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Fault parameters-based earthquake magnitude estimation using Artificial Neural Networks

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Abstract

In this study, a computer-aided methodology is proposed to estimate the earthquake magnitude based on fault parameters. So far, log-linear regression equations are separately employed for each fault parameter. However, this can lead to inconsistent magnitude predictions because non-linear parameter correlations are ignored and those parametric functions cannot take into account potential deviations from log-linear scaling. In order to address the aforementioned deficiencies, we employ Artificial Neural Network (ANN) to estimate the magnitude of earthquakes simultaneously using all available fault parameters such as rupture length and width, thereby excluding the chances of inconsistent estimations. Our evaluation of $M \geq 5$ earthquakes shows that the predictions from the proposed methodology outperform the regression equation-based predictions in terms of mean absolute error and root mean square error. Furthermore, the pictorial view of the performance also demonstrates the strength of ANN to identify and reproduce, without any initial assumption, systematic deviations from the log-linear scaling of earthquake magnitudes as a function of the fault parameters.

Keywords: Fault parameters, Artificial Neural Network, Earthquake magnitude estimation, Seismic hazard Assessment

34 **Introduction**

35 Seismic hazard assessments rely on estimates of the maximum possible magnitude (M_{\max}) of
36 earthquakes. However, instrumental earthquake catalogs are usually too short to cover full
37 seismic cycles and thus do not include the largest possible events. Therefore, geologically
38 mapped faults or paleo-earthquake studies are often used to estimate M_{\max} . For that purpose, the
39 relation between the earthquake magnitude (M , hereinafter refers to the moment magnitude) and
40 fault parameters, such as rupture length (L), rupture width (W), area (A), and slip must be
41 known.

42 In theory, the moment magnitude is simply a function of the shear modulus, the mean slip, and
43 the rupture area. However, the average earthquake slip on the rupture area is usually not known
44 and empirical estimations based only on the rupture dimensions might differ significantly from
45 the true value. Many authors proposed empirical scaling relationships between seismic moment
46 and fault area (Thatcher and Hanks 1973, Kanamori and Anderson 1975, Kanamori 1977) and
47 fault length or width (Scholz 1982, Romanowicz 1992, Romanowicz and Rundle 1993). Previous
48 research studies used regression analysis to develop such empirical relationships between fault
49 rupture parameters and magnitude for large worldwide historic earthquakes (Wells and
50 Coppersmith 1994, Mai and Beroza 2000, Henry and Das 2001, Leonard 2010). Currently, the
51 empirical relations of Wells and Coppersmith (1994) (WC-94) are commonly employed to
52 estimate earthquake magnitudes, but these relations are not self-consistent because the regression
53 equations for the earthquake magnitude are estimated independently for the different fault
54 parameters, which limit their applicability.

55 It is also noted that data for many recent large earthquakes were missing during the time of the
56 aforementioned studies. Furthermore, the conventional methodologies based on regression

57 equations cannot account for non-linear correlations between the rupture parameters. For a given
58 fault parameter (e.g. L), these regression equations simply predict one magnitude value
59 independently of the values of the other fault parameters (e.g. W) and the observed deviations
60 are taken as random fluctuations. Figure 1 shows the fit of the WC-94 regression equation to
61 actual earthquake magnitudes as function of L . The data set used in Figure 1 consists of the
62 combined WC-94 and SRCMOD data sets described in Section 2. The predictions simply follow
63 a line, while true values widely scatter around it with some systematic trends. For example, the
64 WC-94 regression equation fails to correctly predict magnitudes $M \geq 8.0$, thus underestimating
65 the seismic hazard in that range. In order to improve hazard estimations, a methodology capable
66 of incorporating the non-linear dependence of earthquake magnitudes on fault parameters is
67 highly desirable. We investigate the application of intelligent computing algorithms as one
68 solution to this problem.

69 Machine learning is a branch of computer science that has the ability to identify and extract
70 meaningful, hidden relations from data. These learned relations are then used to make
71 predictions for unseen data (Reyes, et al. 2013). In the recent past, the use of machine learning
72 techniques in the field of seismology and earth sciences has increased (Asim, et al. 2017, Asim,
73 et al. 2018, Rouet-Leduc, et al. 2017, DeVries, et al. 2018, Bergen, et al. 2019, Asencio-Cortés,
74 et al. 2016, Morales-Esteban, et al. 2013, Tareen, et al. 2019). This interdisciplinary approach
75 has already provided new insights and increased predictability for different challenging data sets
76 (Kong, et al. 2018). In this paper, we test its applicability to the problem of magnitude estimation
77 based on sets of fault parameters. In particular, we employ Artificial Neural Network (ANN) for
78 the mapping between fault parameters and the corresponding earthquake magnitude. We split the
79 collected earthquake data, consisting of historical and instrumental earthquakes compiled by

80 Wells and Coppersmith (1994) and the finite-source rupture model database SRCMOD (see
81 Section 2), into training and test data, showing that the proposed methodology provides
82 improved, robust, and self-consistent estimations of earthquake magnitude by simultaneously
83 taking into account the knowledge of all available fault parameters.

84 The analysis is divided into two parts. In Section 3.1, we estimate the magnitude of the target
85 events by means of the regression equation proposed by Wells and Coppersmith (1994). Here we
86 also analyze regression equations which are recomputed based on the new and increased data
87 collection including many events occurred after 1993. In Section 3.2, Artificial Neural Network
88 (ANN) is developed for training data and tested for unseen data. The results are then discussed
89 and compared to the conventional regression-based methodologies in Section 4.

90 **Earthquake Data**

91 We analyze data from past earthquakes with magnitude $M \geq 5.0$, which are collected from both
92 the WC-94 catalog and SRCMOD database.

93 ***WC-94 Catalog:***

94 The WC-94 catalog of past large earthquakes was compiled by Wells and Coppersmith (1994).
95 In this publication, a total of 244 events, which occurred until 1993, are listed with mixed focal
96 mechanisms consisting of both strike-slip and dip-slip earthquakes. The fault parameters of these
97 events were estimated either by paleoseismological and seismological studies, aftershock
98 distributions, or geodetic modeling of surface deformations. We selected those events from the
99 catalog which have both fault length L and width W information. If both subsurface and surface
100 rupture lengths were provided for a single event, we chose the subsurface length. Our selection

101 criterion yields a total of 180 earthquake ruptures with $M \geq 5.0$ for our analysis. Out of these
102 cases, 95 include information about the maximum slip of the rupture (See Table S1(a)).

103 ***SRCMOD Database:***

104 A data set consisting of more recent earthquakes is maintained by Martin Mai and his colleagues.
105 The SRCMOD database collects finite-source rupture models (<http://equake-rc.info/SRCMOD/searchmodels/allevnts/>) (Last accessed on April 10, 2019), which are
106 delivered by different research teams. These slip models are obtained from the inversion of
107 seismic, geodetic, tsunami and other geophysical techniques with variable resolutions. At the
108 time of our access, the SRCMOD database contained 347 slip models for a total of 178 different
109 earthquakes. Because of their limited resolution, we excluded slip models which were solely
110 derived from tsunami data. The remaining 316 slip models are used in our analysis, after
111 exclusion of $M < 5.0$ earthquakes. For each case, the dimensions of the fault planes on which the
112 slip had been inverted are provided in the SRCMOD database. However, the dimension for the
113 inversion can be much larger than the actual dimension of the earthquake slip region. Therefore,
114 each model and its associated fault parameters were manually inspected (see Table S1(b)). As an
115 example, the slip model of Motagh, et al. (2010) for the 2007 M7.8 Tocopilla earthquake shows
116 significant slip only in a discrete part of the assumed fault plane, which is 349 km long and 180
117 km wide. The recomputed rupture length and width of the actual slip area are 270 km and 110
118 km, respectively, reducing the area by a factor of approximately two in this case. Note that we
119 calculate the rupture area simply by the product of L and W.
120

121 **Research Methodology**

122 To relate fault parameters to earthquake magnitudes, we firstly employ the traditional
123 regression-based methodology and then apply the new ANN-based approach. This allows us to
124 properly compare the results of both approaches in terms of consistency, accuracy and
125 robustness.

126 ***Regression Analysis***

127 Regression analysis is carried out to derive log-linear relations between fault parameters and
128 earthquake magnitudes. However, these relations are separately derived for each individual fault
129 parameter, i.e. independent regression equations relating either L or W to the earthquake
130 magnitude are obtained. In this regard, the regression equations of Wells and Coppersmith
131 (1994) are widely used, which were derived for the WC-94 data set (including all mechanisms)
132 as follows:

$$133 \quad M = 4.38 + 1.49 \log(L) \quad (1)$$

$$134 \quad M = 4.06 + 2.25 \log(W) \quad (2)$$

135
136 To take advantage of the extended data set, we also perform our own regressions for the
137 combined WC-94 and SRCMOD data collection described in Section 2. Our derived new
138 empirical relations between M, L and M, W, respectively, are given by

$$139 \quad M = 4.33 + 1.57 \log(L) \quad (3)$$

$$140 \quad M = 4.7 + 1.7 \log(W) \quad (4)$$

141 Figure 2 shows the fit of these regression lines to the empirical earthquake data.

142 *Artificial Neural Networks*

143 Artificial Neural Networks (ANN) are inspired from biological neural networks consisting of
144 neurons and weighted connections between different layers of neurons (Hassoun 1995).
145 Earthquake magnitude estimation using fault features is treated as a regression problem and
146 solved using ANN. The network is trained on a part of the known data by providing fault
147 features on the input layer and the corresponding actual earthquake magnitudes on the output
148 layer. The input layer leads to the hidden layer through weighted connections and is further
149 passed to the output neurons. The weights of connections in neurons are either excitatory or
150 inhibitory. An output value is received at the output neuron through the processing of fault
151 parameters. The error between the value received at the output neurons and the actual earthquake
152 magnitude is then calculated and propagated backwards in order to adjust and tune the weighted
153 connections accordingly. This process of adjusting connection weights based upon known data is
154 called “learning”. The explained topology of ANN is called feed forward neural network and the
155 learning process is referred as back propagation.

156 The number of input neurons is equal to the number of fault parameters provided as input. In
157 regression problems, only a single neuron is kept in the output layer. In addition to the input and
158 output layers, a single hidden layer is used. In this case, we chose seven neurons in the hidden
159 layer based upon performance during training and cross-validation. As activation function, we
160 used tan-sigmoid,

$$161 \quad f(x) = \tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}, \quad (5)$$

162 which is widely used as an activation function in shallow neural networks. We also found that it
163 performs better than linear and sigmoid activation functions in our case.

164 The trained ANN model maps the given set of fault parameters, such as L, W, A, and maximum
165 slip S (if available) to the actual earthquake magnitude in an optimized way and is then capable
166 to predict the earthquake magnitude for unseen data. In other words, ANN learns from the
167 known available data and develops a relation between potential inputs (fault parameters) and
168 corresponding output (earthquake magnitude).

169 In this paper, we use two different sets of fault input data for the ANN approach. In the first
170 scenario, we restrict the fault parameter set to the geometrical values, namely L, W and the
171 rupture area (L-W-A). In practical applications, only L-W-A might be available, while the
172 maximum slip value is often not known. However, we also developed a second ANN model
173 simultaneously utilizing all fault parameters including maximum slip (L-W-A-S). Although the
174 second scenario might have fewer applications for hazard assessment, it is interesting to evaluate
175 and compare the overall prediction performance of ANN for both cases, because such a
176 comparison can highlight the information gain due to additional input values. However, for the
177 comparison of our ANN model results with conventional regression results, we concentrate on
178 the L-W-A approach as the most practical one.

179 In order to assess the performance of ANN, we predict earthquake magnitudes from the test data.
180 Only a portion of the available data set (training data set) is fed to ANN for learning and
181 predictions are obtained for unseen data (test data set). In this study, a cross validation strategy is
182 employed to test the ANN predictions on the combined WC-94 and SRCMOD data set. The k -
183 fold cross validation approach is widely applied in demonstrating the performance of
184 classification and regression techniques (Wong 2015). In particular, it is expected to capture the
185 general properties in cases of limited data samples. We choose the specific value of $k=10$, i.e. a
186 10-fold cross-validation (Idris, et al. 2017). In this procedure, we divided the entire data set into

187 10 non-overlapping subsets. One of these 10 subsets was reserved for independent standalone
 188 testing, while the remaining 9 subsets were used for model training. We repeated the process
 189 until all 10 subsets were separately employed once for testing. Therefore, we trained 10 different
 190 ANN models separately and obtained earthquake magnitude predictions for every sample
 191 available in the data set.

192 **Results and discussion**

193 In the following, we describe the results of the new ANN method and compare them with those
 194 obtained by the conventional methodologies to demonstrate that the computer-aided technique
 195 has the potential to improve seismic hazard assessments, especially magnitude predictions based
 196 on fault parameters.

197 The performance of the magnitude estimation is expressed using the Mean Absolute Error
 198 (MAE) and the Root Mean Square Error (RMSE). These errors are computed between actual and
 199 estimated magnitudes for the test data sets to quantify the overall performance of the ANN. In
 200 contrast, for the conventional regression equations, the errors are calculated partly (WC-94
 201 relations) or fully (Eqs.3,4) for the same data for which the models have been developed. The
 202 calculated errors are defined as:

$$203 \quad MAE = \frac{\sum_{i=1}^n |M_{Predicted_i} - M_{Actual_i}|}{n} \quad (6)$$

$$204 \quad RMSE = \sqrt{MSE} = \sqrt{\frac{\sum_{i=1}^n (M_{Predicted_i} - M_{Actual_i})^2}{n}} \quad (7)$$

205 Below we show that the proposed ANN-based estimates are superior to the regression-based
 206 magnitude estimations with respect to consistency and performance.

207 ***Self-consistency of ANN-based methodology***

208 Regression relations, as presented in Eq. 1-4, determine the earthquake magnitude as function of
209 a single fault parameter, i.e. L or W in this case. A major issue in such approaches is the lack of
210 self-consistency. Regression relations tend to yield different magnitude estimations for the same
211 earthquake if either the regression equation for L or W is used. For example, for our data set, the
212 RMSE-value of the difference $M(L_i) - M(W_i)$ is $RMSE = 0.221$ for the WC-94 and $RMSE =$
213 0.162 for the new regression equations, respectively. However, in the proposed ANN-based
214 approach, all given fault parameters are employed simultaneously to estimate the earthquake
215 magnitude. The simultaneous use of all fault parameters eschews different magnitude estimations
216 for the same sample, thereby providing a self-consistent earthquake magnitude estimation
217 methodology by taking potential non-linear parameter correlations into account.

218 Table 1 demonstrates once more the inconsistency of regression equation-based estimations,
219 which show different errors for the equations based on L and W. On the contrary, a trained ANN
220 simultaneously takes all given fault parameters into account and provides a single prediction.

221 ***Performance of ANN-based methodology***

222 The individual magnitude predictions of the ANN-model and the regression equations for the
223 whole data set are provided in the supplementary material (Please see Tables S2(a), S2(b)). A
224 summary of the model performance is provided in Figure 3 in terms of histograms of the
225 residuals and in Table 1 in terms of RMSE and MAE, computed between predicted magnitudes
226 and actual earthquake magnitudes. The results for the test data sets highlight the robustness of
227 ANN-based predictions, demonstrating that ANN has the ability to show decent performance
228 across the whole data set.

229 It is evident from Figure 3 and Table 1 that the L-W-A scenario leads to significantly decreased
230 errors compared to the regression equations. The availability of the maximum slip value S in
231 addition to L , W and A further improves the results of the ANN-approach in terms of RMSE and
232 MAE. Figure 4 shows scatter plots of the actual earthquake magnitudes and ANN-based
233 predictions. We detect systematic deviations from the exponential relations assumed in the
234 regression equations. The model clearly depicts the noticeable scale breaks in the relations
235 between M , L and M , W . For $L \leq 80$ km, the magnitudes scale approximately linearly with the
236 logarithm of length. However, between 80 and 180 km, the slope becomes smaller, then
237 increases again for $L \geq 180$ km (corresponding to $M \geq 7.7$). A quite similar behavior is observed for
238 the dependence of magnitude on fault width. The ANN-predictions reproduces the two observed
239 kinks in the scaling at rupture widths of approximately 25 km and 100 km.

240 We also analyzed the results of the ANN with respect to the predictions for different rupture
241 mechanisms. In Figure 5, the results are separately shown for the strike-slip and dip-slip events
242 in the data set. The general trend of both rupture types is well reproduced. However, some
243 outliers with magnitudes significantly higher than the average value for the given rupture length
244 are observable in the case of strike-slip events. Earthquakes with largely erroneous predictions
245 (encircled in Figure 5a) are mostly related to historical earthquakes in the WC-94 catalog, in
246 particular those which lack subsurface length information. Another example is the 1920 Ms8.5
247 Gansu, China, earthquake, one of two strike-slip earthquakes with magnitude >8.0 in the data set.
248 The largest strike-slip event is the 2012 M8.7 Sumatra intra-plate earthquake. Besides the
249 missing subsurface length information for the Gansu event, the erroneous prediction of the two
250 largest events can be explained by the fact that both events can be rarely seen as a single fault
251 rupture, because they ruptured several subfaults (Huan, et al. 1992). In particular, the Sumatra

252 event consisted of an extraordinarily complex four-fault rupture lasting about 160 seconds (Yue,
253 et al. 2012).

254 The quality, quantity and diversity of data hold crucial importance in training an ANN model.
255 Larger and diversified data sets lead to a better trained model with robust prediction capabilities
256 (Krizhevsky, et al. 2012). The catalog employed in this study contains earthquakes with
257 magnitudes ranging from a minimum magnitude of 5.0 to a maximum of 9.1. However, the
258 catalog is skewed towards higher magnitudes and has fewer events of low magnitudes. The
259 abundant presence of a particular data class in the training set forces the ANN to better fit this
260 class. Therefore, the model is able to identify that class over unseen data with higher accuracy. In
261 our earthquake catalog (provided in the supplementary material), a varying number of samples
262 are present in different magnitude classes. We define different ranges for earthquake magnitudes
263 and analyze the performance of predictions as function of the sample size in the magnitude bins.
264 The result in terms of MAE (Willmott and Matsuura 2005) is provided in Table 2. The MAE is
265 highest for the least abundant magnitude class, while it decreases with increasing number of
266 instances for a class. Thus, the result is in agreement with the expected relation to the sample
267 size in each class. It also verifies the need of data diversity for an improved training of the
268 machine learning model.

269 When an ANN is initialized, random weights are assigned to the connections between layers of
270 neurons. During the learning process, the neurons continually adjust the connection weights until
271 the model's performance reaches a maximum. It is noted that the sufficiency of training data and
272 random initialization also play an important role in the performance of trained models. The
273 performance of ANN may vary in different simulations if the training data set is not available in
274 sufficient quantity. Therefore, it is important to analyze the robustness of the proposed

275 methodology concerning the random initialization. For this purpose, we have carried out 10
276 independent simulation runs and the performance of every run is measured by the MAE-value
277 (Asim, et al. 2018). We found that the MAE-value only varied by 1%, demonstrating the
278 robustness of our ANN-model (See Table S3).

279 The performance of ANN has been compared to another well-known machine learning
280 technique, namely the Random Forest (RF) method. RF is a decision-tree based algorithm, which
281 provides an ensembled outcome of multiple decision-trees (Breiman 2001). We found that RF
282 performs better than the regression equations in estimating earthquake magnitude in the case of
283 the L-W-A-S scenario, but it is outperformed by ANN in all cases.

284 For practical applications of our proposed techniques, researchers can follow two different
285 approaches: (a) They can use the ANN-model trained on our data set; or (b) they can run new
286 simulation on updated data sets. Both options can be employed according to the feasibility of the
287 potential users/researchers. The codes developed for this research study are shared publicly for
288 the use of research community (available on: <https://doi.org/10.6084/m9.figshare.8010608>). The
289 codes are developed in MATLAB and require neural network toolbox for successful execution.

290

291 **Conclusion**

292 We propose a new technique based on ANN for estimating the earthquake magnitude based on
293 given fault information. This is often needed to relate geological fault information to potential
294 maximum earthquake magnitudes for seismic hazard estimations. The ability of ANN to identify
295 hidden patterns in data and its simultaneous use of fault parameters ensures the consistency of
296 the approach. Our analysis of the predictions based on the parameters describing the geometrical
297 dimension of faults (L, W, A) show a clearly improved performance in comparison to

298 conventional regression methods. The proposed method has also the ability to simply integrate
299 additional fault information in a consistent way. The addition of the maximum slip has been
300 shown to further improve these estimations, thereby encouraging the use of additional fault
301 parameters such as fault dip and rake in the future.

302 **Data and Resources**

303 The earthquake catalogs used in this research are taken from the Wells and Coopersmith (1994)
304 and SRCMOD databases (<http://equake-rc.info/SRCMOD/searchmodels/allevnts/>) (Last
305 accessed on April 10, 2019). These data are also available in Table S1. The details regarding
306 usage of data are explained in Section “Earthquake Data”.

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379

380 List of Figure Captions

381 Figure 1: Earthquake magnitudes versus rupture length: Black triangles refer to the actual
382 magnitudes, whereas red circles represent the predicted magnitudes from the regression equation
383 of Wells & Coppersmith (1994).

384

385 Figure 2: Earthquake magnitude versus (a) rupture length and (b) rupture width: Symbols refer to
386 observed values, while lines represent the regression lines (predicted values).

387

388 Figure 3: Histogram comparison of residuals from our ANN methodology for the L-W-A
389 scenario with WC-94 regression equations (WC-L, WC-W) and new regression equations (New-
390 L, New-W)

391

392 Figure 4: Actual and predicted earthquake magnitudes plotted against (a) length, (b) width for
393 the case of the L-W-A scenario, while (c, d) show the same results for the L-W-A-S scenario.

394

395 Figure 5: (a) Scatterplot of actual and predicted earthquake magnitudes as function of fault
396 length for (a) strike-slip and (b) dip-slip events in the case of the L-W-A scenario.

397

398

399 Table 1: Performance of ANN earthquake magnitude estimations for the whole earthquake data
400 set acquired through 10-fold cross-validation.

Performance Measure	ANN		Regression Methods			
	L-W-A	L-W-A-S	L (WC-94)	W (WC-94)	L (new)	W (new)
RMSE	0.303	0.288	0.372	0.593	0.356	0.518
MAE	0.239	0.229	0.293	0.463	0.282	0.407

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403 Table 2: Prediction quality for different available magnitude ranges in the earthquake data set.

Earthquake Magnitude Range	L-W-A		L-W-A-S	
	No. of Instances	MAE	No. of Instances	MAE
[5.0, 6.0)	77	0.242	32	0.258
[6.0, 7.0)	161	0.230	132	0.222
[7.0, 8.0)	187	0.228	176	0.220
>8.0	71	0.286	72	0.238

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