant controlled injection and $\bar{\dot{m}}_{a,cp}$ for the analytical solution (which implies constant pressure). All mean injection rates are obtained with $t_1=0$ and $t_2=20$ years. When the injection is pressure controlled $\dot{m}(t)$ is always the maximum for the time interval and can also be used to set up temporal regression. For power plant controlled injection the determination of temporal regression requires that the actual rate $\dot{m}_{num,pp}(t)$ be scaled in order to ensure that the reservoir can sufficiently buffer the fluctuations so that they do not induce a higher pressure than allowed. The parameter $\bar{\dot{m}}_i$ in equation 3 is time dependent for power plant controlled injection, denoted as $\bar{\dot{m}}_{num,pp}(t)$ and calculated as a window function with the length of the window t_2-t_1 equal to the base length of the load curve, which is 365 days and $t = t_1$.

5.5 Sensitivity analysis

Based on one central point a picture of the impact of each parameter is obtained by variation of one parameter for each simulation (Table 3) while keeping the other parameters constant. However, if several parameters change simultaneously the sensitivity of individual parameters may change due to the nonlinear nature of the processes. Formerly insensitive parameters may become sensitive or vice versa. In order to account for these effects the insensitivity of domain and discretisation are double checked for the highest and lowest injection rates.

Simulations are carried out to ensure that the bottomhole pressure does not exceed the feasible pressure. A constant well pressure is set as boundary condition, for which a transient injection rate is computed by the simulator. This procedure is not applicable for power plant controlled injection. The injection rate is given by the power plant load curve and most of the time the well pressure is below the feasible pressure. The feasible pressure is only reached during short periods, because the constant pressure boundary cannot be used since it would affect the injection rate. The task is to

1 scale the characteristic rate $\bar{m}_{num,pp}(t)$ so that the feasible pressure is reached exactly at the
2 injection peaks. This cannot be carried out by the simulator. The scaling factor is determined by two
3 regression functions instead, which are calculated using values from the annual maximum pressure.
4 Four simulations with different mean injection rates are carried out with annual maximum pressures
5 on both sides of the feasible pressure (an iterative approach). From the temporal regression (see
6 below) it is known that the break-even point (when $\bar{m}_{num,pp}(t)$ is equal to $\bar{m}_{num,pp}$) will be reached
7 after 7 years. Based on this the feasible mean injection rate $\bar{m}_{num,pp}$ is determined.

8 One simulation is carried out with the mean injection rate $\bar{m}_{num,pp}$ for the entire duration. The
9 maximum pressure p is determined for each year. The inverse of the regression function through p
10 describes the temporal scaling for the injection rate. The first year is not included because the base
11 length of the power plant load curve is one year and because the pressure fluctuations are too high
12 to be accurately described with the present approach.

13 Different formulations are applied when fitting the sensitivities, with preference given to the
14 simplest formulation that provides the minimal deviation. Most formulations could be fitted with
15 linear and exponential functions.

16 Polynomial formulations would provide a perfect fit for up to 3 points, but they would potentially
17 include a local maximum. Therefore exponential regression functions were applied and set up with
18 respect to physical behaviour. They include the zero-zero point when reasonable, for example no CO₂
19 is injected at zero injection pressure. The temporal sensitivity of power plant controlled injection
20 requires a more sophisticated regression formulation including three parameters, a reciprocal and a
21 logarithm. The regressions are fitted by a minimisation of the sum of the squared residuals, using the
22 software R (www.r-project.org).

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6 Results

6.1 Model convergence

The results from the model are insensitive with regard to discretisation. Further refinement by a factor of 10 (1 m to 0.1 m) does not change the injection rate, while an increase by a factor of 5 reduces the injection rate by 2 % (191 t/d to 187 t/d). The extent of the model is proven to be large enough to mimic an infinite extent aquifer. When increasing the radius from 100 km to 1000 km with the identical number of cells and the identical size of the cells next to the well, the injection rate for the central point is not affected. Also, for the simulation with the highest injection rate, the latter increase in radius affects the potential injection rate by only 0.4 %, which is considered not to be significant.

6.2 General behaviour

Pressure controlled numerical solution

In the numerical solution with pressure controlled injection at the very beginning ($t < 2 \text{ min}$) of injection the actual injection rate is about twice as high as the mean rate. Later ($t \leq 1 \text{ d}$) the rate decreases to about 70 % of the mean injection rate and then stabilises after 1 day of injection. Beginning from day 30 until the end of the simulation at 20 years the injection rate increases by 10 %, with the maximum at the end of injection (Figure 3).

The regression curve for temporal behaviour is shown in Figure 3. Beginning from day 10 the injection rates are reproduced with sufficient accuracy. They follow an exponential function (Table 4) with a mean numerical injection rate $\bar{m}_{num,cp}$ of 193 t/d. At 2598 days (7.1 years) the break-even point is reached, whereby the actual injection rate $\dot{m}_{num,cp}(t)$ is identical to the mean injection rate $\bar{m}_{num,cp}$.

Pressure controlled analytical solution

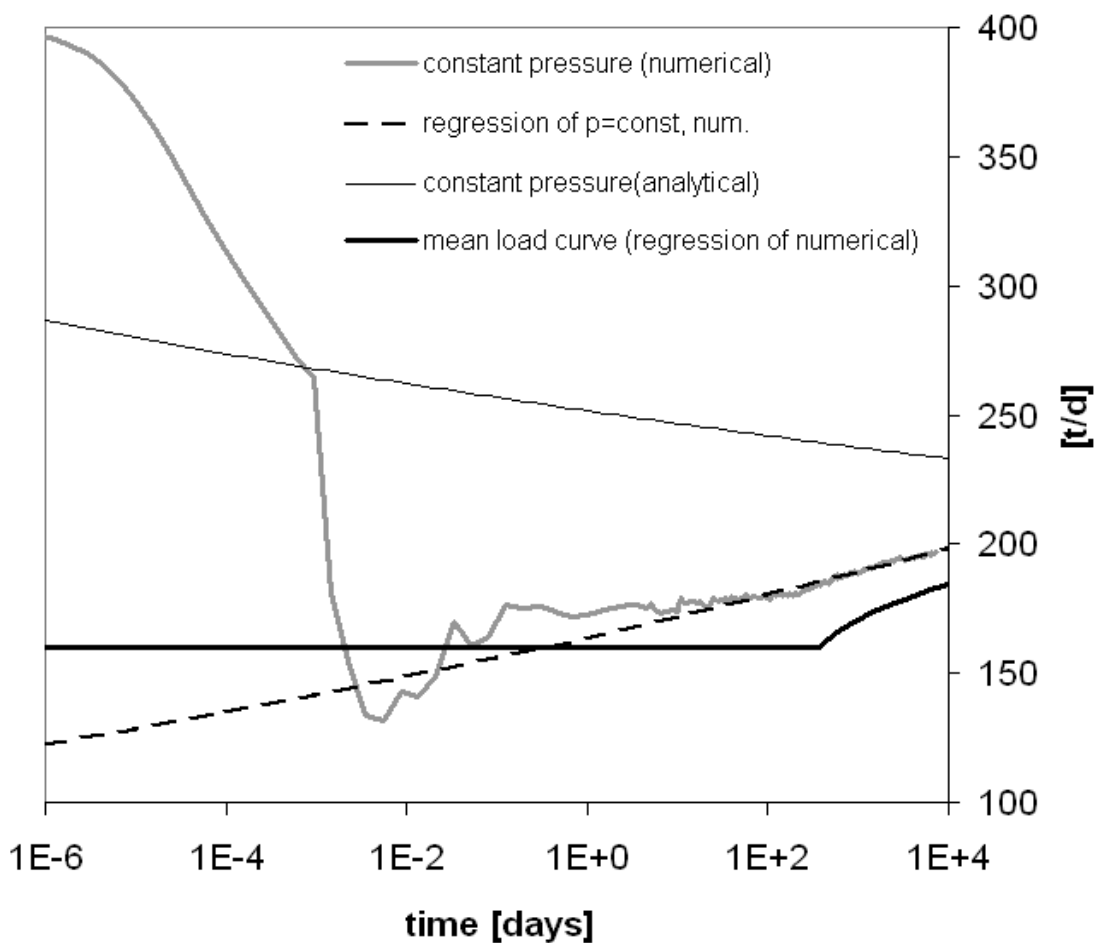
The analytical solution shows some important differences. The mean injection rate $\bar{m}_{a,cp}$ is 233 t/d, which is 21 % higher than in the numerical solution. At all times the rates are higher than calculated with the numerical model. The main reason is that the relative permeability of CO_2 is always equal to 1, whereas it has values of between 0 and 0.6 in the numerical solution and that the CO_2 phase is considered to be incompressible. In contrast to the numerical model, the injection rate decreases

1 continuously. At 2957 days (8.1 years) the break-even point is reached and the actual injection rate
2 $\dot{m}_a(t)$ is identical to the mean injection rate \bar{m}_a .

3 Power plant controlled numerical solution

4 The maximum mean injection rate for the power plant load curve $\bar{m}_{num,pp}$ is 178 t/d, which is 8 %
5 lower than in the numerical solution with constant injection pressure. During the first year the
6 injection is simulated at a constant rate because the reservoir potential to dampen load curve
7 oscillations is reduced if the mass of reservoir CO₂ is too small. Injection fluctuations should be
8 especially avoided during this time. Similar to the numerical solution with constant pressure, the
9 injection potential continuously increases with time. At 2949 days (8.1 years) the actual injection rate
10 $\bar{m}_{num,pp}(t)$ is identical to the mean injection rate $\bar{m}_{num,pp}$.

11



12

13 **Figure 3: Temporal injection rate at the central point, calculated with the numerical model and the analytical**
14 **solution. The regression function corresponds to the numerical model.**

1

2 6.3 Sensitivities

3 All sensitivities (eight) have been calculated with the numerical solution of constant pressure
4 injection. With the analytical solution only six sensitivities could be calculated, as due to the
5 limitations it was not possible for vertical anisotropy and for power plant controlled injection to be
6 calculated. For power plant controlled injection only two sensitivities are determined, those for the
7 pressure and duration of injection.

8 The impact of the parameters on the injection rate is presented in Table 4. Except for anisotropy and
9 temporal dependence an initial estimation could be carried out applying linear sensitivities. On the
10 other hand, except for permeability and aquifer thickness, a nonlinear fit provides increased
11 accuracy. The exponent of the nonlinear sensitivity shows the grade of nonlinearity.

12 For the purpose of design sensitivities have to be considered in conjunction with respective
13 parameter variability. From this point of view the most important parameter is aquifer permeability.
14 The injection rates are almost proportional to this parameter and the high variability results in an
15 absolute sensitivity of 0.1 to 10.2 (Table 4). Sensitivity differences between the analytical solution
16 and numerical solution are small.

17 Injection pressure has the second highest impact on the mean injection rates. They are nearly
18 proportional to the pressure for both constant well pressure and power plant injection, but for the
19 analytical solution the exponent of 1.158 exhibits a considerable non-linear rate dependence.
20 Doubling injection pressure increases the injection rate by a factor of 2.23. This is because
21 intermediate saturations do not exist and therefore relative permeabilities are always equal to one.
22 With compressible CO₂ the nonlinearity would be even stronger. The mean injection rate is
23 proportional to aquifer thickness. The sensitivities are identical for numerical and analytical
24 solutions, which show that buoyancy effects are negligible.

25 The potential injection rate increases by a factor of about 1.8 for reservoir depths between 650 m
26 and 2000 m in the numerical solution. The viscosity of the brine decreases with higher temperature
27 at a greater depth, but the density of the brine hardly changes. For the CO₂ phase the temperature
28 effect is compensated by the higher pressure, i.e. density and viscosity increase roughly
29 simultaneously, so that flow resistance per mass flux remains roughly constant ($\pm 5\%$). However, for
30 the same mass, the specific injection volume becomes more important for shallow depths because
31 the density of CO₂ increases by 134 % between 650 m and 1000 m and only by 5 % between 1000 m

1 and 2000 m. Therefore the volume flux is much higher and more brine has to be replaced for the
2 same mass of CO₂. Furthermore, the rate decrease for shallow injection is much more pronounced in
3 the analytical solution because the CO₂ phase is treated as incompressible. By contrast, in the
4 numerical solution the compressibility of the CO₂ increases significantly with depth and hence leads
5 to a higher storage coefficient for shallow aquifers. This decreases the radius of influence and
6 therefore allows a higher injection rate. Numerical simulations show that the assumption of
7 incompressible CO₂ reduces injection rates by 5% at 1000 m depth and by 51% at 650 m depth.

8 Increasing rock compressibility allows higher injection rates with a parameter range variability factor
9 of 1.5 to occur. The reason is again due to higher compressibility decreasing the radius of influence.
10 The impact of rock compressibility is highest for the deepest scenario where the total compressibility
11 (sum of CO₂, brine and rock) is smallest. Since CO₂ compressibility is disregarded rock compressibility
12 has the highest impact on the radius of influence in the analytical solution, with a variability factor of
13 1.72 (Table 3).

14 The injection rate changes with the duration of the injection. The trend can be described with an
15 exponential function, leading to a much higher impact at the beginning of injection than at the end.
16 In the numerical solutions the potential rate increases, while it decreases in the analytical solution.
17 The decrease occurs due to the reduced relative permeability at intermediate phase saturation,
18 where CO₂ and brine obstruct each other. The sum of both relative permeabilities is significantly
19 lower than one (Figure 3). With increasing time this region migrates further from the injection well
20 and has a lower impact. Numerical simulations show that the assumption of incompressible CO₂
21 hardly affects temporal behaviour at the central point.

22 The rate of reduction is more pronounced for power plant controlled injection. After one year
23 $\bar{m}_{num,pp}(t)$ is only 90 % of $\bar{m}_{num,pp}$, while $\dot{m}_{num,cp}(t)$ is 96 % of $\bar{m}_{num,cp}$. Later the dampening effect of
24 increased storativity becomes more important. After 20 years $\bar{m}_{num,pp}(t)$ is 103 % of $\bar{m}_{num,pp}$ and
25 $\dot{m}_{num,pp}(t)$ is 102 % of $\bar{m}_{num,pp}$.

26 In the analytical solution neither relative permeability nor compressibility are incorporated.
27 Therefore it behaves more like an ordinary pumping test and the rate decreases continuously with
28 constant pressure injection. The rate difference is smaller than in the numerical solution, equalling
29 only 7 % between 1 day and 20 years.

1 For load curve controlled injection the overpressure is below the feasible pressure for most of the
2 time. Therefore, the mean injection rate is 8 % lower compared to constant pressure injection.
3 Nevertheless, due to periods of low injection, it is possible to increase the rate for short periods by
4 about 19 % above the pressure controlled rate. Because maximum injection pressure also depends
5 on the rate history it does not occur at the maximum injection rate, but the rates are within a range
6 of 3 % below maximum.

7 Several parameters show a very low sensitivity. Hysteresis does not affect the injection rate. Slight
8 pressure differences occur for power plant controlled injection during phases when the rate is low
9 and the well pressure is far below the feasible value. Physically this is reasonable, the injection never
10 ceases and therefore drainage is the dominant process. The pore pressure is also practically
11 insensitive. When disregarded the injection rates decrease by only 2 %. Also the sensitivity of the
12 well diameter is low. A change by more than a factor of 4 results in a 4 % difference in the injection
13 rate.

14

15 **7 Discussion**

16 The present study allows quantification of the potential mass flow of CO₂ during well injection with a
17 constrained maximum injection pressure. All methods provide mean rates which are within a
18 variation range of 30 %. The analytical method of Mathias et al. (2009b) provides the largest
19 predicted value $\bar{m}_{a,cp}$ of 233 t/d. However this solution tends to overestimate the rates because it
20 does not consider permeability reduction due to relative permeabilities, and also tends to
21 underestimate the rates because the CO₂ is assumed to be incompressible. With the numerical
22 model both effects are considered and a mean injection rate $\bar{m}_{num,cp}$ of 193 t/d can be achieved,
23 which shows that the latter effect is dominant at the applied central point for a depth of 1000 m.
24 Additionally the fact that the CO₂ load curve displays temporal variations because it depends on the
25 load curve of a power plant must be considered. With a realistic load curve an injection rate $\bar{m}_{num,pp}$
26 of 178 t/d can be achieved. This is 30% lower than the prediction from the analytical method.
27 Nevertheless, considering the numerous impacting factors on the potential injection rate, the
28 relevance of this difference should not be overestimated.

29 The temporal behaviour differs for the three approaches. In the analytical solution the temporal
30 development of the injection rate shows only a slight decrease. The rate has the minimum value at

1 the end of the injection period, where it is only 199 % of the mean rate, while an increase is
2 predicted in the numerical solutions for constant pressure and power plant load curve with 102 %
3 and 103 % of the mean injection rates, respectively. The initial behaviour is more important. For
4 constant pressure injection after one year 96 % of the mean injection rate $\bar{m}_{num,cp}$ can be achieved
5 and the ratio is only 90 % of $\bar{m}_{num,pp}$ for the power plant controlled rate. For the latter case it must be
6 taken into account that during the first year the injection rates are constant, otherwise the ratio
7 would be much lower.

8 The predicted rates depend on the prediction tool. The analytical solution shows an unrealistically
9 high depth sensitivity for depths shallower than 1000 m. At 650 m the rates are 68% lower, while the
10 numerical solution provides results that are only 21 % lower than the respective rates at the central
11 point. The difference of 47 % occurs because at shallow depths CO₂ is highly compressible. If this is
12 neglected the radius of influence is much higher, whereby injection rates are much lower. At greater
13 depths the difference is only 3 % because CO₂ compressibility decreases significantly. A slight
14 overestimation of injection pressures (in our case underestimation of the rates) was expected by
15 Mathias et al. (2009b) since the assumption of incompressible CO₂ is not strictly valid for the
16 temperature and pressure regions which typically occur during CO₂ sequestration. It can be affirmed
17 that the effect occurs, but it must be emphasised that the effect is much more pronounced for
18 shallow depths. Due to incompressible CO₂ the analytical solution is also more sensitive to rock
19 compressibility, but the difference between the methods is only between 2 % and 15 %.
20 Nevertheless, rock compressibility shows moderate sensitivities to the rates and may have an impact
21 factor of 1.5.

22 The geological situation has a much higher impact than the prediction method. The most important
23 parameters are hydraulic permeability and aquifer thickness. The injection rate is proportional to
24 these values, but since hydraulic permeability varies by several orders of magnitude aquifer thickness
25 has less of an impact. Caprock stability defines the maximum feasible injection pressure and the
26 stability itself depends on depth. As a rule of the thumb feasible pressure increases linearly with
27 hydrostatic pressure (Birkholzer et al. 2009) or with lithostatic pressure (Hovorka et al. 2004),
28 whereas sustainable injection pressure increases linearly with depth. The mean injection rate is
29 nearly proportional to the pressure for both constant well pressure and power plant injection. Taking
30 this into consideration the potential injection rate between 1000 m and 2000 m increases by a factor
31 of about 2. Additionally higher temperatures cause lower brine viscosity, which increases the

1 potential injection rate by a factor of about 0.5. Altogether the depth related effects add up to a
2 factor of 2.5 for the increase in the potential injection rate between 1000 and 2000 m.

3 The technical means to increase injection rates are limited. The only parameter which is not directly
4 or indirectly affected by geological properties is the borehole diameter. However, within a
5 reasonable range, the absolute sensitivity is only 4 %. In reality this could be slightly higher because
6 the analysed approaches do not include drying due to brine evaporation.

7 Technical injection schemes imply a temporal change in the CO₂ load curve. For the present load
8 curve the peak injection rate $\dot{m}_{num,pp}(t)$ is 29 % higher than the mean, but the mean injection rate
9 $\bar{m}_{num,pp}$ is only 8 % lower compared to the pressure controlled rate $\bar{m}_{num,pp}$ since reserves are built
10 up during times of lower injection. The peak injection rate $\dot{m}_{num,pp}(t)$ may be 19 % higher than the
11 mean injection rate $\bar{m}_{num,cp}$, which also means that technical solutions to decrease the peak rate have
12 an impact potential of less than 8 % on the mean injection rate. Nevertheless, at the beginning peak
13 loads should be decreased by technical measures to rapidly achieve a certain amount of CO₂, which
14 can effectively dampen the pressure response of the rate variations.

15 The geological setting is adapted to the unfavourable Ketzin conditions. A mean injection rate
16 $\bar{m}_{num,pp}$ of 178 t/d might appear to be low but this value is highly sensitive to a number of
17 parameters. In storage formations permeabilities are frequently higher (Kopp et al. 2009). Also
18 aquifer thickness and maximum injection pressure (Mathias et al. 2009b) may have considerably
19 higher values. For more favourable conditions, namely higher permeability, greater thickness and
20 depth, and considering the respective sensitivities, injection rates of 1000 t/d or greater are within a
21 realistic scope.

22 As an initial approximation the potential injection rate may be assumed proportional to the values
23 for permeability, aquifer thickness and injection pressure, which allows sensitivity to be determined
24 with just one simulation. This may not be strictly valid, and also depends on the characteristics of the
25 actual relative permeability function. In the analytical solution for example it is not included,
26 therefore injection rate increases more than proportionally with pressure.

27 This study is based on the assumption of single well injection. When injection is carried out with
28 multiple wells their pressure cones would intersect and reduce the usable injection overpressure.

29 The present assumption of an infinite extent aquifer is optimistic. When the extent of the aquifer is

1 limited, namely a reservoir, it will be necessary to install relief wells to avoid a rapid increase in
2 reservoir pressure and the decrease in usable injection overpressure. Both effects counteract the
3 increasing potential injection rate with time.

4

5 **8 Conclusions**

6 Injection rates were predicted and the sensitivities of different geological, technical and operational
7 parameters were determined with respect to achievable mass flow for single well CO₂ injection into a
8 saline aquifer. The relevance of the parameters is assessed by applying a reasonable parameter
9 range for the sensitivity function. The central point of the analysis was constructed to mimic
10 conditions at the Ketzin test site. For these conditions a mean injection rate $\overline{m}_{num,pp}$ of 178 t/day can
11 be achieved for power plant controlled injection.

12 The impact of the prediction method should be considered. The analytical solution provides the most
13 optimistic prediction for both injection rates and temporal behaviour, while the numerical simulation
14 with a power plant controlled injection rate provides the most realistic behaviour, but with the
15 smallest mean rate and the highest temporal variability of the annual mean injection rate. These
16 effects may add up to a difference in the rate factor of 1.45.

17 Injection rates are nearly proportional to aquifer permeability, which is the most important
18 influencing factor due to its high variability. Aquifer thickness also shows linear sensitivity, resulting
19 in considerable impact. The sensitivity of aquifer depth between 1000 m and 2000 m equals a factor
20 of 2.5. This is a combined effect resulting from different CO₂ and brine properties due to changing
21 temperatures and hydrostatic pressures, but the depth dependent increase in the feasible injection
22 pressure is more important.

23 Rock compressibility shows a moderate sensitivity and may increase injection rates for highly
24 compressible aquifers by about one third. It is of minor importance to consider vertical anisotropy,
25 pore pressure and hysteresis, as their impact on injection rate is each less than 5 %. The insensitivity
26 of anisotropy shows again that the system is dominated by horizontal flux and that buoyancy effects
27 are negligible.

28 During the initial phase the reservoir reacts sensitively to variations in the injection rate. During this
29 phase the rate should be held constant in order to avoid large pressure variations and to ensure that

1 the reservoir contains enough mass of CO₂ to effectively dampen rate variations at a later time. In
 2 the current example, for one year and later, the injection rate may be increased by just 8 % if all rate
 3 variations could be levelled out. This implies that a transient injection regime allows periods with
 4 injection rates above the mean. For the applied realistic power plant CO₂ load curve the peak rate
 5 may be 29 % higher than the mean and 19 % above the pressure controlled rate. The borehole
 6 diameter has a minor impact. Within a reasonable range of between 5 cm and 21.6 cm the well
 7 diameter has an impact of less than 4%.

8 The study shows that injection rates depend mainly on the geological setting and the analysed
 9 technical measures have only a slight impact. However, the interaction of multiple wells, which may
 10 considerably affect the potential injection rate, are not taken into account.

11

12 **9 Nomenclature**

13 A [-] vertical aquifer anisotropy

14 a [-] capillary pressure parameter

15 b [-] capillary pressure parameter

16 d [cm] well diameter

17 $k_{r,i}$ [-] relative permeability, for i as CO₂/Brine

18 n_i [-] Corey parameter, for i as CO₂/Brine

19 h [m] aquifer thickness

20 K [mD] aquifer permeability

21 $\dot{m}_i(t)$ [t/d] actual injection rate, with i =num,cp: numerical constant pressure injection, i =num,pp:
 22 numerical, power plant controlled, i =a,cp analytical, constant pressure injection

23 \bar{m}_i [t/d] mean injection rate for entire period with i =num,cp: numerical constant pressure injection,
 24 i =num,pp: numerical, power plant controlled, i =a,cp analytical, constant pressure injection

25 $\bar{m}_{num,pp}(t)$ [t/d] mean mass injection rate for power plant controlled injection, determined for a one
 26 year interval beginning with time t .

27 n [-] capillary pressure parameter

28 p [bar] injection overpressure (above hydrostatic pressure)

29 p_c [Pa] capillary pressure

30 r_w [m] well radius

31 r_m [m] model radius

32 S [1/bar] rock compressibility

33 S_i [-] saturation, for i as CO₂/Brine

34 $S_{i,residual}^j$ [-] residual saturation with i as the phase CO₂/Brine and j as drainage/imbibition

35 t [d] time

36 ϕ [-] aquifer porosity

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1 **12 Tables**

2

3 **Table 1:** Corey parameters for CO₂ and brine for drainage and imbibition.

Corey parameters	CO ₂	Brine
n	1.5	5.5
$S_{r,imb}^i$	0.3	0.15
$S_{r,dm}^i$	$S_{r,dm}^{CO_2} = 0.05$ $S_{r,dm}^{bri} = 0.05$	0.15

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1 **Table 2: Aquifer parameters at the Ketzin test site and corresponding values at the central point.**

	Ketzin	Central point of sensitivity study
Well diameter, r_w	21.59 cm	21.59 cm
Permeability, K	40-110 mD	100 mD
Porosity, ϕ	0.26	0.26
Relative permeability, $k_{r,co2}, k_{r,brine}$	Schepernisse and Maas (2009)	Figure 2
Capillary pressure p_c	Schepernisse and Maas (2009)	Equation 2
Aquifer thickness h	12 m	12 m
Anisotropy A	3	10
Extent r_m	Unknown	Quasi infinite (100 km radius)
Temperature gradient	3.7 °C/100m	3.5 °C/100m
Vertical pressure gradient	1.1 bar/10m	1.1 bar/10m
Depth	642 m	1000 m
Salinity	24 w/w%	20 w/w%
Injection regime	Variable	Pressure controlled
Max. injection overpressure p	22.9 bar	20 bar

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1 **Table 3: Model parameters for the central point and variation.**

Parameters	Central point of sensitivity study	Scenarios
Discretisation (inner cells)	1 m	0.1 m, 0.5 m, 5 m
Model extent (radius), r_m	100 km	10 km, 1000 km
Well diameter, d	21.59 cm	5 cm, 10 cm
Permeability, K	100 mD	10 mD, 1000 mD
Hysteresis	Not applied	See Figure 2 and Equation 2
Aquifer thickness h	12 m	6 m, 24 m
Anisotropy, A	10	1, 1000
Depth	1000 m	650 m, 2000 m
Rock compressibility, S	$7.2 \cdot 10^{-5} \text{ bar}^{-1}$	None, $7.2 \cdot 10^{-6} \text{ bar}^{-1}$, $7.2 \cdot 10^{-4} \text{ bar}^{-1}$
Max. injection overpressure p	20 bar	1 bar, 40 bar
Injection regime	Pressure controlled	Power plant load curve controlled

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- 1 **Table 4: Sensitivities of model parameters. The central point parameters from Table 3 are applied. The injection rate as a function of the sensitivity is calculated by**
- 2 **multiplication of the injection rate at the central point with the respective sensitivity term. The sensitivity term is the product of all sensitivities. The scale of the values**
- 3 **is presented in the right two columns.**

Input parameter	Min Max	Output rate [t/d]	Numerical Evaluation Linear Sensitivity	Numerical Evaluation Nonlinear Sensitivity	Analytical Evaluation Linear Sensitivity	Analytical Evaluation Nonlinear Sensitivity	Injection regime	Value range numeric/analytic	
Pressure p	0 40	$\bar{m}(p)$	$\bar{m}_{num,cp} 0.0536 p$	$\bar{m}_{num,cp} 0.0453 p^{1.04}$	$\bar{m}_{a,cp} 0.0542 p$	$\bar{m}_{a,cp} 0.0313 p^{1.158}$	pressure controlled	0 2.14	0 2.25
	0 40		$\bar{m}_{num,pp} 0.0523 p$	$\bar{m}_{num,pp} 0.0396 p^{1.08}$	-	-	power plant controlled	0 2.12	
Time t	1 7300	$\dot{m}(t)$	-	$\bar{m}_{num,cp} 0.8475 t^{0.0209}$	-	$\bar{m}_{a,cp} 1.071 t^{-0.0089}$	pressure controlled	0.85 1.02	0.99 1.06
	365 7300		-	$\bar{m}_{num,pp} \left(0.809 - \frac{20.8}{t} + 0.0251 \ln(t) \right)$	-	-	power plant controlled	0.9 1.03	
Well Diameter d	5 21.59	$\bar{m}(d)$	$\bar{m}_{num,cp} \left(\frac{0.955 +}{2.13 \cdot 10^{-3} d} \right)$	$\bar{m}_{num,cp} 0.925 d^{0.0255}$	$\bar{m}_{a,cp} \left(\frac{0.001356 +}{0.971 d} \right)$	$\bar{m}_{a,cp} 0.951 d^{0.016}$	pressure controlled	0.96 1	0.98 1
Depth D	650 2000	$\bar{m}(D)$	$\bar{m}_{num,cp} \left(\frac{0.501 +}{4.62 \cdot 10^{-4} D} \right)$	$\bar{m}_{num,cp} 0.0258 D^{0.528}$	$\bar{m}_{a,cp} \left(\frac{6.98 \cdot 10^{-4} +}{0.1003 D} \right)$	$\bar{m}_{a,cp} 2.68(632-D)^{0.29}$	pressure controlled	0.79 1.43	0.42 1.46
Permeability K	10 1000	$\bar{m}(K)$	$\bar{m}_{num,cp} 0.0102 K$	-	$\bar{m}_{a,cp} 0.0097 K$	$\bar{m}_{a,cp} 0.0105 K^{0.9885}$	pressure controlled	0.1 10.2	0.1 9.7
Aquifer thickness h	6 24	$\bar{m}(h)$	$\bar{m}_{num,cp} 0.0842 h$	-	$\bar{m}_{a,cp} 0.0833 h$	-	pressure controlled	0.51 2.02	0.5 2
Anisotropy A	1 1000	$\bar{m}(A)$	-	$\bar{m}_{num,cp} 1.03 A^{-0.0118}$	-	-	pressure controlled	1.03 0.95	
Rock compressibility S	0 $7.2 \cdot 10^{-4}$	$\bar{m}(S)$	$\bar{m}_{num,cp} \left(\frac{0.913 +}{549 S} \right)$	$\bar{m}_{num,cp} (0.885 + 76.7 S^{0.705})$	$\bar{m}_{a,cp} \left(\frac{0.889 +}{827.7 S} \right)$	$\bar{m}_{a,cp} (0.821 + 44.77 S^{0.579})$	pressure controlled	0.89 1.35	0.87 1.5

13 Figures

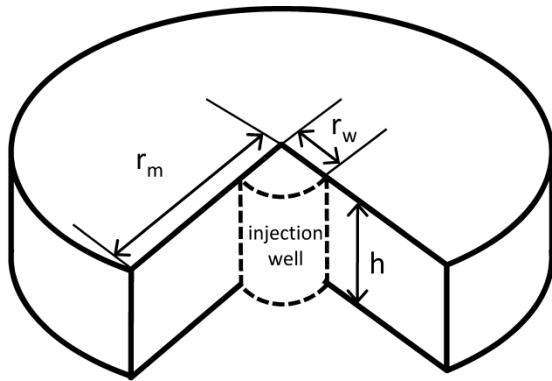
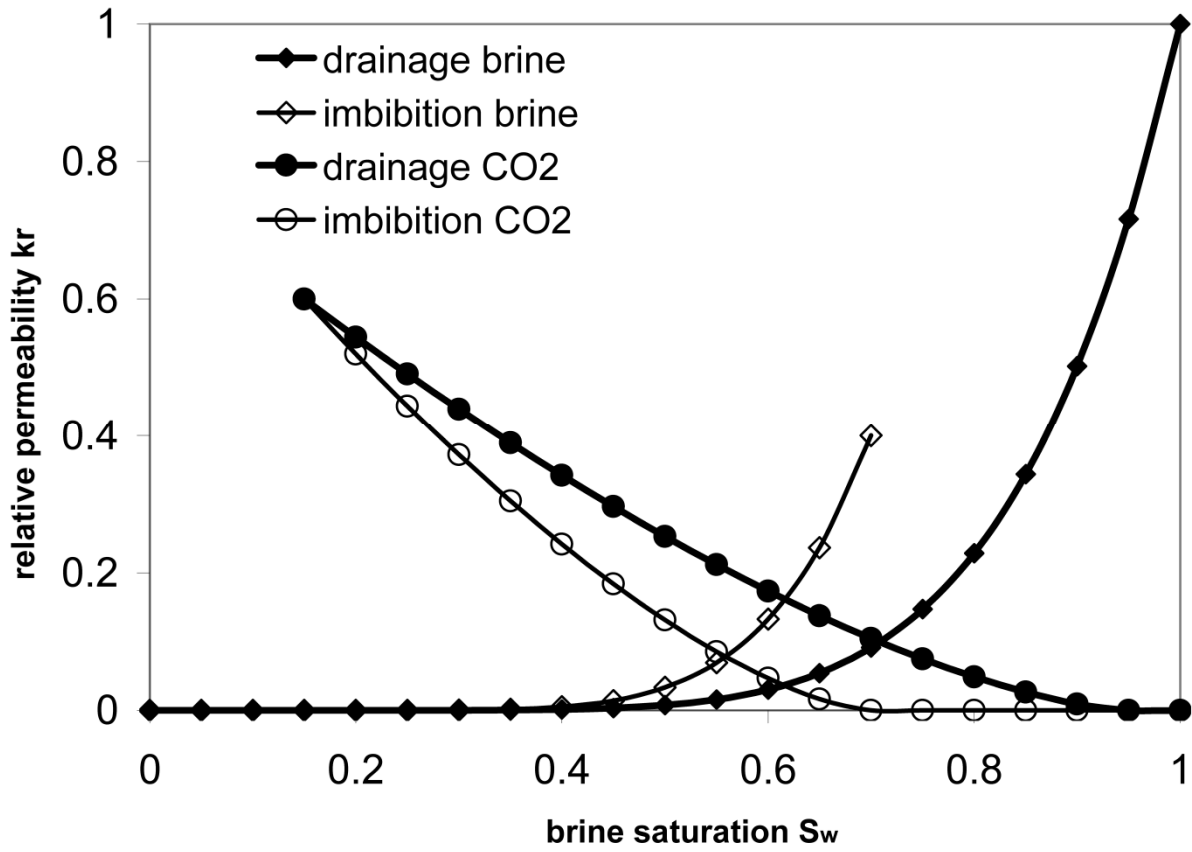
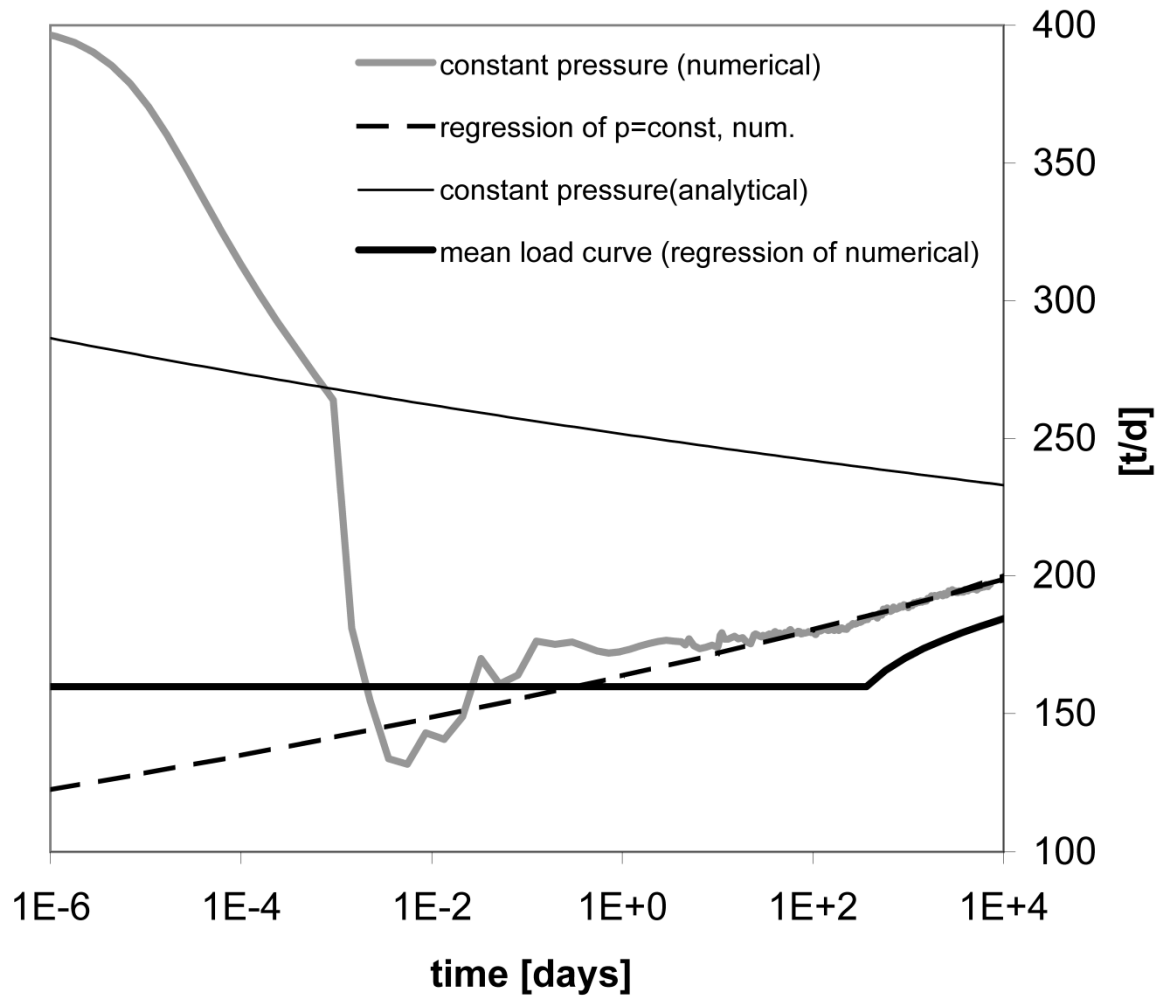


Fig. 1. Model domain of the numerical models. The model is 2-D radially symmetric, r_w is the radius of the injection well, r_m the radius of the model domain, h denotes the thickness of the aquifer. Except for the injection well all boundaries are no flow.



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2 Fig. 2. Relative permeabilities of brine and CO₂. Residual brine saturation is 15%.



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2 Fig. 3. Temporal injection rate at the central point, calculated with the numerical model and
 3 the analytical solution. The regression function corresponds to the numerical model.

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