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## Highlights

State of stress and stress rotations: Quantifying the role of surface topography and subsurface density contrasts in magmatic rift zones (Eastern Rift, Africa)

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- Surface topography influences shallow stress localization
- Subsurface density contrasts influences lower crustal stress localization
- Topography, subsurface, and extension can produce local stress rotation
- Subsurface stresses are important in complete spatial understanding of rift tectonics

# State of stress and stress rotations: Quantifying the role of surface topography and subsurface density contrasts in magmatic rift zones (Eastern Rift, Africa)

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## Abstract

In rift settings, the crustal stress field is dominated by extension, which leads to rift-parallel topography and basin alignments. However in some continental rift systems, some observables of the orientation of principal stresses show substantial deviations from these patterns. Such stress field rotations are currently poorly understood and could reflect the critical role of rift magmatism in the creation of topography, the plate state-of-stress, and volcanic and tectonic processes. Yet the role of magma intrusions, crustal thinning, and rift basin and flank topography on rift zone stress field rotations remain poorly quantified. The seismically- and volcanically-active Magadi-Natron-Manyara region of the East African Rift shows a 60° local stress field rotation with re-

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spect to regional extension. Here, we test the hypothesis that such rotation is due to the cumulative effects of surface and subsurface loads (lateral subsurface density contrasts). We use analytical and calibrated numerical models of magmatic rift zones to simulate lithospheric deformation in the presence of magma bodies, crustal thinning, and topography to quantify their effect on intrusions and fault kinematics in a rift setting. Our 3D static models of a weakly extended rift suggest that surface topography influences shallow stress localization, whereas subsurface density contrasts play a larger role in lower crustal stress localization. Both patterns suggest a preferred region for melt storage beneath the rift valley. We show that the interaction between topography, crustal thinning, extension, and a pressurized magma reservoir could generate principal stress orientations consistent with the local stress rotation observed from earthquake focal mechanisms. Our results demonstrate how rift topography and the geometry of crustal thinning can guide magmatism and strain localization, highlighting the need for a three-dimensional treatment of rift kinematics.

Keywords: rift, continental rifting, tectonics, stress, topography

## 1 1. Introduction

Continental rift zones are sites of intraplate stretching, commonly with
adiabatic decompression melting accompanying lithospheric thinning. Large
fault systems bound the rift and are segmented along the length of the rift,
with strain linkage by rift-oblique transfer faults and relay ramps (e.g., Acocella et al., 2005; Ebinger, 1989; Larsen, 1988; Tibaldi et al., 2020). Volcanoes and underlying crustal magma chambers cause fundamental changes

to the density and thermal structure, load the plates, and change the state 8 of stress within the crust and mantle lithosphere (e.g., Karlstrom et al., 9 2009). In magmatic regions, the local stress field induced by volcanic edifice 10 loading/unloading (e.g., Kervyn et al., 2009; Maccaferri et al., 2014) and/or 11 weak zones (e.g., Corti et al., 2004) then influence subsequent magma migra-12 tion and vent distribution (e.g., Karlstrom et al., 2009; Rivalta et al., 2019) 13 Generally, dike and fracture orientations are favored perpendicular to the 14 direction of the least compressive stress (e.g., Pollard, 1987; Sibson, 1985). 15 Although published two-dimensional models of loading on plates without in-16 plane regional stresses offer insight (e.g., Karlstrom et al., 2009), a critical 17 gap in understanding remains on how surface (e.g., volcanoes, rift flanks) and 18 subsurface intrusions (sills, dikes, magma chambers) combine with regional 19 stresses in rift zones. In this study, we aim to address this gap and comple-20 ment existing conceptual models of magmatic rift zone structural patterns 21 (e.g., Magee et al., 2016; Muirhead et al., 2015; Tibaldi et al., 2020). 22

We build analytical and numerical models of magmatic rift zones to simu-23 late lithospheric deformation in the presence of magma bodies to quantify the 24 interactions between surface and subsurface loading on intrusions and fault 25 kinematics in a rift setting. We use the open-source finite element modeling 26 package PyLith v2.2.1 (Aagaard et al., 2013, 2017a,b) to build two- (2D) and 27 three-dimensional (3D) physics-based static models, calibrated to analytical 28 stress models, to quantify the effects of loading on the crustal state of stress. 29 We probe how inclusions (subsurface volumes of density different than host 30 material, e.g., magmatic intrusions) and loads/excavations of different spa-31 tial scales guide local stress field rotation and strain localization to favor the 32

initiation of extensional faults, dikes, and eruptive centers oriented obliquely
to the regional extension direction (e.g., Ebinger, 1989; Acocella et al., 2005).
Our approach is two-fold: we first evaluate model sensitivities to topography
and subsurface density contrasts separately, and then we compare our models
with observed stress indicators (i.e., earthquake locations and focal mechanisms). The static elastic modeling approach allows us to consider each load
separately, and summatively.

#### 40 2. Tectonic Background

The Magadi-Natron-Manyara basins are located in the southernmost sec-41 tor of the magmatic Eastern rift (Fig. 1). The Natron basin, which contains 42 lavas and sedimentary strata dating to  $\sim 3$  Ma, developed in metasomatized 43 Archaean lithosphere, as confirmed by mantle xenoliths (Mana et al., 2015; 44 Aulbach et al., 2011; McHenry et al., 2011; Foster et al., 1997). The present-45 day Natron basin is a N-S trending half-graben bounded by a monocline to 46 the east, that formed during a major phase of faulting at  $\sim 1.2-1$  Ma when 47 the east-dipping Songo border fault developed within the original wider basin 48 (Foster et al., 1997; Muirhead et al., 2016). Gelai volcano formed at  $\sim 1$  Ma 49 whereas carbonatite volcano Oldoinyo Lengai ( $\sim 0.37$  Ma, OL, Fig. 1) post-50 dates the main phases of rift faulting and basaltic volcanism (Mana et al., 51 2015; Foster et al., 1997; Muirhead et al., 2015, 2016). The Naibor Soito 52 monogenetic cone field (NS, Fig. 1) lies between Oldoinyo Lengai and Gelai 53 (e.g., Weinstein et al., 2017; Dawson, 1992). 54

The region is an ideal place to quantify the different loading contributions on crustal state-of-stress because the 2013-2014 Continental Rift and Fluid-

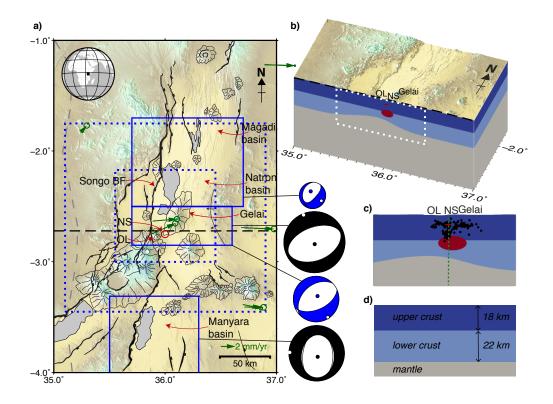


Figure 1: Study area and model geometry. a) Map of the Magadi-Natron-Manyara basins of the East African Rift system. Inset shows the location on the globe. Solid blue boxes enclose areas of seismicity analyzed by Weinstein et al. (2017) and the corresponding summed moment tensors (blue beachballs are from local focal mechanisms, black beachballs are from teleseismic focal mechanisms) that reveal along-axis local stress rotation. Green arrows are GNSS velocity vectors for a Nubia-fixed model with their error ellipses (King et al., 2019). Large dotted blue box describes the extent of the 3D model domain, with higher resolution topography (1 km) within the smaller dotted box (nodal spacing doubles at every step outward until the edge of the domain). The black dashed line represents the E-W transect at 2.72°S latitude which is used in the 2D models. Faults and edifices are from Muirhead et al. (2015). BF: border fault; NS: Naibor Soito; OL: Oldoinyo Lengai. b) Perspective figure looking northwest shows a section of the 3D model domain sliced along 2.72°S. The upper crust is dark blue, lower crust is light blue, mantle is gray, and the sill and magma chamber are red. c) Double-difference earthquake locations within 5 km north and south of the cross-section (dotted white box in b). Dashed green line  $(x = 2750 \text{ m}, \text{ where } x = 0 \text{ is } 36^{\circ} \text{ longitude})$  indicates the location of the 1D profile in Fig. 3. d) Reference model thicknesses.

Tectonic Interaction (CRAFTI) network (Weinstein et al., 2017), as well as 57 the recent Seismic and Infrasound Networks to study the volcano Oldoinyo 58 Lengai (SEISVOL) project in 2019-2020 (Reiss et al., 2021), provide excel-59 lent constraints for modeling. Nubia-fixed rigid plate models predict 2–5 60 mm/yr approximately E-W opening in the area (Saria et al., 2014; King 61 et al., 2019) (green arrows, Fig. 1). Receiver function studies show crustal 62 thinning from 40 km to 29 km in the middle of the rift valley (Plasman 63 et al., 2017). A velocity contrast at  $\sim 18$  km depth is interpreted from a 64 clear negative peak in receiver functions around 3 s, which is also evident in 65 the tomography (Plasman et al., 2017; Roecker et al., 2017). Seismicity and 66 tomography studies (from the regional CRAFTI network) image a magma 67 chamber and sill complex in the subsurface (Weinstein et al., 2017; Roecker 68 et al., 2017; Reiss et al., 2021). The local SEISVOL network allowed fur-69 ther detailed seismic studies and identified clusters beneath the Naibor Soito 70 volcanic field at 5–10 km depth interpreted as stress concentrations at the 71 edges of pressurized sills, and at 12-18 km depth representing the top of 72 the lower-crustal magma chamber, confirming that some seismicity patterns 73 observed in the earlier network are consistent over longer timescales (Reiss 74 et al., 2021). Focal mechanisms of both local and teleseismic earthquakes 75 reveal an along-axis local stress rotation of  $\sim 60^{\circ}$  in the OL-NS-Gelai com-76 plex ( $\sim$ N150°E extension), relative to the  $\sim$ E-W regional extension indicated 77 by seismic and geodetic data (Weinstein et al., 2017) (Fig. 1). Reiss et al. 78 (2021) report a mean T-axis direction of NW-SE in the OL-NS-Gelai area, 79 noting that beneath Naibor Soito, there was no dominant mechanism above 80 the magma chamber (below 13 km) and in the sill complex (5-7 km; 9-11)81

km). Instead, the local stress rotation (~N-S T-axes) was mainly observed at 82  $\sim$ 7–9 km depth. A detailed study of the variations in fault, dike, and cone 83 orientations in the East African Rift suggest that in different regions, dif-84 ferent stresses dominate: the regional stress state, magma overpressure and 85 volcanic edifice load, pre-existing structures, or local stress rotations due to 86 mechanical interactions of rift basin segments (Muirhead et al., 2015). A 87 separate study of East African Rift volcanoes hypothesized that rift-oblique 88 dikes and fissures were either due to lithospheric heterogeneities or mag-89 matic processes (Wadge et al., 2016). Since dikes are subvertical (e.g., Calais 90 et al., 2008; Muirhead et al., 2015; Weinstein et al., 2017), it is unlikely that 91 they reactivated Archaean and Pan-African strain fabrics that dip at an-92 gles  $\leq 45^{\circ}$  (e.g., Le Gall et al., 2008; Smith and Mosley, 1993), although the 93 pre-existing oblique fabric might influence later structures by lowering the 94 residual strength of the rock. 95

In June–August 2007, the Naibor Soito complex and the flanks of Gelai 96 were the site of 50+ 3.6  $< m_b < 5.9$  earthquakes and diking with associ-97 ated opening of 1.0-2.4 m, followed by eruption at Oldoinvo Lengai through 98 2008 (Baer et al., 2008; Biggs et al., 2009; Calais et al., 2008). During the 99 seismomagmatic sequence, 65% of the total geodetic moment release was at-100 tributed to dike opening, highlighting the importance of magma intrusions 101 in accommodating rift opening (Calais et al., 2008). New geophysical results 102 reinterpret the 2007 diking event to have occurred above a shallow sill com-103 plex underlain by a low-velocity mid-crustal magma mush (Oliva et al., 2019; 104 Roecker et al., 2017; Weinstein et al., 2017). 105

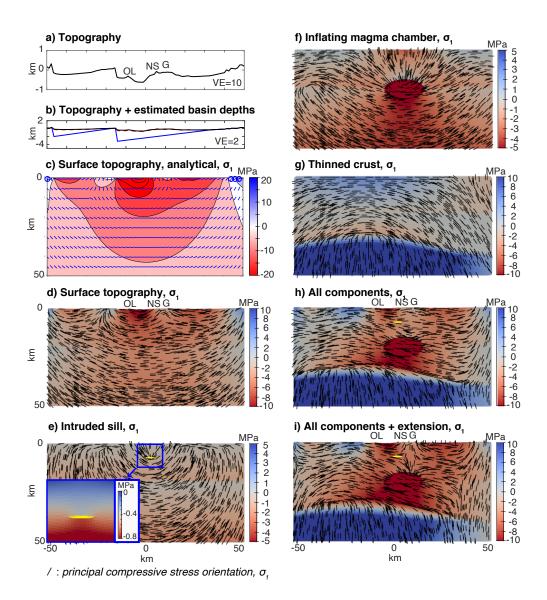


Figure 2: Two-dimensional static model results. Cross-sections are E-W transects at 2.72°S, centered at 36°E (black dashed line in Fig. 1). a) Topography with  $10 \times$  vertical exaggeration. b) Topography (black), estimated basin depths (blue) (Birt et al., 1997), and topography corrected for low-density basin fill (red dashed) with  $2\times$  vertical exaggeration. c) Analytical model of topographic loading (as in b) colored by stress magnitude (positive stress values are compressive). Line segments (blue on c and black elsewhere) are orientations of the principal stress (greatest compressive),  $\sigma_1$ . d–i) Numerical models of separate stress contributions of each rift component colored by stress magnitude. Stresses are deviations in gravitational stress  $(g = 9.78 \text{ m/s}^2)$  with respect to a reference model: a uniform-thickness three-layer model with no magmatic systems. Numerical models show the separate effects of d) surface topography, e) an intruded sill (density contrast, yellow ellipse), f) an overpressurized magma chamber (density contrast and outward pressure), g) the Moho topography of a thinned crust, h) the combined effects of the four above-mentioned components, and i) the combined effects of all components including a displacement boundary condition to represent regional extension. OL: Oldoinyo Lengai, NS: Naibor Soito, G: Gelai.

## <sup>106</sup> 3. Modeling approach and limitations

The crustal stress field is determined by the combination of stress-generating 107 mechanisms (e.g., topographic loads, magma overpressure) and stress-relieving 108 mechanisms (e.g., inelastic deformation, earthquakes). Here we focus on the 109 former and treat the location and orientation of dikes and faults, as well as 110 Global Navigation Satellite System (GNSS)-derived plate motion directions, 111 as stress indicators. Crustal stresses control the predominant orientation of 112 faults and the slip direction during earthquakes. Elastic stresses cycle phases 113 of stress accumulation from the action of tectonic forces, punctuated by re-114 lease events during major earthquakes. Constraining the pattern of elastic 115 stresses at the regional, "tectonic environment" scale can help us understand 116 these cycles and any stress rotation occurring. 117

To investigate first-order stress contributions of different components, we 118 use present-day constraints for model geometry and evaluate static elastic 119 stress models. With elastic models, we take advantage of linear superpo-120 sition, wherein the net response to various components is the sum of the 121 individual responses. This enables us to investigate each component of inter-122 est separately, while also being able to superimpose them to see the combined 123 effect. Note that because time is an important aspect of ductile behavior, 124 our static models cannot capture time-dependent rheological behavior. 125

In our models, we do not include faults as discontinuities and instead only consider the influence of surface topography, magma bodies, and crustal thinning to the stresses on a continuous crustal model. Faults both respond to and influence stress orientations, and modeling this feedback is difficult to capture in a static model and would be more appropriately done in a separate dynamic modeling study. In addition, long-wavelength gravitational loads
(such as those considered in this study) would dominate the short-wavelength
effect of faults, except the largest faults (e.g., Maccaferri et al., 2014).

The abovementioned modeling decisions enable us to evaluate the state-134 of-stress within the continental crust, specifically the stress contributions of 135 topography, crustal thinning, and magma bodies. Our goal is to quantify 136 the resulting spatial stress patterns, to summarize first-order effects, and 137 discuss the implications of our findings on the evolution of magmatic and 138 fault systems. Our goal is not to simulate the detailed state-of-stress within 139 the Natron-Magadi system. Hence, we avoid additional model complexities 140 to ensure that the first-order effects we are interested in are not obscured. 141 While viscous stresses are certainly important in the long-term evolution 142 of the system, in the short timescales of earthquakes and dikes, the elastic 143 component of the stresses are more important. The caveat is that our results 144 are generally limited to the strong part (~upper crust) of the lithosphere, 145 where viscous effects are less important. 146

### 147 4. Methods

## 148 4.1. Model geometry

Our 2D models are about 200 km across and 100 km deep, and the 3D models are about 200 km  $\times$  200 km  $\times$  100 km (Fig. 1c,d). We only interpret the results within a smaller 100 km ( $\times$  100 km)  $\times$  50 km box embedded within the larger domain to avoid effects due to boundary conditions (see dashed white box on Fig. 1b). The model geometry was built from the Shuttle Radar Topography Mission (SRTM) 90m digital elevation database

	Depths	ho	Vs	Vp	$\lambda$	$\mu$
Layer	$(\mathrm{km})$	$\left(\mathrm{kg}/\mathrm{m}^3\right)$	$(\rm km/s)$	$(\rm km/s)$	$(\times 10^{10})$	$(\times 10^{10})$
upper crust	$0\!-\!18$	2761	3.6	6.2	3.46	3.58
lower crust	18 - 22	2833	3.4	6.5	5.38	3.29
mantle	22 - 100	3300	4.5	8.1	8.29	6.68
sill	${\sim}7$	2661	3.6	6.2	3.33	3.45
chamber	15 - 25	2661	3.3	5.5	2.25	2.90

Table 1: Material properties. First-order crustal densities ( $\rho$ ) were estimated from seismic velocities (Vp, Vs) (Plasman et al., 2017; Roecker et al., 2017; Tiberi et al., 2018), using an empirical relation between crustal density and seismic velocity (Brocher, 2005). The mantle velocity and density were adapted from the velocity models of Plasman et al. (2017) and Tiberi et al. (2018). Sill and magma chamber velocities are taken from Roecker et al. (2017). Lamé parameters are calculated from density and seismic velocities:  $\mu = \rho V s^2$ ;  $\lambda = \rho V p^2 - 2\mu$ .

v.4 (Jarvis et al., 2008), estimated basin depths from refraction and wideangle reflection data (Birt et al., 1997), and crustal tomography (Roecker
et al., 2017). The Moho structure was constrained from receiver functions
(Plasman et al., 2017) assuming a velocity contrast at 18 km (Plasman et al.,
2017; Roecker et al., 2017) and that unstretched crust is 40 km thick (Mansur
et al., 2014; Tugume et al., 2012).

## 161 4.2. Analytical models

We first modeled topography and extension using analytical 2D models. Because our study area sits at the edge of the uplifted Tanzanian craton and we do not include dynamic topography in the models, we removed a longwavelength trend from the SRTM topography. Detrended topography with adjustments based on lower density basin fill (dotted red line, Fig. 2b) was modeled analytically as a line load in an elastic 2D half-space (e.g., Dahm, 2000). Basin-fill adjustments were made such that the surface load of the adjusted topography with uniform density ( $\rho = 2.7 \text{ g/cm}^2$ ) is equivalent to that of original topography with lower-density basins ( $\rho = 2.55 \text{ g/cm}^2$ , Birt et al. (1997)).

#### 172 4.3. Numerical models

The 2D and 3D finite-element (FE) models were built using the mesh-173 ing software Trelis and modeled with regional extension and gravity using 174 the open-source lithospheric modeling package PyLith (Aagaard et al., 2013, 175 2017a,b). PyLith was specifically designed for the solution of tectonic prob-176 lems, and is capable of solving static, quasi-static, and dynamic problems in 177 geophysics. We do not consider time and thermomechanical effects in our 178 modeling efforts, and we therefore restrict our models to static elastic simu-179 lations without faults. Sample Trelis and PyLith input files are provided in 180 Supplementary materials SM3–SM4. 181

#### 182 4.3.1. Mesh generation

In 2D models, we mesh with quadrilateral elements (paving) with a mesh size of 0.5 km within the crust and the magma chamber, 0.2 km within the sill, and 0.8 km in the mantle. In 3D models, we mesh with tetrahedral elements and implement adaptive meshing to create a mesh with finer spacing along areas of interest that gets coarser towards the lateral and bottom boundaries. We use Trelis' bias sizing function to produce gradients of mesh size that respect the predefined discretization size along curves (see Supplementary material SM2). The discretization size is set to 1 km along the surface
topography, 1 km along the magma chamber boundary, 0.2 km along the sill
boundary, 2.5 km along the interface at 18 km depth, 5 km along the Moho,
and 10 km at the bottom of the model.

#### 194 4.3.2. Material parameters

Using an empirical relation between crustal density and seismic velocity 195 (Brocher, 2005), the first-order crustal densities were estimated from seismic 196 velocities (Plasman et al., 2017; Roecker et al., 2017; Tiberi et al., 2018). 197 The mantle velocity and density were adapted from the velocity models of 198 Plasman et al. (2017) and Tiberi et al. (2018). In the cases with the sill 199 and the magma chamber, magma density was taken to be slightly lower than 200 surrounding rock with seismic velocities taken from Roecker et al. (2017), 201 which imposes a buoyancy effect on the models. Although temperature, 202 pressure, composition, and hydration state also influence density, seismic 203 velocity, and rheology (e.g., Guerri et al., 2015), these are not considered 204 in this study; that is, the elastic parameters (Lamé constants) used in the 205 numerical model were calculated using density and seismic velocities only 206 (Table 1). Because the static models do not include the time component, 207 ductile behavior is not captured (e.g., Maccaferri et al., 2014). 208

#### 209 4.3.3. Initial and boundary conditions

We first evaluated separate stress contributions of each rift structure, then later combined them all together. Stress contributions were calculated as deviations in gravitational stress (with acceleration due to gravity g = 9.78 $m/s^2$ ) with respect to the assumed lithostatic equilibrium state of a reference

model (Fig. 1d, see Supplementary material Fig. SM1): a uniform-thickness 214 three-layer model with no magmatic systems and no topographic variations 215 (z = 0 on Fig. 2a). Topography and crustal thinning were represented by 216 modifications to the model geometry. The upper-crustal sill was modeled as 217 an ellipsoid 500 m thick, circular in plan-view (major axis of 5 km), centered 218 at 7 km depth. The mid-crustal magma chamber, which likely consists of 219 geometrically complex zones of mush and melt (Cashman et al., 2017), was 220 modeled as a 10 km thick, 20 km wide spheroidal inclusion, centered at 20 221 km depth, with an outward-directed pressure boundary condition of 10 MPa 222 to represent inflation (Allmann and Shearer, 2009). 223

For all models, a roller boundary condition was imposed on the bottom 224 of the block and a free surface on the top. For models without extension, 225 the lateral boundaries had a zero-displacement boundary condition. For 226 extensional models, five meters of displacement was imposed on each lateral 227 side,  $2.5 \times 10^{-5}$  of strain, which corresponds to ~3 MPa horizontal upper 228 crustal stress. The choice of imposed stresses is guided by the assumption 220 that deviatoric stresses significantly larger than 10 MPa would be released 230 by earthquakes, since 10 MPa is the global median stress drop associated 231 with earthquakes (Allmann and Shearer, 2009). 232

In 2D models, plane strain is assumed. No discontinuity or weakness is introduced to represent the known faults, since we treat faults as stress indicators rather than stress-generating structures.

### 236 4.3.4. Post-processing

Principal stress orientations are calculated from total stress values whereas
 stress magnitudes are relative to the assumed lithostatic equilibrium state of

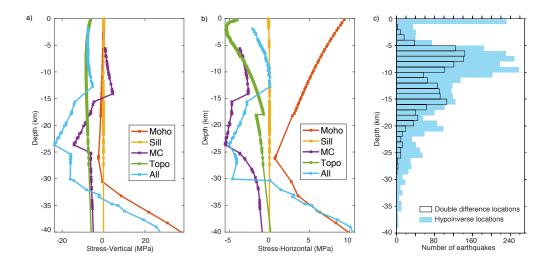


Figure 3: One-dimensional profiles from 2D static models. a) Vertical stresses along the 1D depth profile (green dashed line on Fig. 1c) with the stresses from a reference model subtracted. Initial stress state is assumed to be that of the reference model: a uniform-thickness three-layer model with no magmatic systems. Model values, marked with  $\times$ 's along the lines, are taken within 100 meters of the profile (x = 2750 m, where x = 0 is 36° longitude). Topo: topography model (Fig. 2d), Sill: sill model (Fig. 2e), MC: magma chamber model (Fig. 2f), Moho: thinned crust model (Fig. 2g), All: all-components model (Fig. 2h). b) Corresponding horizontal stresses along the 1D depth. c) Depth histogram of earthquakes in the study area from Weinstein et al. (2017).

the reference model (see Supplementary material SM5). The greatest compressive stress,  $\sigma_1$ , is taken as a proxy for preferred orientation of magmatic intrusions which is perpendicular to the preferred opening direction. The orientation of the least compressive stress ( $\sigma_3$ ) is comparable to the T-axis of earthquake focal mechanisms or the regional extensional GNSS direction. Model results are viewed using the open-source visualization software ParaView 5.7.

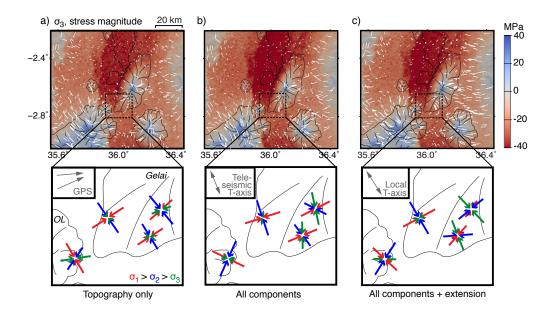


Figure 4: Depth slices of principal stresses in the upper crust (0–18 km depth)
These are 3D model results of a) topography only, b) all components together, c) all components together with extension. The top row are colored by stress magnitudes with white lines representing the least compressive stress orientations (σ<sub>3</sub>), where dots represent a line coming off the page or vertical. The bottom row shows 3D principal stress orientations (projected to 2D onto the map) in the Naibor Soito region along with other stress markers from Fig. 1 on the top left corner for comparison. σ<sub>1</sub>: greatest compressive stress; σ<sub>2</sub>: intermediate compressive stress.

## 246 5. Results

## 247 5.1. Topography and validation of finite-element model

The 2D analytical model of topographic loading (Fig. 2c) reveals stress 248 concentrations beneath the basin where sills or horizontal magma storage 249 may be favored (greatest compressive stresses are horizontal) (e.g., Maccaferri 250 et al., 2014). The corresponding numerical model (Fig. 2d) reveals similar 251 patterns of stress concentrations but with smaller stress amplitudes, due to 252 the material and domain constraints in the numerical model that do not exist 253 in the half-space of the analytical model. The similarities between Figs. 2c 254 and 2d help us validate the numerical model. In the analytical models, the 255 effect of the lower-density basin fill is minimal (black vs. dashed red line on 256 Fig. 2b are nearly coincident) hence the basin-fill density correction is not 257 considered in succeeding models. 258

The topography-driven preferred region (shallow red areas in Figs. 2c,d) 250 for melt storage beneath the basin is focused to a narrow region between the 260 Natron rift flank on the west and the Gelai volcanic edifice on the east. The 261 local topography creates a path of likely intrusion propagation ( $\sigma_1$ , black 262 lines on Fig. 2) from beneath the basin towards the flanks of Gelai, similar 263 to the models of off-rift volcanism of Maccaferri et al. (2014); that is, if there 264 were magma at  $\sim 10$  km depth between OL and NS, it might intrude to 265 shallower depths tracing along the  $\sigma_1$  direction (black lines) towards Gelai 266 to the east or towards OL to the west. This topographic loading effect is 267 focused in the shallow crust, to a depth that scales with the length scale of 268 the loading/unloading. For example, in the cross-section of the analytical 2D 269 model (Fig. 2c), we see that the wide basin effect ( $\sim 80$  km wide) reaches 40 270

km depth, although the highest stresses due to the topographic depression 271 between the border fault and Gelai ( $\sim 15$  km wide) are limited to < 20 km 272 depth. On Fig. 3a, we observe that vertical strain due to topography peaks 273 at  $\sim 10$  km depth. The lateral shift from zero of the entire topographic effect 274 profile is arbitrary and depends on the assumed height of the reference model, 275 and so for example, we can shift the profile to the right such that topographic 276 stress is zero at the base of unrifted crust (40 km thick) (e.g., Roman and 277 Jaupart, 2014). 278

## 279 5.2. Subsurface magmatic system

Both the sill and magma chamber produce a similar principal stress pat-280 tern with near-vertical  $\sigma_1$  above them, but the stresses are about an order of 281 magnitude apart, mainly due to the difference in size and magma pressure. 282 For the sill, the stress perturbation is only due to the density difference which 283 produces an upwards buoyancy push, but the stress magnitude is very small 284 compared to all the other components considered in the study (Fig. 2e). For 285 the magma chamber, in addition to the buoyancy effect, inflation adds an 286 outward-directed pressure (Fig. 2f). Vertical  $\sigma_1$  above the magma bodies cre-287 ates a possible pathway for magma to reach the surface, where diking may 288 be preferred. 289

## 290 5.3. Thinned crust

High-density mantle material replaces stretched continental crust that is 470 kg/m<sup>2</sup> lighter, imposing a downward pull on the system proportional to the crustal thinning (Fig. 2g). Crustal thinning has a long wavelength (riftwidth scale) thereby affecting a larger region of the model, compared to the high-frequency spatial variation of topography and smaller size of the magma bodies. The vertical  $\sigma_1$  beneath the crust and horizontal  $\sigma_1$  at the bottom of the crust suggest that stresses induced by crustal thinning may facilitate ponding of mafic magma around the Moho (e.g., Thybo and Artemieva, 2013; Maccaferri et al., 2014).

## <sup>300</sup> 5.4. All components in 2D models

After testing each component separately, we create a model with all 301 the components – topography, magma chamber, sill. Without extension 302 (Fig. 2h), the 2D model has the recognizable stress patterns produced by the 303 thinned crust, the inflated magma chamber, and the topography. Adding 304 extension (Fig. 2i) noticeably changes the orientations of the greatest com-305 pressive stress. At shallow depths just beneath the Naibor Soito monogenetic 306 cone complex and Gelai volcano,  $\sigma_1$  is vertical, where it was near-horizontal 307 without extension, suggesting that the large-scale heterogeneities (Moho, 308 magma chamber, topography) facilitate localization of extensional stress and 309 indicating the importance of taking into consideration the regional exten-310 sional setting in models. 311

On a one-dimensional profile of vertical stress (Fig. 3a), topography has 312 the largest effect close to the surface, showing negative stresses in our models 313 since topography at the location is below zero, hence lower than the refer-314 ence model. The magma chamber inflation has a large effect near the magma 315 chamber but becomes negligible within a few km distance farther away (Ro-316 man and Jaupart, 2014). The sill effect is negligible. The thinned crust 317 imposes a large stress at the bottom of the crust that gradually decreases 318 towards the surface. The horizontal stresses are smaller than the vertical 319

stresses, except for the rift-wide effect of the thinned crust which introduces a horizontal stress that is comparable to the vertical stresses. However when extension is added to the system, the effect of the thinned crust on the horizontal stresses close to the surface is lessened, as also observed in Fig. 2i.

### 324 5.5. Stress orientations in 3D

The similarity between principal stress orientations due to topography only (Fig. 4a) and all components (Fig. 4b) suggests that either 1) topography exerts the dominant stress field in the shallow upper crust, or 2) the most dominant stress-generating mechanisms considered contribute similarly-oriented stresses, especially away from southern Gelai and the Ngorongoro crater region. Beneath Lake Natron,  $\sigma_3$  is near-vertical, and is probably mainly controlled by basin topography and crustal thinning.

On the southern flank of Gelai, topography alone without extension pro-332 duces a stress field with  $\sigma_3$  oriented NE–SW (Fig. 4a). Adding the subsurface 333 effects, the direction of  $\sigma_3$  becomes roughly N-S in southern Gelai (Fig. 4b), 334 and with extension the  $\sigma_3$  orients close to NW-SE (Fig. 4c), which is con-335 sistent with the local extensional (T-axis) direction in previous seismicity 336 studies (Reiss et al., 2021; Weinstein et al., 2017). The agreement with local 337 stress rotation observed from the recent local seismicity studies as well as 338 teleseismically-detected earthquakes since 1964 in the Global Centroid Mo-339 ment Tensor catalog suggest that subsurface effects and extension play an 340 important role in the crustal state-of-stress. 341

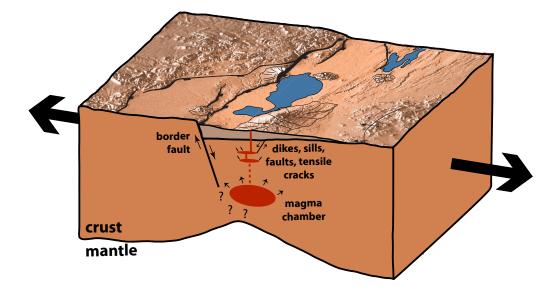


Figure 5: Schematic diagram of early-stage rifting. In addition to topographic loading, the subsurface density gradients from a thinned crust and the crustal magmatic complex also alter the stress field at depth. GNSS measurements constrain surface motions but do not represent strain at depth; they measure surface displacements. Thus, they are most sensitive to shallow stress fields and not deeper processes unless of greater magnitude, and generally are too sparse to provide information on deeper processes. Seismicity provides a better constraint on the stress field (strain field) at depth. Among the rift components considered in this study, surface topography and extension influences the shallow stress field the most (~upper crust), but at depth (~lower crust), subsurface density contrasts play a larger role. These large subsurface stresses may be overlooked when only considering surface-motion constraints but are key to a holistic three-dimensional understanding of rift tectonics.

## 342 6. Discussion

## 343 6.1. Three-dimensional rift tectonics

Stresses vary with depth, notably near-surface stresses differ from that 344 of the rest of the upper crust and the lower crust (Fig. 3a,b). We note that 345 topography has a significant influence on shallow vertical stresses, but subsur-346 face components strongly affect deeper stresses and these cannot be ignored 347 (Fig. 5). Surface observations, such as GNSS and Interferometric Synthetic 348 Aperture Radar (InSAR) data, and surface lineaments, are most sensitive to 349 shallow stress fields and not deeper processes except those of greater magni-350 tude. Hence, considering only surface constraints on plate motion paints a 351 two-dimensional picture of rifting that underestimates subsurface stress con-352 trols on the system. In addition, at the shallow level there are sedimentary 353 basins that provide complexity through additional processes such as com-354 paction, dewatering, and fluid overpressure. These processes influence near-355 surface stress fields, which factor in strongly in near-surface observations, but 356 may not be representative of deeper, regional, tectonic-level processes. Most 357 of the earthquakes in the study region are in the upper crust, from 5–15 km 358 depths (Weinstein et al., 2017) (Fig. 3c), and hence provide stress constraints 350 at depth, which are highly complementary with surface observations. 360

## <sup>361</sup> 6.2. Rift evolution and strain transfer

Border faults form very early during rift initiation and may reach a maximum length largely determined by the thickness of strong lithosphere (e.g., Jackson and Blenkinsop, 1997; Ebinger et al., 1999). New faults, called transfer faults, may form to link initially discrete border faults and rift segments

into a contiguous system. Results of this study suggest that local changes in 366 the stress field caused by the topographic loads, presence of crustal magma 367 reservoirs, and evolution of crustal stretching within the system determine 368 the orientation and evolution of these transfer fault systems. The local stress 369 field influences where magmatism develops. For example, intrabasinal vol-370 canic centers form in the high-strain accommodation zone. But it is im-371 portant to note that once the magmatic systems are formed, they in turn 372 impose their own stresses on the region and provide a local stress control 373 where new faults and magmatic systems might develop, creating a feedback 374 loop. Hence, geometric rift segment linkage models that do not consider the 375 magmatic system (e.g., Acocella et al., 2005) may not be applicable in some 376 magmatic rift zones. 377

The Natron basin sits at a transition zone, between the Kenya rift to the 378 north which has central volcanoes along the rift axis, and the study region 379 where there are no central rift volcanoes. In the Magadi basin, intra-rift 380 faults accommodate 67–80% of regional extension, whereas in the Natron 381 basin, the border faults accommodate >69% of the extension (Muirhead 382 et al., 2016). The local changes to the stress field in the Natron area can 383 guide fluids that move up the plate and could be indicative of the mechanism 384 by which strain begins to localize intra-rift to the central depression during 385 early-stage rifting. The  $\sim 10$ -km crustal thinning imposes the largest stresses. 386 especially horizontal stresses, but the feature generally follows the rift axis 387 and so it cannot produce a local stress rotation (see Supplementary mate-388 rial Fig. SM2). Instead, the local stress rotation could be produced by the 389 interplay between the volcanic edifices and the subsurface magmatic system. 390

The distribution and presence of magma within the crust contributes more to stresses at depth, whereas the loading effect of volcanic edifices is largest at shallow depths. The magmatic system (surface and subsurface) induces a local stress field rotation that might allow extensional faults or dikes to form at rift-oblique angles, which then later facilitate rift linkage between segmented basins and strain migration towards intra-rift faults where magma intrusion accommodates a larger percentage of extension.

## 398 7. Conclusions

Using physics-based numerical models, constrained by data and com-399 pared to analytical models, we explore the effects of different rift loading 400 components on the crustal state-of-stress. Models suggest that a local stress 401 field rotation to NW–SE extension (T-axis) from the regional  $\sim$ E-W exten-402 sion (from GNSS) can be due to the combined top loading from topography 403 and bottom loading from magma chamber inflation. We find that topo-404 graphic loading governs shallow upper crustal stresses but subsurface com-405 ponents (magma bodies, crustal thinning) can strongly influence lower crustal 406 stresses, which in turn may guide the location and upward path of magma 407 intrusion. The magmatic system (surface and subsurface) in an early-stage 408 rift provides a mechanism (local stress rotation) for later rift linkage between 409 segmented basins and strain migration towards the central rift zone. Studies 410 constrained only by surface observations underestimate stresses from crustal 411 thinning and lower crustal magmatic systems. Inclusion of the internal and 412 subsurface loads provides new insights into strain and magma migration dur-413 ing rift evolution. 414

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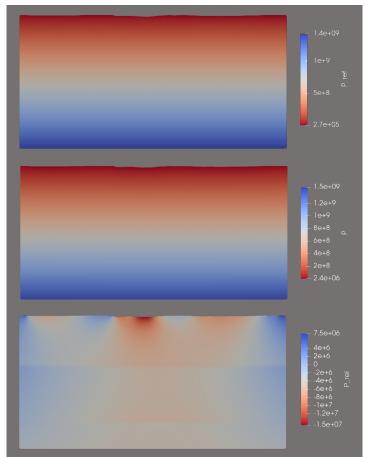
### Supplementary material of

# State of stress and stress rotations: Quantifying the role of surface topography and subsurface density contrasts in magmatic rift zones (Eastern Rift, Africa)

S. J. Oliva, C. J. Ebinger, E. Rivalta, C. A. Williams, C. Wauthier, C. Currie

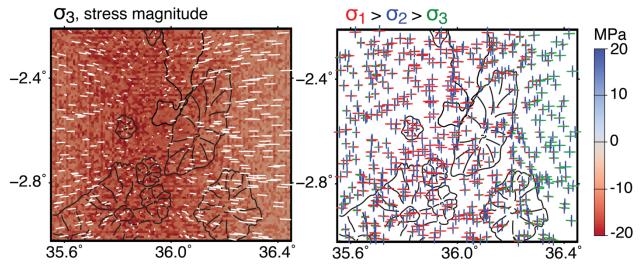
## Contents of this file:

- SM1 Figure: Gravitational stresses due to reference model
- SM2 Figure: Map view of stresses due to crustal thinning
- SM3 Trelis input for 2D and 3D model geometry and meshing
- SM4 General PyLith parameters (pylithapp.cfg)
- SM5 Post-processing calculations



**Figure SM1.** The top figure (P\_ref) shows the gravitational stresses of the reference model, a uniform-thickness three-layer model with no magmatic systems. The middle figure (P) shows the stresses due to topography – note that the gravitational stresses dominate and obscure any stress patterns due to topography. Hence, we subtract the assumed initial stress state corresponding to the reference model (P\_ref) from our models of different components (P) to obtain the stress

patterns that we interpret in the figure (P\_rel, bottom figure). All three figures have color bars scaled to the data range. The bottom figure is equivalent to Fig. 2d, but in the main text all color bars are centered at zero.



**Figure SM2.** 3D modeling of crustal thinning: Left panel is colored by stress magnitude with while lines representing the least compressive stress orientations (sigma 3), where dots represent a line coming off the page or vertical. Right panel shows the 3D principal stress orientations, projected to 2D onto the map. Note that sigma 1 is oriented E-W, sigma 2 is N-S, and sigma 3 is near-vertical along the rift basin. With the principal stress orientations generally aligned rift-parallel, rift-perpendicular, and vertical, we conclude that the crustal thinning cannot produce the map-view 60-degree local stress rotation observed from focal mechanisms.

## SM3. Geometry and Mesh

Below we include the Trelis codes (.jou) to create the geometry and build the mesh of the complete model that includes all components (topography, moho, sill, magma chamber) in 2D and 3D.

```
# 2D Geometry
# ------
# -*- Python -*- (syntax highlighting)
# ------
reset
${Units('si')}
# ------
# Import Topo and Moho curves
# ------
import Acis "curve_moho.sat"
import Acis "curve_topo_272_100m_detrendzero.sat"
# ------
# Create surface using vertices
# -------
${domainW=300.0*km}
${domainH=110.0*km}
```

```
create vertex {-0.5*domainW} {-domainH+10.0*km}
                                           0.0
${idVSbegin=Id("vertex")}
create vertex {-0.5*domainW} {10.0*km} 0.0
create vertex {+0.5*domainW} {10.0*km} 0.0
create vertex {+0.5*domainW} {-domainH+10.0*km} 0.0
${idVSend=Id("vertex")}
create surface vertex {idVSbegin} to {idVSend}
# _____
# Create material interface surfaces
# _____
# Magma chamber
create vertex {5.5*km} {-20.0*km} 0.0
${idVCirc=Id("vertex")}
create curve arc center vertex {idVCirc} radius {10.0*km} full
curve 7 name "chamber"
surface chamber scale x 1 y 0.5 about {5.5*km} {-20*km}
imprint surface 1 with curve chamber
# Constant thickness crust
${ucrustD=18.0*km}
create vertex {-0.5*domainW} {-ucrustD} 0.0
${idVM1=Id("vertex")}
create vertex {+0.5*domainW} {-ucrustD} 0.0
${idVM2=Id("vertex")}
create curve vertex {idVM1} vertex {idVM2} on surface 2
imprint surface 2 with curve 9
# Split across Moho curve
split curve 17 crossing curve moho
split curve 18 crossing curve moho
imprint surface 5 with curve moho
# Split across topo curve
split curve 11 crossing curve topo
split curve 12 crossing curve topo
imprint surface 4 with curve topo
delete surface 8
# Sill complex
create vertex {0.0*km} {-7.0*km} 0.0
${idVertex1=Id("vertex")}
create vertex {2.5*km} {-6.75*km} 0.0
${idVertex2=Id("vertex")}
create vertex {2.5*km} {-7.0*km} 0.0
${idVertex3=Id("vertex")}
create curve vertex {idVertex1} vertex {idVertex2} vertex {idVertex3} ellipse first
angle 0 last angle 360
curve 29 name "sill"
imprint surface 9 with curve sill
surface 11 name "s ucrust"
surface 6 name "s lcrust"
surface 7 name "s mantle"
surface 10 name "s sill"
surface 3 name "s chamber"
# ____
      _____
# Name geometric entities for use in meshing.
# _____
curve 28 name "c_topo"
#curve 6 name "c conrad"
#curve 15 name "c_moho"
```

```
curve 6 name "c_bottom"
curve 30 name "c sill"
curve 14 name "c chambertop"
curve 15 name "c_chamberbottom"
curve 16 name "c_chamberright"
curve 24 name "c_ucrust_xneg"
curve 27 name "c_ucrust_xpos"
curve 22 name "c_lcrust_xneg"
curve 19 name "c lcrust xpos"
curve 21 name "c mantle xneg"
curve 20 name "c_mantle_xpos"
delete vertex all
# End of file
# 2D Mesh
# _____
# -*- Python -*- (syntax highlighting)
# _____
# _____
# Set discretization size
# _____
surface all size {1.0*km}
surface s sill size {0.2*km}
surface s chamber size {0.5*km}
surface s_ucrust size {0.5*km}
surface s_lcrust size {0.5*km}
surface s mantle size {0.8*km}
# _____
# Generate the mesh
# _____
delete mesh
surface all scheme pave
mesh surface all
# _____
# Smooth mesh to improve quality
# _____
surface all smooth scheme condition number beta 1.3 cpu 10
smooth surface all
# _____
# Create blocks for materials
# _____
block 1 surface s ucrust
block 1 name "ucrust"
block 2 surface s lcrust
block 2 name "lcrust"
block 3 surface s mantle
block 3 name "mantle"
block 4 surface s sill
block 4 name "sill"
block 5 surface s chamber
block 5 name "chamber"
```

```
# _____
# Create nodeset for +x edge
# _____
group "boundary xpos" add node in curve c ucrust xpos
group "boundary_xpos" add node in curve c_lcrust_xpos
group "boundary_xpos" add node in curve c_mantle_xpos
nodeset 20 group boundary_xpos
nodeset 20 name "boundary xpos"
# _____
# Create nodeset for -x edge
# _____
group "boundary_xneg" add node in curve c_ucrust_xneg
group "boundary_xneg" add node in curve c_lcrust_xneg
group "boundary_xneg" add node in curve c_mantle_xneg
nodeset 21 group boundary_xneg
nodeset 21 name "boundary xneg"
# _____
# Create nodeset for +y edge
# _____
group "boundary_ypos" add node in curve c_topo
nodeset 22 group boundary_ypos
nodeset 22 name "boundary ypos"
# _____
# Create nodeset for -y edge
# _____
group "boundary yneg" add node in curve c bottom
nodeset 23 group boundary_yneg
nodeset 23 name "boundary yneg"
# _____
# Create nodeset for sill complex
# _____
group "boundary_sill" add node in curve c sill
nodeset 24 group boundary sill
nodeset 24 name "boundary sill"
# _____
# Create nodeset for magma chamber
# _____
group "boundary_chamber" add node in curve c_chambertop group "boundary_chamber" add node in curve c_chamberbottom
group "boundary chamber" add node in curve c chamberright
nodeset 25 group boundary_chamber
nodeset 25 name "boundary chamber"
# _____
# Export exodus file
# _____
export mesh "mesh 2d mod6.exo" dimension 2 overwrite
# End of file
# 3D Geometry
# _____
# -*- Python -*- (syntax highlighting)
# _____
reset
${Units('si')}
# ------
# Create block
```

```
# _____
# Block is 250 km x 500 km x 62 km
${blockLength=200.0*km}
${blockWidth=190.0*km}
${blockHeight=110.0*km}
brick x {blockLength} y {blockWidth} z {blockHeight}
${idVol=Id("volume")}
# Translate block so top can be chopped with topography and so faults
# intersect upper surface rather than side.
fmoveX=0.0*km
${moveY=13.0*km} #topo centered at 2.72 S
#volume {idVol} move x {moveX} y {moveY} z {0.0*km}
volume {idVol} move x {moveX} y {moveY} z {-0.5*blockHeight+10.0*km}
# _____
                  _____
# Import topography.
# _____
import Acis "srtm 1km detrend/crafti topo detrend.sat"
# Scale topo, 1 km = 1000 m
surface 7 scale 1000
#save
# _____
# Webcut block with topography and delete volume lying above topography.
# _____
webcut volume {idVol} with sheet surface 7
delete volume 3
delete body 2
#save
# _____
# Divide upper crust, lower crust, and mantle
# _____
create planar surface with plane zplane offset {-18.0*km}
webcut volume 1 with sheet surface 18
# Magma chamber
create sphere radius {5*km}
${idSphere=Id("volume")}
volume {idSphere} move x {5.5*km} y 0 z {-20*km}
volume {idSphere} scale x 2 y 2 z 1 about \{5.5*km\} 0 \{-20*km\}
subtract volume 6 from volume 1 imprint keep
subtract volume 6 from volume 5 imprint keep
delete volume 1 5
# Sill
create sphere radius {0.5*km}
${idSphere=Id("volume")}
volume {idSphere} move x {2.5*km} y 0 z {-7*km}
volume {idSphere} scale x 10 y 10 z 1 about \{2.5*km\} 0 \{-7*km\}
subtract volume 9 from volume 7 imprint keep
delete volume 7
# Moho
import Acis "curve moho 3d.sat"
curve moho move x \overline{0} y {-90 \times \text{km}} z 0
webcut volume 8 sweep curve moho vector 0 1 0 distance {220*km}
delete body 4
delete curve moho
```

```
imprint all with volume all
merge all
delete vertex all
# ______
# Name geometric entities for use in meshing.
# _____
surface 49 name "topo"
surface 38 name "conrad"
surface 53 name "moho"
surface 43 name "sbottom"
surface 45 name "chambertop"
surface 37 name "chamberbottom"
surface 44 name "sill surf"
volume 10 name "ucrust"
volume 8 name "lcrust"
volume 11 name "mantle"
volume 6 name "chamber"
volume 9 name "sill"
surface 50 name "ucrust_ypos"
surface 51 name "ucrust_xneg"
surface 47 name "ucrust_yneg"
surface 48 name "ucrust_xpos"
surface 56 name "lcrust yneg"
surface 57 name "lcrust xpos"
surface 54 name "lcrust_ypos"
surface 55 name "lcrust xneg"
surface 61 name "mantle_yneg"
surface 62 name "mantle_xneg"
surface 59 name "mantle ypos"
surface 60 name "mantle xpos"
# End of file
# 3D Mesh
# _____
# -*- Python -*- (syntax highlighting)
# _____
                                 _____
# _____
# Set discretization size
# _____
surface topo size {1.0*km}
surface conrad size {2.5*km}
surface moho size {5.0*km}
surface sbottom size {10.0*km}
surface chambertop size {1.0*km}
surface chamberbottom size {1.0*km}
surface sill surf size {0.2*km}
# Sizing functions for faces surrounding upper crust.
surface ucrust xneg sizing function type bias start curve 95 finish curve 71
surface ucrust xpos sizing function type bias start curve 93 finish curve 73
surface ucrust_yneg sizing function type bias start curve 90 finish curve 72
surface ucrust ypos sizing function type bias start curve 94 finish curve 70
# Sizing functions for faces surrounding lower crust.
surface lcrust_xneg sizing function type bias start curve 71 finish curve 100
surface lcrust xpos sizing function type bias start curve 73 finish curve 102
```

```
surface lcrust_yneg sizing function type bias start curve 72 finish curve 99
surface lcrust_ypos sizing function type bias start curve 70 finish curve 101
# Sizing functions for faces surrounding mantle.
surface mantle_xneg sizing function type bias start curve 100 finish curve 78
surface mantle_xpos sizing function type bias start curve 102 finish curve 81
surface mantle yneg sizing function type bias start curve 99 finish curve 75
surface mantle ypos sizing function type bias start curve 101 finish curve 80
# _____
# Generate the mesh
# _____
                _____
delete mesh
volume all scheme tetmesh
mesh surface topo
mesh surface all except topo
mesh volume all
# _____
# Smooth mesh to improve quality
# _____
volume all smooth scheme condition number beta 2.0 cpu 3
smooth volume all
# _____
# Create blocks for materials
# _____
block 1 volume ucrust
block 1 name "ucrust"
block 2 volume lcrust
block 2 name "lcrust"
block 3 volume mantle
block 3 name "mantle'
block 4 volume sill
block 4 name "sill"
block 5 volume chamber
block 5 name "chamber"
# _____
# Create nodeset for +x edge
# _____
group "boundary xpos" add node in surface ucrust xpos
group "boundary_xpos" add node in surface lcrust_xpos
group "boundary_xpos" add node in surface mantle xpos
nodeset 30 group boundary_xpos
nodeset 30 name "boundary_xpos"
# _____
# Create nodeset for -x edge
# _____
group "boundary xneg" add node in surface ucrust xneg
group "boundary_xneg" add node in surface lcrust_xneg
group "boundary_xneg" add node in surface mantle_xneg
nodeset 31 group boundary_xneg
nodeset 31 name "boundary_xneg"
# _____
# Create nodeset for +y edge
# _____
group "boundary ypos" add node in surface ucrust ypos
group "boundary_ypos" add node in surface lcrust_ypos
```

```
group "boundary_ypos" add node in surface mantle_ypos
nodeset 32 group boundary ypos
nodeset 32 name "boundary ypos"
# _____
# Create nodeset for -y edge
# _____
"group "boundary_yneg" add node in surface ucrust_yneg
group "boundary_yneg" add node in surface lcrust_yneg
group "boundary_yneg" add node in surface mantle_yneg
nodeset 33 group boundary yneg
nodeset 33 name "boundary yneg"
# _____
# Create nodeset for +z edge
# _____
group "boundary_zpos" add node in surface topo
nodeset 34 group boundary_zpos
nodeset 34 name "boundary zpos"
# _____
# Create nodeset for -z edge
# _____
group "boundary_zneg" add node in surface sbottom
nodeset 35 group boundary zneg
nodeset 35 name "boundary zneg"
# _____
# Create nodeset for sill
# _____
group "boundary sill" add node in surface sill surf
nodeset 36 group boundary_sill
nodeset 36 name "boundary_sill"
# End of file
```

#### SM4. General PyLith parameters

Below is the pylithapp.cfg file used in 2D and 3D models.

```
# PyLith parameters for 2D models
# The settings in this file (pylithapp.cfg) will be read automatically
# by pylith, as long as the file is placed in the run directory.
# The settings in this file will override any settings in:
# PREFIX/etc/pylithapp.cfg
# $HOME/.pyre/pylithapp/pylithapp.cfg
# The settings in this file will be overridden by any .cfg file given
# on the command line or by any command line settings.
[pylithapp]
# _____
# journal
# _____
# The settings below turn on journal info for the specified components.
# If you want less output to stdout, you can turn these off.
[pylithapp.journal.info]
timedependent = 1
```

```
implicit = 1
petsc = 1
solverlinear = 1
meshiocubit = 1
homogeneous = 1
elasticityimplicit = 1
fiatlagrange = 1
pylithapp = 1
materials = 1
# _____
# mesh generator
# _____
# The settings below control the mesh generation (importing mesh info).
# Turn on debugging output for mesh generation.
[pylithapp.mesh generator]
debug = 1
reader = pylith.meshio.MeshIOCubit
# This component specification means we are using PyLith ASCII format,
# and we then specify the filename and number of space dimensions for
# the mesh.
[pylithapp.mesh generator.reader]
filename = mesh/mesh 2d mod1.exo
coordsys.space \dim = 2
# _____
# problem
# _____
          _____
# Specify the problem settings.
# This is a time-dependent problem, so we select this as our problem type.
# We select a total time of 0 sec, and a time step size of 1 sec, so we
# are performing a single time step.
# The spatial dimension for this problem is 2.
# For an implicit formulation (using implicit.cfg), we will perform 1
# implicit time step from t = -1.0 to t = 0.0 (elastic solution step).
[pylithapp.timedependent]
dimension = 2
formulation = pylith.problems.Implicit
formulation.solver = pylith.problems.SolverNonlinear
[pylithapp.timedependent.formulation.time step]
total time = 1.0*year
dt = \overline{1.0}*year
# _____
# materials
# _____
# Specify the material information for the problem.
# The material type is isotropic elastic formulated for plane strain.
[pylithapp.timedependent]
materials = [ucrust,lcrust,mantle]
[pylithapp.timedependent.materials]
ucrust = pylith.materials.ElasticPlaneStrain
lcrust = pylith.materials.ElasticPlaneStrain
mantle = pylith.materials.ElasticPlaneStrain
#[pylithapp.timedependent.materials.material]
# Upper Crust
[pylithapp.timedependent.materials.ucrust]
label = Elastic ucrust
```

```
# The id corresponds to the block number from CUBIT.
id = 1
db properties = spatialdata.spatialdb.SimpleDB
db properties.label = Elastic ucrust properties
db_properties.iohandler.filename = spatialdb/mat_ucrust_elastic.spatialdb
db properties.query type = nearest
# We are doing 2D quadrature for a triangle.
quadrature.cell = pylith.feassemble.FIATLagrange
quadrature.cell.dimension = 2
# Lower crust
[pylithapp.timedependent.materials.lcrust]
label = Elastic lower crust
# The id corresponds to the block number from CUBIT.
id = 2
db properties = spatialdata.spatialdb.SimpleDB
db properties.label = Elastic lcrust properties
db_properties.iohandler.filename = spatialdb/mat_lcrust_elastic.spatialdb
#db_properties.iohandler.filename = spatialdb/mat_lcrust_Maxwell.spatialdb
db properties.query type = nearest
# We are doing 2D quadrature for a triangle.
quadrature.cell = pylith.feassemble.FIATLagrange
guadrature.cell.dimension = 2
# Mantle
[pylithapp.timedependent.materials.mantle]
label = Elastic mantle
# The id corresponds to the block number from CUBIT.
id = 3
db properties = spatialdata.spatialdb.SimpleDB
db_properties.label = Elastic mantle properties
db_properties.iohandler.filename = spatialdb/mat_mantle_elastic.spatialdb
#db properties.iohandler.filename = spatialdb/mat_mantle_Maxwell.spatialdb
db properties.query type = nearest
# We are doing 2D quadrature for a triangle.
quadrature.cell = pylith.feassemble.FIATLagrange
guadrature.cell.dimension = 2
# _____
# output
# _____
                      _____
# Names of output files are set in stepXX.cfg. We consolidate all of the
# output settings that are common to all of the simulations here.
[pylithapp.timedependent.formulation]
# Set the output to an array of 2 output managers.
# We will output the solution over the domain and the ground surface.
output = [domain]
# Domain
[pylithapp.problem.formulation.output.domain]
vertex data fields = [displacement]
writer = pylith.meshio.DataWriterHDF5
# Materials
[pylithapp.timedependent.materials.ucrust.output]
writer = pylith.meshio.DataWriterHDF5
```

```
cell_data_fields = [stress,cauchy_stress,total_strain]
# Comment this out for if rerunning Step 3 to get initial conditions for Step 8.
cell filter = pylith.meshio.CellFilterAvg
[pylithapp.timedependent.materials.lcrust.output]
writer = pylith.meshio.DataWriterHDF5
cell data fields = [stress,cauchy stress,total strain]
# Comment this out for if rerunning Step 3 to get initial conditions for Step 8.
cell filter = pylith.meshio.CellFilterAvg
[pylithapp.timedependent.materials.mantle.output]
writer = pylith.meshio.DataWriterHDF5
cell data fields = [stress,cauchy stress,total strain]
# Comment this out for if rerunning Step 3 to get initial conditions for Step 8.
cell filter = pylith.meshio.CellFilterAvg
# _____
# PETSC
# ____
                             _____
# We are using all of the default settings for PETSc except for
# specifying the block Jacobi preconditioner. Additional PETSc
# command-line arguments may be found in the PETSc documentation.
[pylithapp.petsc]
# Preconditioner settings.
pc type = bjacobi
# Convergence parameters.
ksp rtol = 1.0e-50
ksp_atol = 1.0e-12
# Linear solver monitoring options.
ksp monitor = true
ksp converged reason = true
ksp_error_if_not_converged = true
# Nonlinear solver monitoring options.
snes rtol = 1.0e-50
snes atol = 1.0e-10
snes max it = 100
snes monitor = true
snes converged reason = true
snes linesearch monitor = true
snes error if not converged = true
# start in debugger = true
# debugger timeout = 100
# End of file
# PyLith parameters for 3D MODELS
# The settings in this file (pylithapp.cfg) will be read automatically
# by pylith, as long as the file is placed in the run directory.
# The settings in this file will override any settings in:
# PREFIX/etc/pylithapp.cfg
# $HOME/.pyre/pylithapp/pylithapp.cfg
# The settings in this file will be overridden by any .cfg file given
# on the command line or by any command line settings.
```

```
[pylithapp]
```

```
# _____
# journal
# _____
# The settings below turn on journal info for the specified components.
# If you want less output to stdout, you can turn these off.
[pylithapp.journal.info]
timedependent = 1
implicit = 1
petsc = 1
solverlinear = 1
meshiocubit = 1
homogeneous = 1
elasticityimplicit = 1
fiatsimplex = 1
pylithapp = 1
materials = 1
mesh distributor = 1
# _____
# mesh generator
# _____
              _____
# The settings below control the mesh generation (importing mesh info).
# Turn on debugging output for mesh generation.
[pylithapp.mesh_generator]
debug = 1
reader = pylith.meshio.MeshIOCubit
# This component specification means we are using PyLith ASCII format,
# and we then specify the filename and number of space dimensions for
# the mesh.
[pylithapp.mesh_generator.reader]
filename = ../mesh/mesh 3d mod6.exo
# _____
# problem
# _____
         _____
# Specify the problem settings.
# This is a time-dependent problem, so we select this as our problem type.
# We select a total time of 0 sec, and a time step size of 1 sec, so we
# are performing a single time step.
# The spatial dimension for this problem is 2.
# For an implicit formulation (using implicit.cfg), we will perform 1
# implicit time step from t = -1.0 to t = 0.0 (elastic solution step).
[pylithapp.timedependent]
dimension = 3
formulation = pylith.problems.Implicit
formulation.solver = pylith.problems.SolverNonlinear
[pylithapp.timedependent.formulation.time step]
total time = 1.0*year
dt = 1.0*year
# _____
# materials
# _____
                  _____
# Specify the material information for the problem.
# The material type is isotropic elastic formulated for plane strain.
[pylithapp.timedependent]
materials = [ucrust,lcrust,mantle,sill,chamber]
# Upper Crust
```

```
[pylithapp.timedependent.materials.ucrust]
label = Elastic ucrust
# The id corresponds to the block number from CUBIT.
id = 1
db properties = spatialdata.spatialdb.SimpleDB
db properties.label = Elastic ucrust properties
db_properties.iohandler.filename = ../spatialdb/mat ucrust elastic.spatialdb
db_properties.query_type = nearest
# We are doing 2D quadrature for a triangle.
quadrature.cell = pylith.feassemble.FIATSimplex
quadrature.cell.dimension = 3
# Lower crust
[pylithapp.timedependent.materials.lcrust]
label = Elastic lower crust
# The id corresponds to the block number from CUBIT.
id = 2
db properties = spatialdata.spatialdb.SimpleDB
db properties.label = Elastic lcrust properties
db_properties.iohandler.filename = ../spatialdb/mat_lcrust_elastic.spatialdb
db properties.query type = nearest
# We are doing 2D guadrature for a triangle.
quadrature.cell = pylith.feassemble.FIATSimplex
quadrature.cell.dimension = 3
# Mantle
[pylithapp.timedependent.materials.mantle]
label = Elastic mantle
# The id corresponds to the block number from CUBIT.
id = 3
db_properties = spatialdata.spatialdb.SimpleDB
db properties.label = Elastic mantle properties
db properties.iohandler.filename = ../spatialdb/mat mantle elastic.spatialdb
db properties.query type = nearest
# We are doing 2D quadrature for a triangle.
quadrature.cell = pylith.feassemble.FIATSimplex
quadrature.cell.dimension = 3
# Sill
[pylithapp.timedependent.materials.sill]
label = Elastic sill
# The id corresponds to the block number from CUBIT.
id = 4
db properties = spatialdata.spatialdb.SimpleDB
db properties.label = Elastic sill properties
db_properties.iohandler.filename = ../spatialdb/mat_magmanew_elastic.spatialdb
db properties.query type = nearest
# We are doing 2D quadrature for a triangle.
quadrature.cell = pylith.feassemble.FIATSimplex
guadrature.cell.dimension = 3
# Chamber
[pylithapp.timedependent.materials.chamber]
```

```
label = Elastic chamber
# The id corresponds to the block number from CUBIT.
id = 5
db_properties = spatialdata.spatialdb.SimpleDB
db properties.label = Elastic chamber properties
db properties.iohandler.filename = ../spatialdb/mat mush elastic.spatialdb
db properties.query type = nearest
# We are doing 2D guadrature for a triangle.
quadrature.cell = pylith.feassemble.FIATSimplex
quadrature.cell.dimension = 3
# _____
# output
# _____
# Names of output files are set in stepXX.cfg. We consolidate all of the
# output settings that are common to all of the simulations here.
[pylithapp.timedependent.formulation]
# Set the output to an array of 2 output managers.
# We will output the solution over the domain and the ground surface.
output = [domain]
# Domain
[pylithapp.problem.formulation.output.domain]
vertex data fields = [displacement]
writer = pylith.meshio.DataWriterHDF5
# Materials
[pylithapp.timedependent.materials.ucrust.output]
writer = pylith.meshio.DataWriterHDF5
cell data fields = [stress,cauchy stress,total strain]
# Comment this out for if rerunning Step 3 to get initial conditions for Step 8.
cell filter = pylith.meshio.CellFilterAvg
[pylithapp.timedependent.materials.lcrust.output]
writer = pylith.meshio.DataWriterHDF5
cell data fields = [stress, cauchy stress, total strain]
# Comment this out for if rerunning Step 3 to get initial conditions for Step 8.
cell filter = pylith.meshio.CellFilterAvg
[pylithapp.timedependent.materials.mantle.output]
writer = pylith.meshio.DataWriterHDF5
cell data fields = [stress,cauchy stress,total strain]
# Comment this out for if rerunning Step 3 to get initial conditions for Step 8.
cell filter = pylith.meshio.CellFilterAvg
[pylithapp.timedependent.materials.sill.output]
writer = pylith.meshio.DataWriterHDF5
cell data fields = [stress, cauchy stress, total strain]
# Comment this out for if rerunning Step 3 to get initial conditions for Step 8.
cell_filter = pylith.meshio.CellFilterAvg
[pylithapp.timedependent.materials.chamber.output]
writer = pylith.meshio.DataWriterHDF5
cell data fields = [stress,cauchy stress,total strain]
# Comment this out for if rerunning Step 3 to get initial conditions for Step 8.
cell_filter = pylith.meshio.CellFilterAvg
```

```
# _____
                     _____
# PETSC
# _____
# We are using all of the default settings for PETSc except for
# specifying the block Jacobi preconditioner. Additional PETSc
# command-line arguments may be found in the PETSc documentation.
[pylithapp.petsc]
malloc dump =
# Preconditioner settings.
pc type = asm
sub_pc_factor_shift_type = nonzero
# Convergence parameters.
ksp rtol = 1.0e-10
ksp atol = 1.0e-20
ksp_max_it = 1000
ksp gmres restart = 200
# Linear solver monitoring options.
ksp_monitor = true
ksp converged reason = true
ksp error if not converged = true
# Nonlinear solver monitoring options.
snes rtol = 1.0e-10
snes atol = 1.0e-9
snes max it = 100
snes monitor = true
snes converged reason = true
snes linesearch monitor = true
snes_error_if_not_converged = true
# PETSc summary -- useful for performance information.
log view = true
# End of file
```

#### SM5. Post-processing.

We subtract the gravitational stresses due to the reference model (SM1), and calculate principal stresses and pressure = (sigma1 + sigma2 + sigma3) / 3 using the python script shown below for the 3D case:

```
rhoLC = 2833.0
rhoM = 3300.0
vsUC = 3600.0
vsLC = 3400.0
vsM = 4500.0
vpUC = 6200.0
vpLC = 6500.0
vpM = 8100.0
g = 9.80665
z1 = -20000.0
z_2 = -40000.0
stressUC = rhoUC*g*z1
stressLC = rhoLC*g*(z2 - z1)
# Compute material properties.
muUC = rhoUC*vsUC*vsUC
muLC = rhoLC*vsLC*vsLC
muM = rhoM*vsM*vsM
lamUC = rhoUC*vpUC - 2.0*muUC
lamLC = rhoLC*vpLC*vpLC - 2.0*muLC
lamM = rhoM*vpM*vpM - 2.0*muM
def getCellCenters(vertices, cells):
    Function to compute cell centers.
   cellCoords = vertices[cells, :]
   cellCenters = numpy.mean(cellCoords, axis=1)
   return cellCenters
def generate(sim, fileRoot, materials):
    for material in materials:
        filenameH5 = "%s-%s.h5" % (sim, material)
        # Open HDF5 file and get coordinates, cells, and stress.
        h5 = h5py.File(filenameH5, "r")
        vertices = h5['geometry/vertices'][:]
        cells = numpy.array(h5['topology/cells'][:], dtype=numpy.int)
        filenewH5 = "%s-%s-pstresses.h5" % (sim, material)
        copyfile(filenameH5,filenewH5)
        h5new = h5py.File(filenewH5, "r+")
        # Get stresses from final time step.
        stress = h5['cell_fields/stress'][-1,:,:]
        refStress = numpy.zeros_like(stress)
        h5.close()
        # Compute coordinates of quadrature points.
        quadCoords = getCellCenters(vertices, cells)
        # Compute reference stress.
        z = quadCoords[:,2]
        coordsUC = numpy.where(z \ge z1)
        coordsLC = numpy.where(numpy.logical_and(z >= z2, z < z1))</pre>
        coordsM = numpy.where(z < z2)
        if (coordsUC[0].shape[0] != 0):
            refStress[coordsUC,0] = rhoUC*g*z[coordsUC]
        if (coordsLC[0].shape[0] != 0):
            refStress[coordsLC,0] = stressUC + rhoLC*g*(z[coordsLC]-z1)
        if (coordsM[0].shape[0] != 0):
            refStress[coordsM,0] = stressUC + stressLC + rhoM*g*(z[coordsM]-z2)
        refStress[:,1] = refStress[:,0]
```

```
refStress[:,2] = refStress[:,0]
        refStress *= -1.0
        pressureRef = (refStress[:,0] + refStress[:,1] + refStress[:,2])/3
        # Define square 3x3 array
        sigmal = [] # principal compressive stress, negative stress in PyLith
        sigma2 = []
        sigma3 = [] # principal tensile stress, positive stress in PyLith
        theta1 = []
        theta2 = []
        theta3 = []
        pressure = []
        for cell in stress:
            stresstensor =
numpy.array([(cell[0],cell[3],cell[5]),(cell[3],cell[1],cell[4]),(cell[5],cell[4],ce
11[2])])
        # Calculate principal stresses
            [w, v] = numpy.linalq.eigh(stresstensor)
            sigma1.append(w[0])
            sigma2.append(w[1])
            sigma3.append(w[2])
            theta1.append(v[:,0])
            theta2.append(v[:,1])
            theta3.append(v[:,2])
            pressure.append((w[0]+w[1]+w[2])/3)
        # Create pressure array as well as pressure minus reference model.
        pressure = numpy.array(pressure)
        pressureRel = pressure - pressureRef
        pressureRelneg = pressureRel*(-1)
        # change row vector to column vector
        sigmal = numpy.array(sigmal).reshape(-1,1)
        sigma2 = numpy.array(sigma2).reshape(-1,1)
        sigma3 = numpy.array(sigma3).reshape(-1,1)
        # add zero for z column
        theta1 = numpy.array(theta1)
        theta3 = numpy.array(theta3)
        theta2 = numpy.array(theta2)
        nrows = stress.shape[0]
        ncols = stress.shape[1]
        #dataset sigma = h5new.create dataset('cell fields/sigma', (1,nrows,3),
maxshape=(None,nrows,3), data=sigma)
        dataset sigma1 = h5new.create dataset('cell fields/s1', (1,nrows,1),
maxshape=(None,nrows,1), data=sigma1)
        dataset sigma2 = h5new.create dataset('cell fields/s2', (1,nrows,1),
maxshape=(None,nrows,1), data=sigma2)
        dataset sigma3 = h5new.create dataset('cell fields/s3', (1,nrows,1),
maxshape=(None, nrows, 1), data=sigma3)
        dataset theta1 = h5new.create dataset('cell fields/t1', (1,nrows,3),
maxshape=(None, nrows, 3), data=theta1)
        dataset theta2 = h5new.create dataset('cell fields/t2', (1,nrows,3),
maxshape=(None, nrows, 3), data=theta2)
        dataset_theta3 = h5new.create_dataset('cell_fields/t3', (1,nrows,3),
maxshape=(None, nrows, 3), data=theta3)
        dataset pressure = h5new.create dataset('cell fields/P', (1,nrows,1),
maxshape=(None, nrows, 1), data=pressure)
        dataset_pressure_ref = h5new.create_dataset('cell_fields/P_ref',
(1,nrows,1), maxshape=(None,nrows,1), data=pressureRef)
```

```
dataset_pressure_rel = h5new.create_dataset('cell_fields/P_rel',
(1,nrows,1), maxshape=(None,nrows,1), data=pressureRel)
        dataset pressure relneg = h5new.create dataset('cell fields/P relneg',
(1,nrows,1), maxshape=(None,nrows,1), data=pressureRelneg)
        #dataset_sigma.attrs.create(name='vector_field_type',data="tensor")
dataset_sigma1.attrs.create(name='vector_field_type',data="scalar")
dataset_sigma2.attrs.create(name='vector_field_type',data="scalar")
dataset_sigma3.attrs.create(name='vector_field_type',data="scalar")
        dataset_theta1.attrs.create(name='vector_field_type',data="vector")
        dataset theta2.attrs.create(name='vector field type',data="vector")
        dataset theta3.attrs.create(name='vector field type',data="vector")
        dataset_pressure.attrs.create(name='vector_field_type',data="scalar")
        dataset_pressure_ref.attrs.create(name='vector_field_type',data="scalar")
        dataset_pressure_rel.attrs.create(name='vector_field_type',data="scalar")
        dataset pressure relneg.attrs.create(name='vector field type',data="scalar")
        h5new.close()
    return
# _____
                   _____
                                      _____
if __name__ == "__main__":
    import argparse
    parser = argparse.ArgumentParser()
    parser.add_argument("--sim", action="store", dest="sim",
default="novel_grav_mod0")
    parser.add argument("--file-root", action="store", dest="fileRoot",
default="mat principal stress")
    parser.add argument("--materials", action="store", dest="materials",
default="ucrust,lcrust,mantle")
    args = parser.parse args()
    materials = args.materials.split(",")
    generate(args.sim, args.fileRoot, materials)
# End of file
```